### Single-head OOD Experiments

The single-head gaussian experiments tell us

- Naively combining two datasets can increase the risk on target task
- However, weighted combination of the datasets guarantees that the risk decreases.
- We also get diminishing returns as the tasks become more dissimilar.

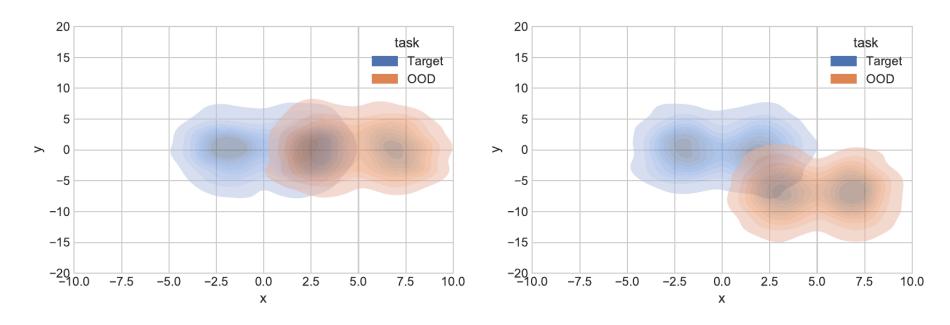
## Accuracy on task [2, 3]

| Samples | Acc   |
|---------|-------|
| 50      | 34.5  |
| 125     | 29.25 |
| 250     | 25.94 |
| 500     | 23.29 |
| 1000    | 20.49 |
| 1500    | 10 70 |

Lower accuracies are probably due to data augmentation but that shouldn't affect the trends.

#### **Multi-head**

Where does multi-head fit into all this? The key idea is all tasks share a low-dimensional representation.



To understand this idea, we consider tasks constructed using two-dimensional Gaussians

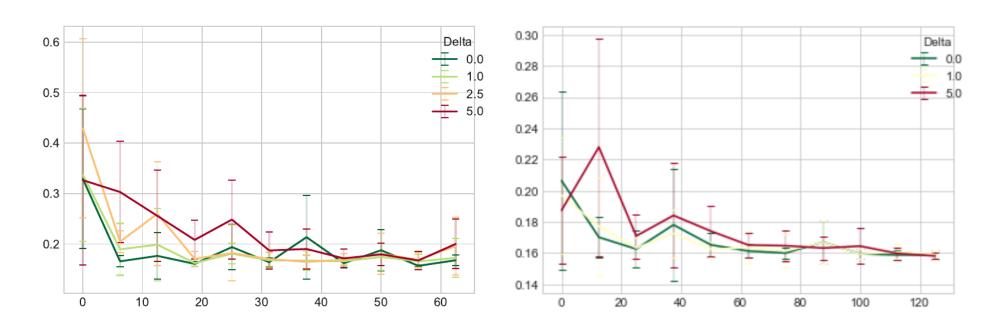
### Multi-head: Gaussian Experiments

We want to find a 1-dimensional embedding that is useful to both tasks. We consider the following neural net architecture

$$ext{input} 
ightarrow ext{FC}(2,100) 
ightarrow ext{FC}(100,1) 
ightarrow ext{FC}(1,1)_i$$

Multi-head is useful as long as the OOD and target task are simple translations of each other. In this case, both tasks share an optimal 1-dimensional embedding.

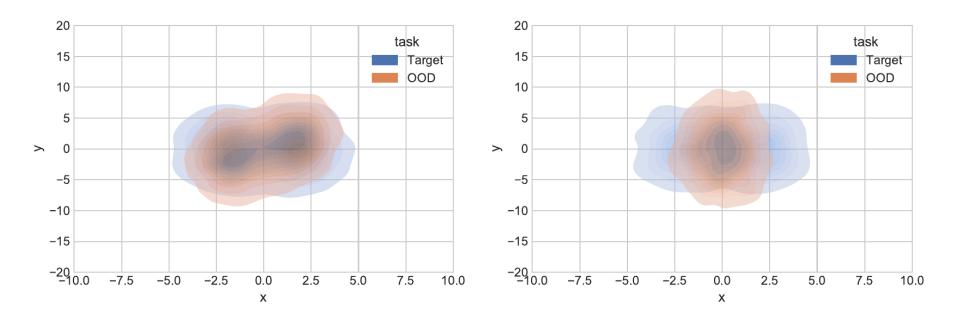
#### **Multi-head: Translated OOD task**



Left(n=2) and right(n=8). In both cases, the accuracy dips with more OOD samples. This happens regardless of the value of  $\Delta$ .

#### Multi-head: Rotated OOD task

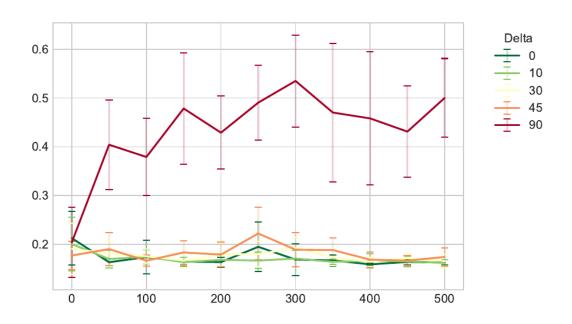
Next, we consider rotated OOD-tasks



Caption: (Left) 45 degree rotation and (right) 90 degree rotation

Here there exists no optimal 1D embedding.

#### Multi-head: Rotated OOD tasks



In general, Baxter's model only works if there exists a  $\mathbb{R}^k$  dimensional embedding that as useful to separate the classes from any single task. Such an embedding need to exist for dissimilar tasks.

# More questions on Singlhead/Multihead

- How does more tasks affect both models?
- Weighted sampling for multihead?

#### Next?

- Single-head and multi-head are both useful
  - We can understand augmentations as a version of single-head
- Do tasks like CIFAR100 have this low-dimensional embedding. How small is this dimension (can we estimate it?).
- How do we think of a task with more/less classes. Is it more informative if we have more classes?
- ImageNet is this giant model. Can I create similar tasks from it?