

# Is a whole insect brain connectome bilaterally symmetric?

## A case study on comparing two networks

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### Summary

- Aimed to define bilateral symmetry for a pair of networks, and formally test this hypothesis.
- Left and right hemispheres are significantly different under even the simplest model of a pair of networks
- Left and right differ significantly in cell type connection probabilities, even when adjusting for the difference in density
- Difference between hemispheres can be explained as combination of network-wide and cell type-specific effects
- Provided a definition of bilateral symmetry exhibited by this connectome, tools for future connectome comparisons

### Motivation

- Connectomes are rich sources of inspiration for architectures in artificial intelligence.
- Comparing connectomes could help elucidate which structural features are necessary for yielding the capabilities animal intelligences.
- Bilateral symmetry for connectomes has been investigated, but not clearly defined as a network hypothesis.

### Larval *Drosophila* brain connectome

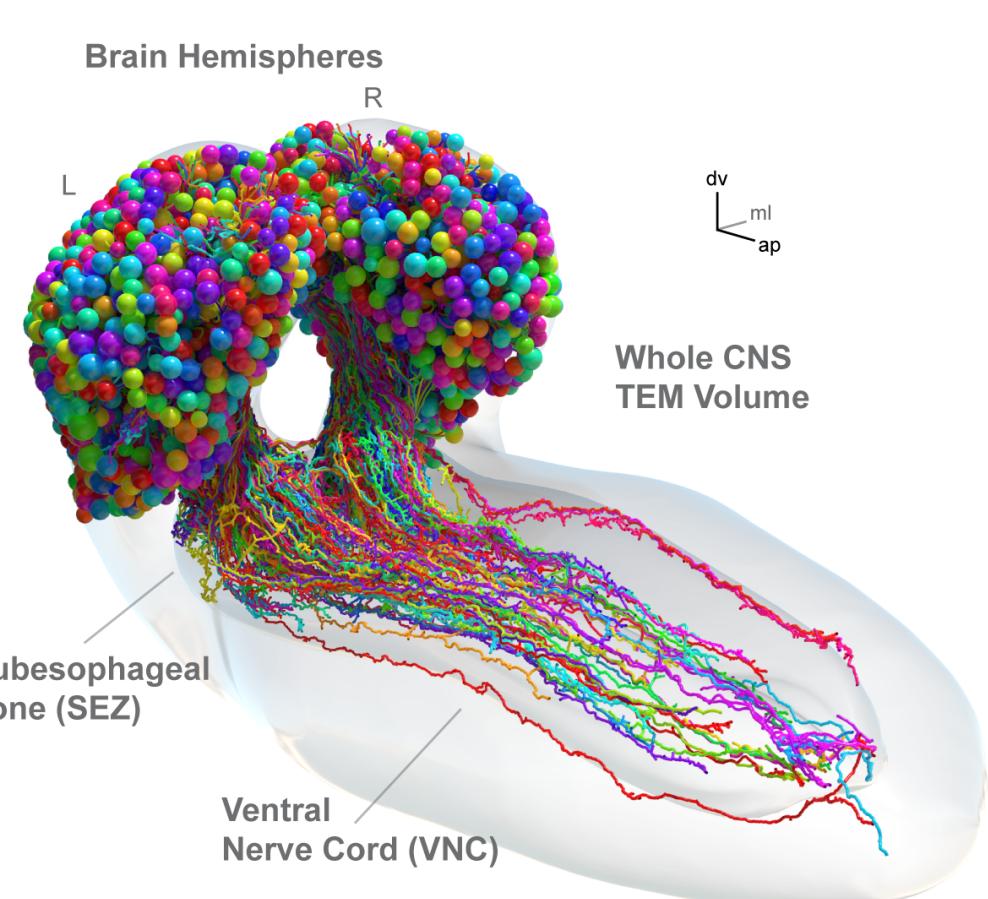


Fig 1A: 3D rendering of larval *Drosophila* brain connectome [1]. Comprised of ~3k neurons and ~544k synapses.

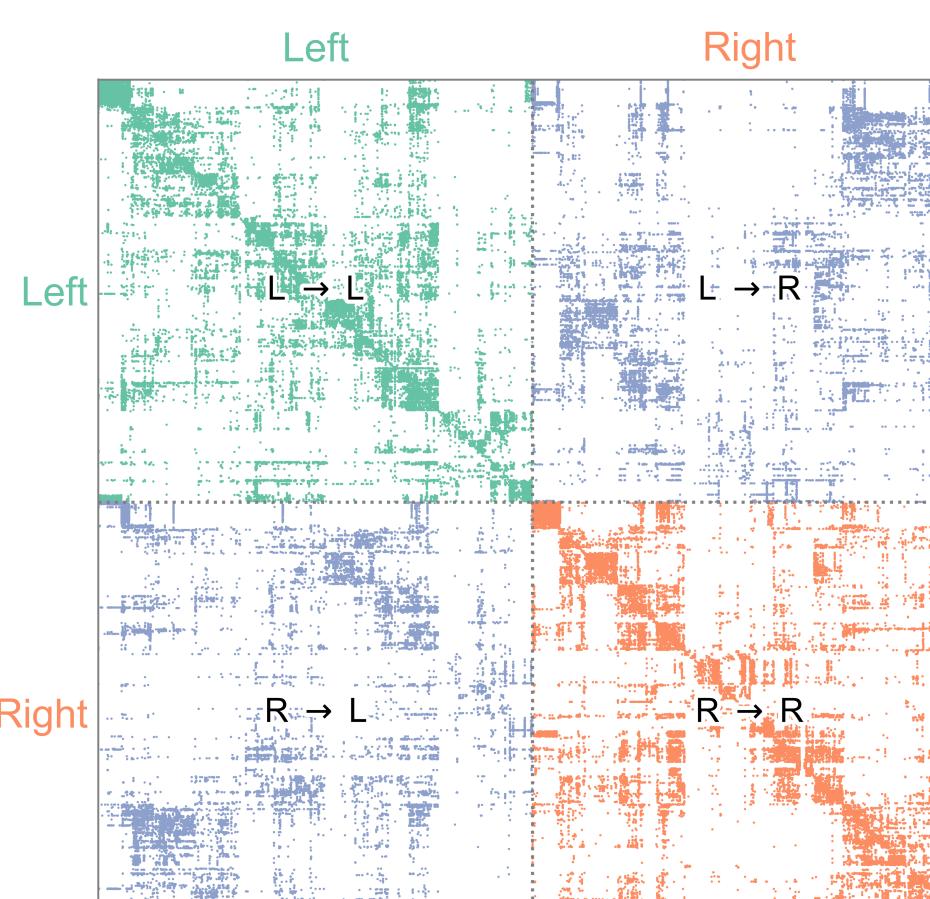


Fig 1B: Adjacency matrix sorted by brain hemisphere. We focus on comparing  $L \rightarrow L$  vs.  $R \rightarrow R$  subgraphs.

### Are the left and right networks "different"?

Requires that we define what we mean by "different" for a pair of networks, and develop a test procedure for any definition.

### Density testing

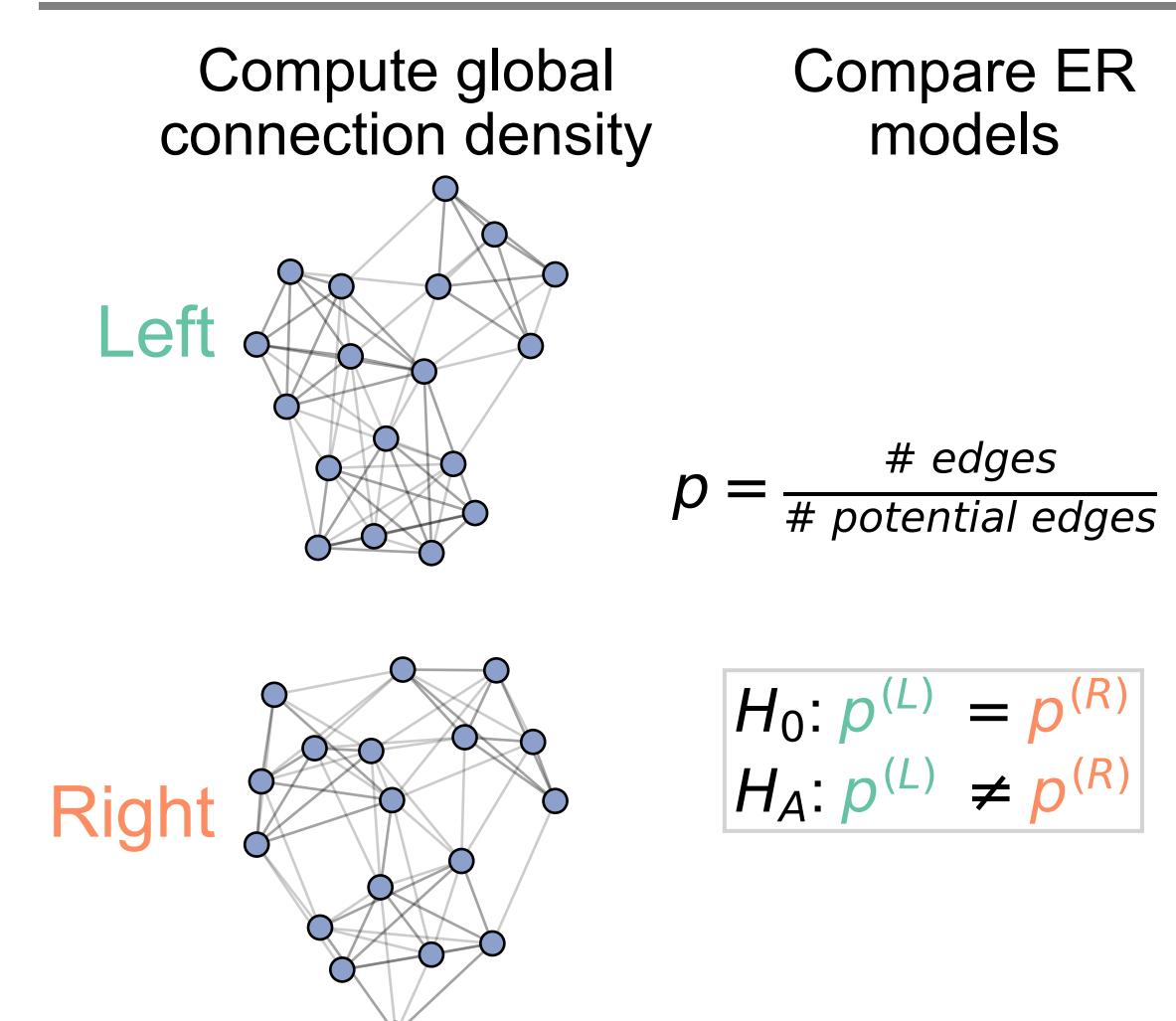


Fig 2A: Testing symmetry under Erdos-Renyi (ER) model [2] amounts to comparing densities (here via Fisher's exact test).

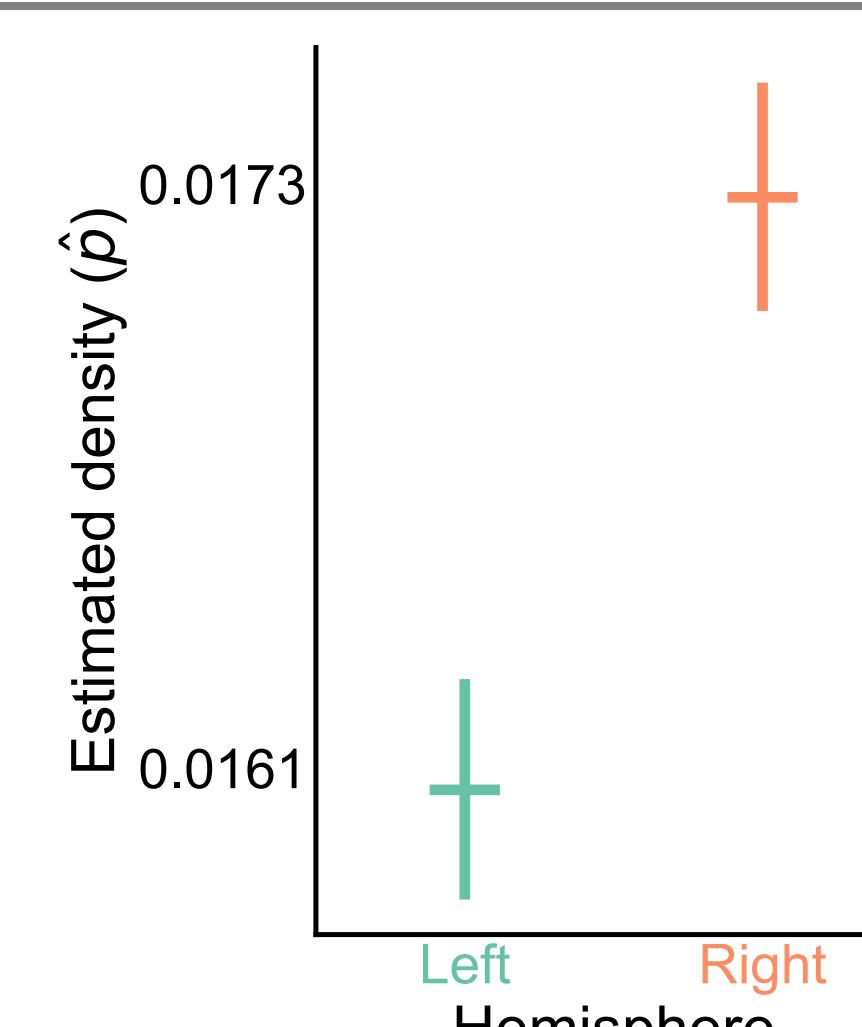


Fig 2B: Densities are significantly different between hemispheres ( $p < 10^{-23}$ ).

### Group connection testing

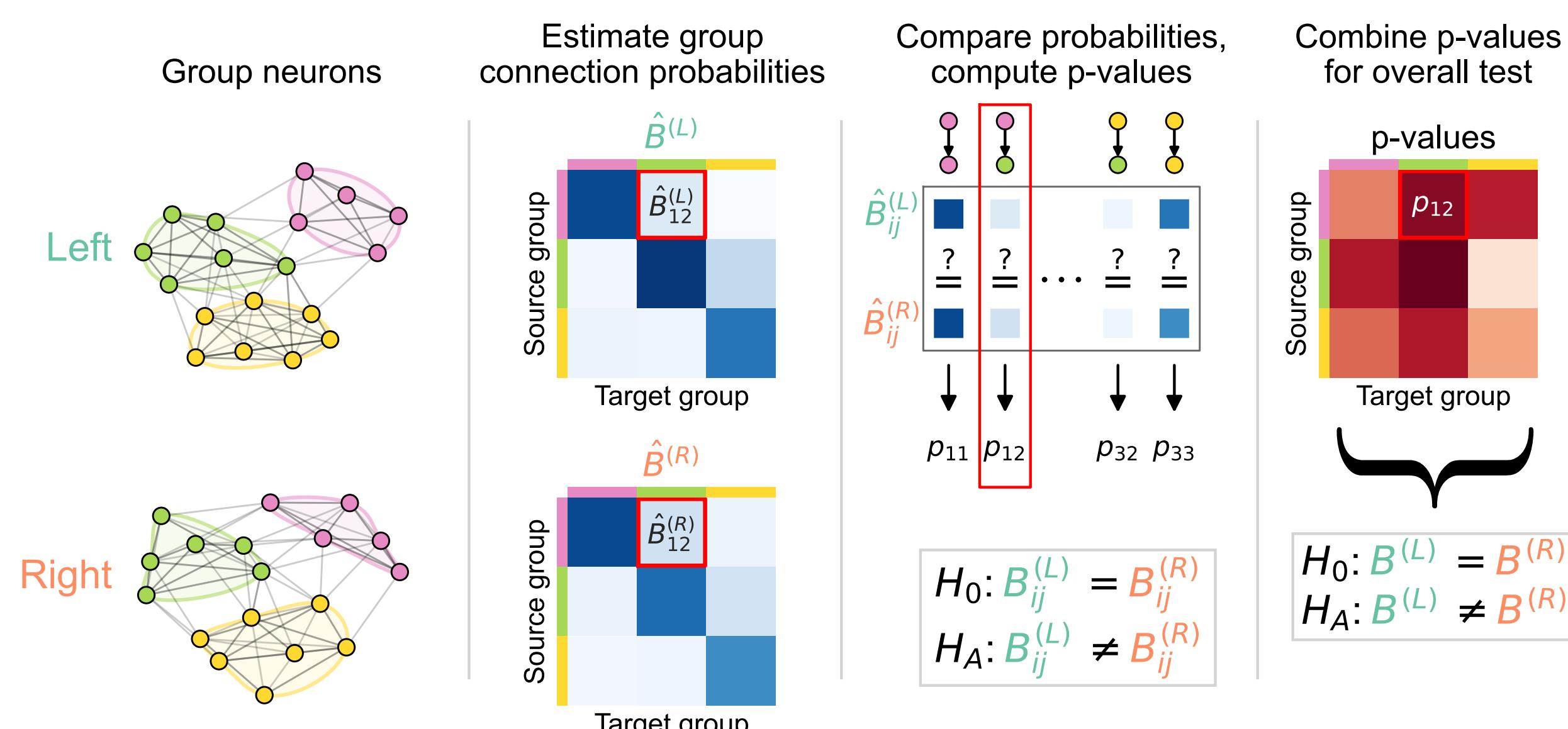


Fig 3A: Testing under stochastic block model (SBM) compares probabilities of connections between groups (here using cell types).

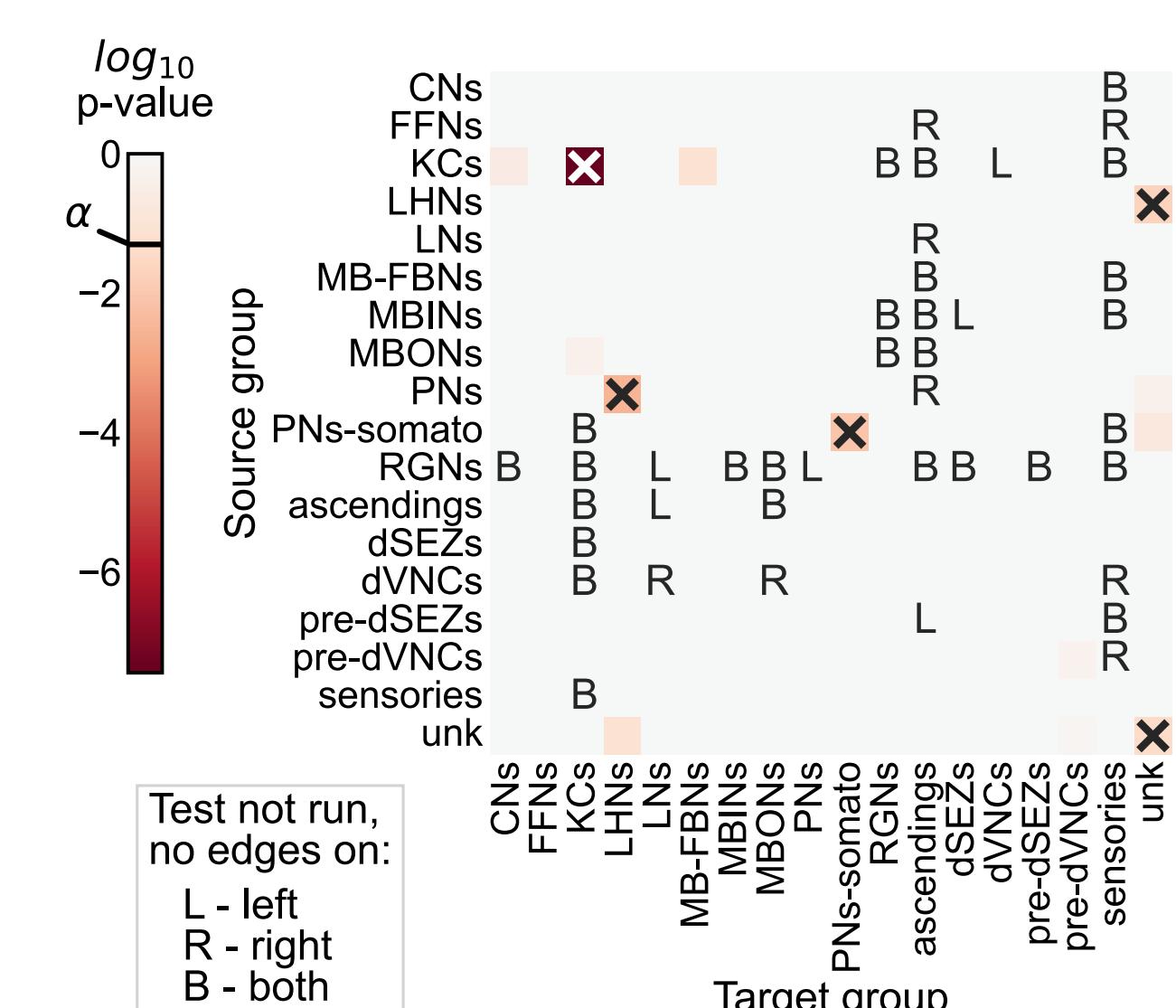


Fig 3B: Corrected p-values for each group connection.

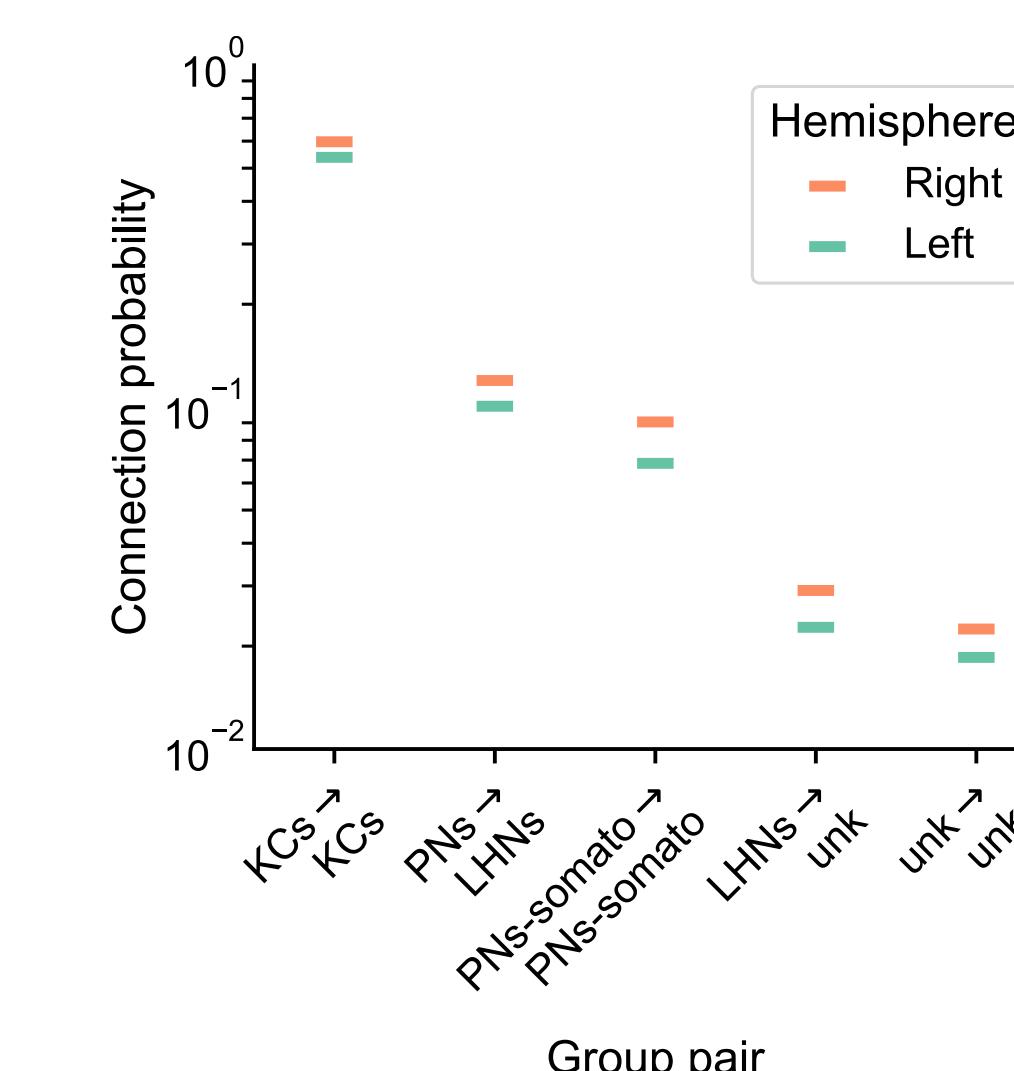


Fig 3C: Comparison of probabilities for significant connections.

### Density-adjusted group connection testing

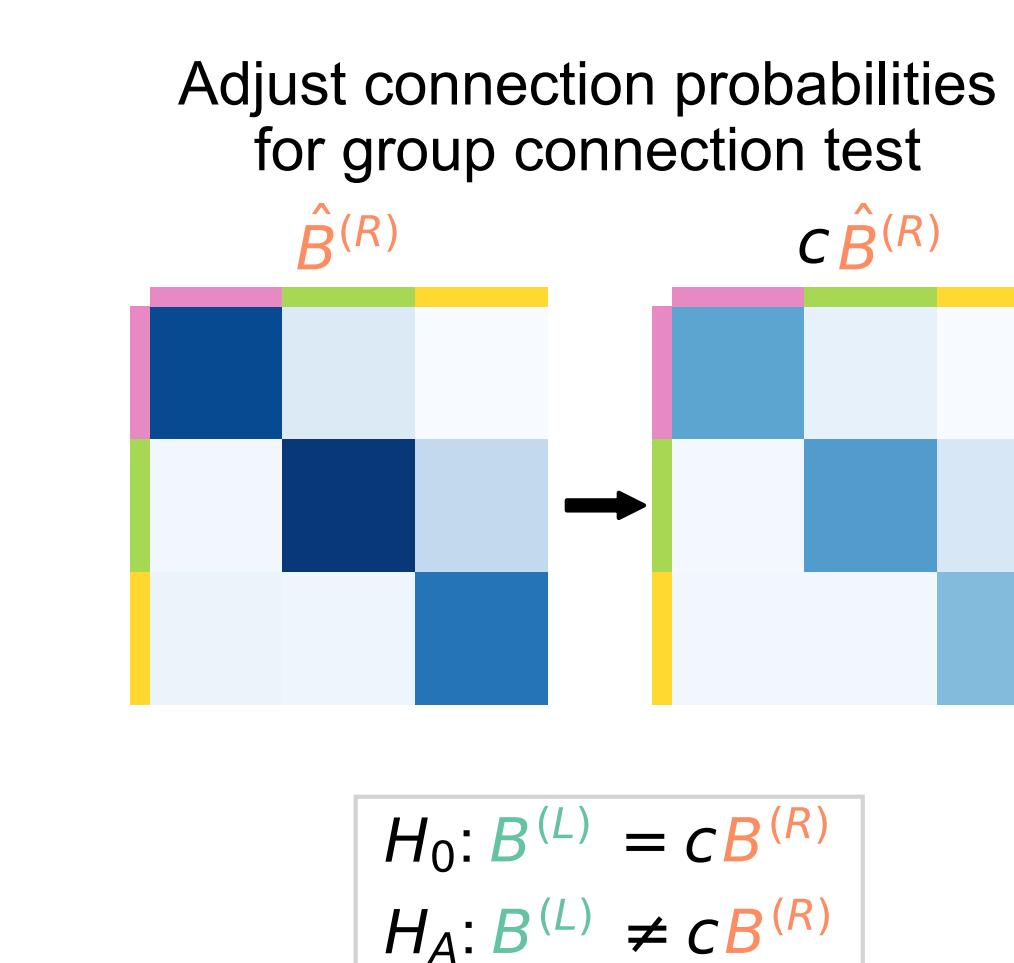


Fig 4A: Density-adjusted hypothesis, modified from Fig 3.

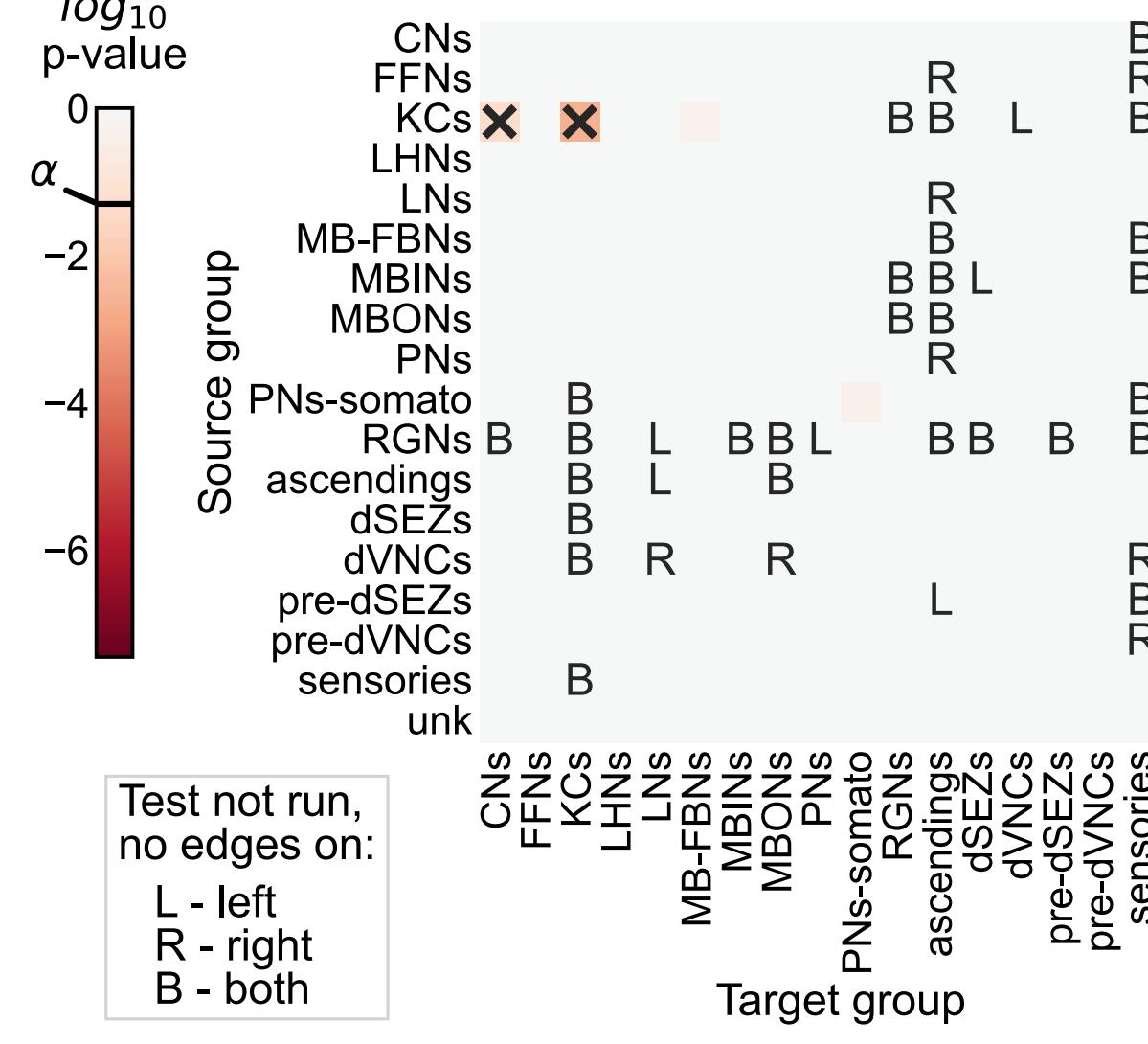


Fig 4B: Corrected p-values for group connections w/ density adjustment.

### Removing Kenyon cells

Reran all tests after removing the asymmetric cell type (see below)

### Notions of bilateral symmetry

Model	$H_0$ (vs. $H_A \neq$ )	KCs	p-value	Interpretation
ER	$p^{(L)} = p^{(R)}$	+	$< 10^{-23}$	Reject equal densities
SBM	$B^{(L)} = B^{(R)}$	+	$< 10^{-7}$	Reject equal group connection probabilities
aSBM	$B^{(L)} = cB^{(R)}$	+	$\approx 0.002$	Reject above even w/ density adjustment
ER	$p^{(L)} = p^{(R)}$	-	$< 10^{-26}$	Reject equal densities
SBM	$B^{(L)} = B^{(R)}$	-	$\approx 0.003$	Reject equal group connection probabilities
aSBM	$B^{(L)} = cB^{(R)}$	-	$\approx 0.43$	Fail to reject above after density adjustment

### Edge weight thresholds

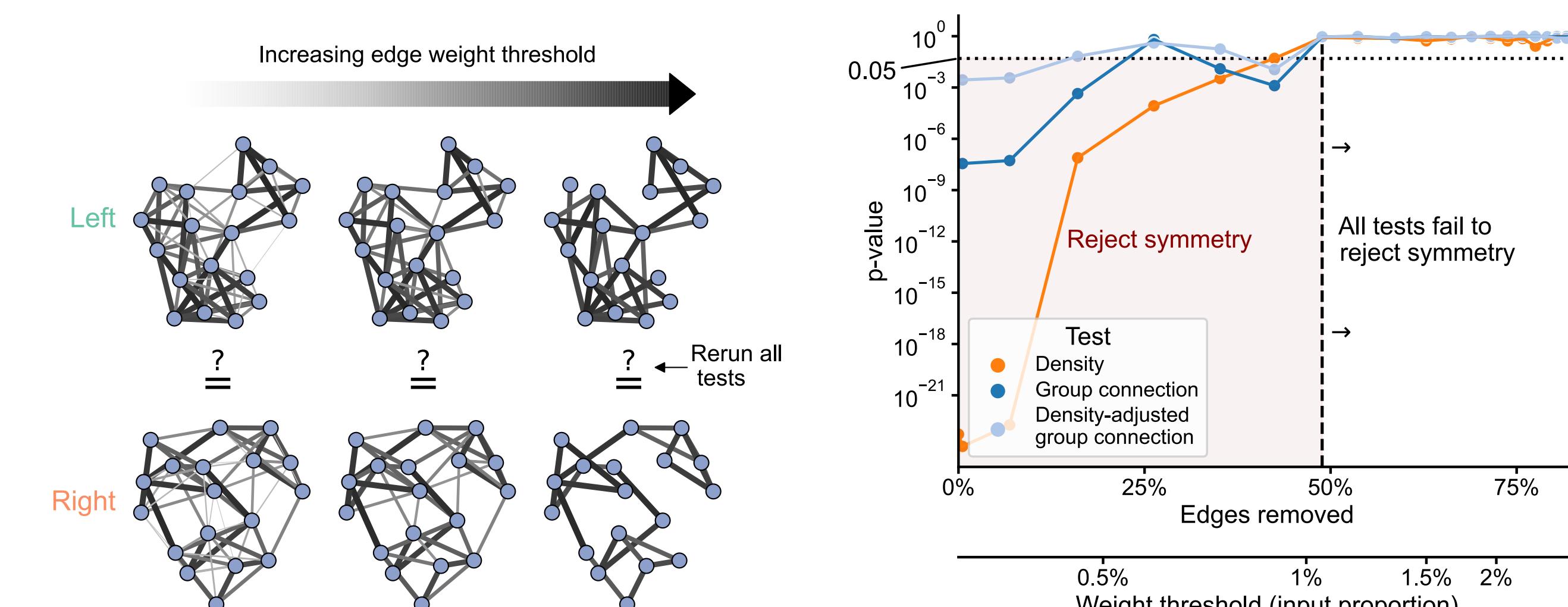


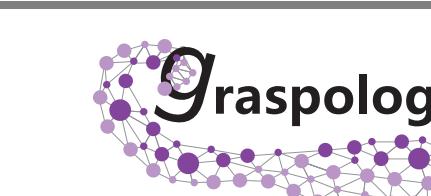
Fig 5A: Removed edges below some edge weight (synapse count or proportion of input to downstream neuron) threshold, testing bilateral symmetry for each resulting pair of networks.

Fig 5B: Higher edge weight thresholds generally make networks more symmetric. Less apparent when using synapse counts as edge weights (not shown).

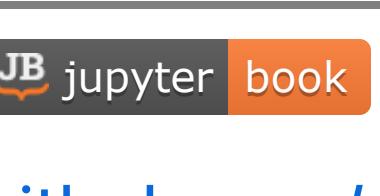
### Limitations and extensions

- Many other models to consider (e.g. random dot product graph [3])
- Many other potential neuron groupings for group connection testing
- Matched nodes between networks

### Code and references



downloads 115k  
Stars 245



github.com/neurodata/bilateral-connectome  
github.com/microsoft/graspologic

- [1]: Winding, Pedigo et al. "The complete connectome of an insect brain," In prep. (2022)  
[2]: Chung et al. "Statistical connectomics," Ann. Rev. Statistics and its Application (2021)  
[3]: Athreya et al. "Statistical inference on random dot product graphs: a survey," JMLR (2017)