

Welcome! Today, we hope to introduce you to Newton's Laws, as well as provide some practice problems to solve. There is a total of **32** points. Points indicate relative difficulty.

### Idea 1: Newton's First Law

Newton's 1st Law, also known as the law of inertia, states the following: **A body moves with constant velocity (which may be zero) unless acted on by a force.** Essentially, this law states that an object will not change velocity unless acted on by a force.

- [1] **Problem 1.** Use Newton's First Law to explain why you lean to the side when a car turns.

### Idea 2: Newton's Second Law

Newton's 2nd Law, also known as  $F = ma$ , states: **The rate of change of the momentum of a body equals the force acting on the body.** This is commonly referred to as the equation

$$F_{\text{net}} = ma$$

where  $F_{\text{net}}$  denotes the net force, and  $m$  and  $a$  denote mass and acceleration, respectively.

- [1] **Problem 2.** A 2 kg toy car is pushed with a net force of 10 N. What is the acceleration of the car?

### Idea 3: Newton's Third Law

Newton's 3rd Law states that **Given two bodies  $A$  and  $B$ , if  $A$  exerts a force on  $B$ , then  $B$  exerts an equal and opposite force on  $A$ .** We can call these action-reaction pairs, and it essentially says that things don't happen in isolation; if an object feels a force, then there must be another object somewhere feeling the opposite force.

- [1] **Problem 3.** Describe the action-reaction pairs at play when you are walking along the floor.

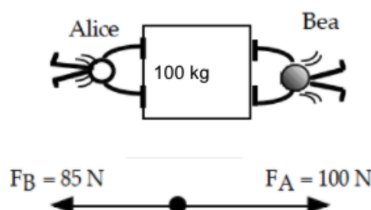
### Important Idea 1:

Be sure you understand how to draw and interpret a free body diagram! We aren't covering them today, but they are extremely important in physics so make sure you are comfortable with them.

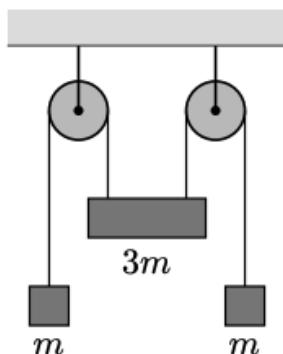
## 1 Practice Problems

- [3] **Problem 4.** Two people, Alice and Bea, are trying to push a 100 kg crate across the floor, but they are doing so very clumsily. The forces they exert are shown as viewed from above. The vertical forces ( $F_g$  and  $F_N$ ) cancel and are not shown. Find

- The net force and acceleration of the crate.
- Alice and Bea stop after pushing the crate for 100 seconds. How far, in meters, did they push the crate?
- Alice, instead of pushing towards eastward against Bea, starts pushing northbound with 100 N of force. Find the new net force and acceleration of the crate, including their directions.

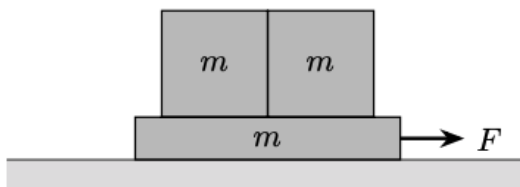


- [4] **Problem 5.** (2023 F=ma Problem 5) Two blocks of mass  $m$  and a block of mass  $3m$  are attached to a system of massless fixed pulleys and massless string, as shown.



Assume all surfaces are frictionless. In terms of  $g$ , find the acceleration of each mass  $m$ .

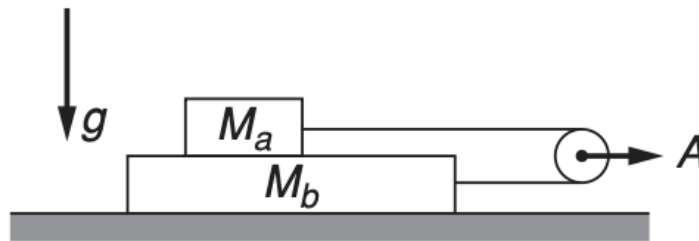
- [4] **Problem 6.** (2023 F=ma Problem 7) Two boxes are stacked side-by-side on top of a larger box as shown.



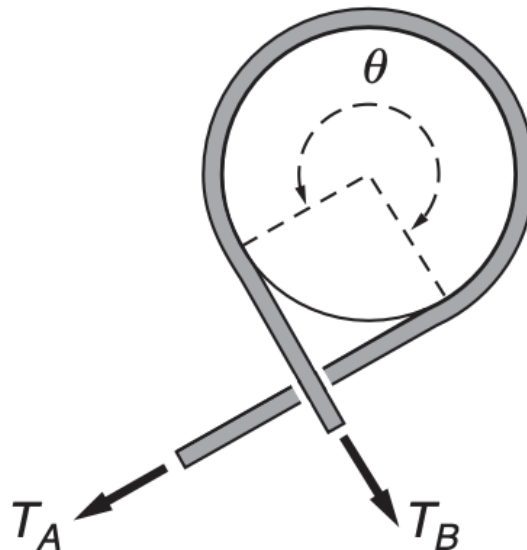
All three boxes have mass  $m$ , the coefficient of static friction between the left box and the bottom box is  $\mu_s$ , and all other surfaces are frictionless. A rightward force  $F$  is applied to the bottom box. In terms of  $F$ ,  $m$ , and  $g$ , find the minimum value of  $\mu_s$  so that the upper boxes don't slide.

## 2 Challenge Problems

- [5] **Problem 7.** Mass  $M_a$  lies on top of mass  $M_b$ , as shown. Assume  $M_b > M_a$ . The two blocks are pulled from rest by a massless rope passing over a pulley. The pulley is accelerated at rate  $A$ . Block  $M_b$  slides on the table without friction, but there is a constant friction force  $f$  between  $M_a$  and  $M_b$  due to their relative motion. Find the tension in the rope.



- [6] **Problem 8.** A device called a capstan is used aboard ships in order to control a rope which is under great tension. The rope is wrapped around a fixed drum, usually for several turns (the drawing shows about a three-quarter turn). The load on the rope pulls it with a force  $T_A$ , and the sailor holds it with a much smaller force  $T_B$ . Show that  $T_B = T_A e^{-\mu\theta}$ , where  $\mu$  is the coefficient of friction and  $\theta$  is the total angle subtended by the rope on the drum.



- [7] **Problem 9.** Find the shortest possible period of revolution of two identical gravitating solid spheres that are in circular orbit in free space about a point midway between them. The spheres have uniform density  $\rho$ . (Note that the two spheres cannot overlap!)