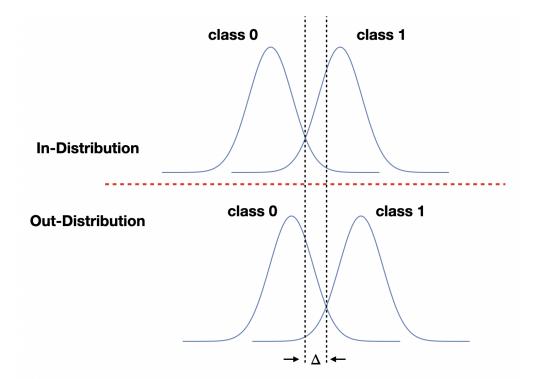
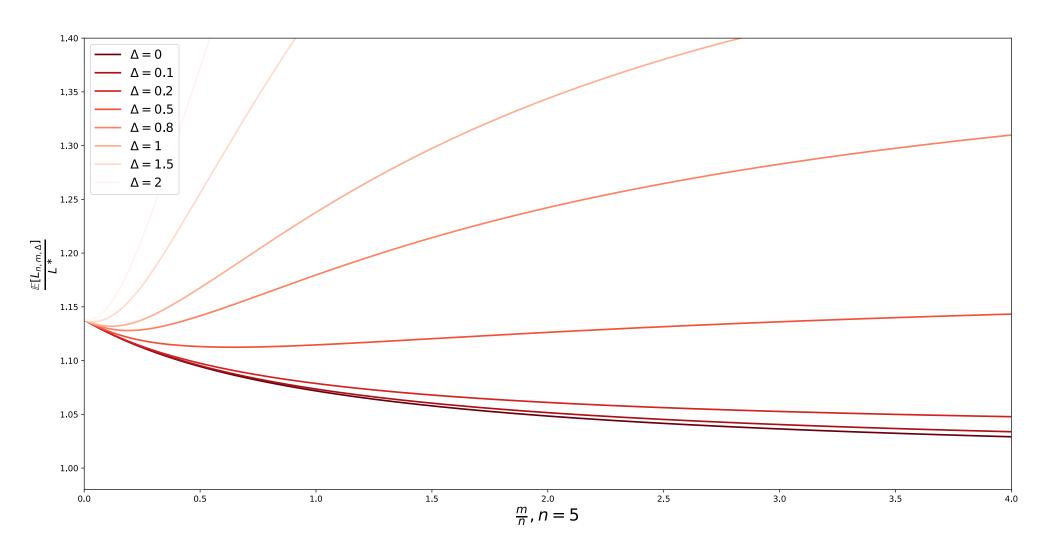
# **Out-of-Distribution Learning**

- Consider an in-distribution task that consists of two class conditional gaussians.
- Now, consider an out-of-distribution task similar to the above task, but whose center is displaced by an amount  $\Delta$ .
- ullet The amount  $\Delta$  reflects the "similarity" between the two tasks.

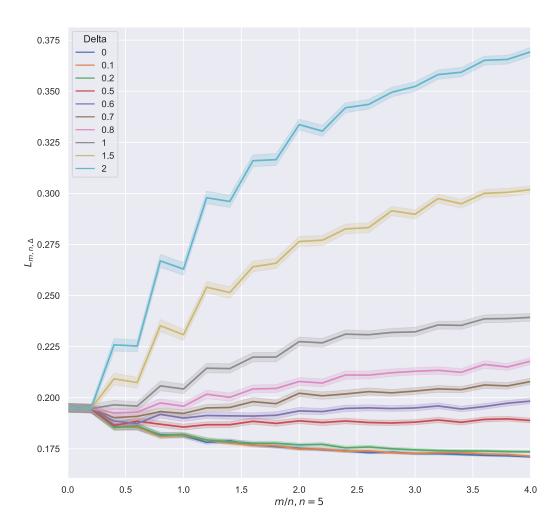


- ullet We have access to n samples from the in-distribution task, and m samples from the out-of-distribution task.
- ullet Using both the in-distribution and out-of-distribution samples, we train a classifier h aimed at the in-distribution classification task.
- Let's denote the classification error of h by  $\mathbb{E}[L_{n,m,\Delta}]$ .

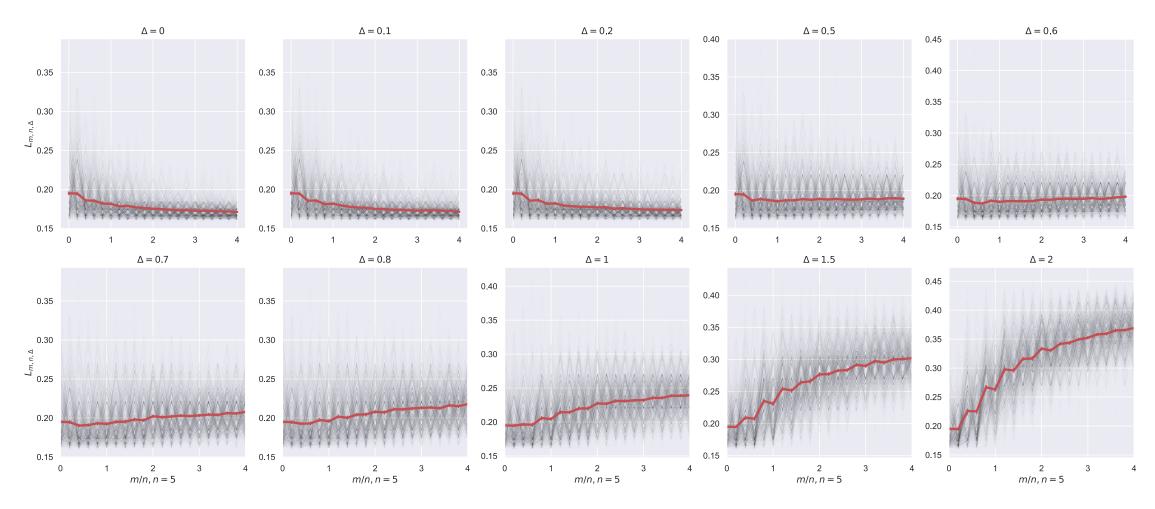
- ullet Let n be a small fixed constant. We hypothesize that,
  - $\circ$  For very small  $\Delta$ , as we add more out-of-distribution data (as m increases) the  $\mathbb{E}[L_{n,m,\Delta}]$  would decrease.
  - $\circ$  For moderately large  $\Delta$ , as we add more out-of-distribution data (as m increases) the  $\mathbb{E}[L_{n,m,\Delta}]$  would initially decrease and start increasing later. The initial decrease is due to the reduction in the variance of h. The later increase is due to the increase in bias of h caused by the out-of-distribution samples.
  - $\circ$  For very large  $\Delta$ , as we add more out-of-distribution data (as m increases) the  $\mathbb{E}[L_{n,m,\Delta}]$  would keep increasing.



• Number of replicates: 1000

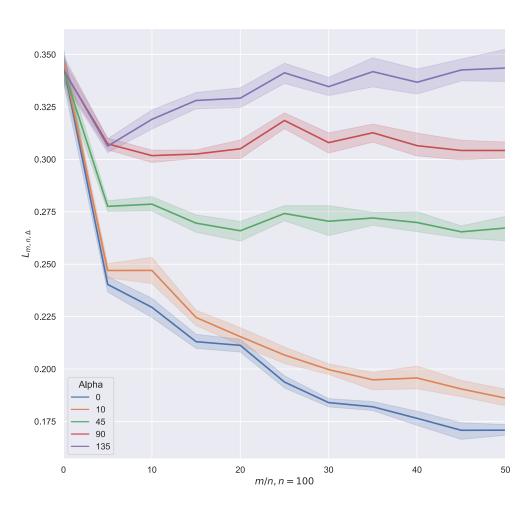


• Number of replicates: 1000



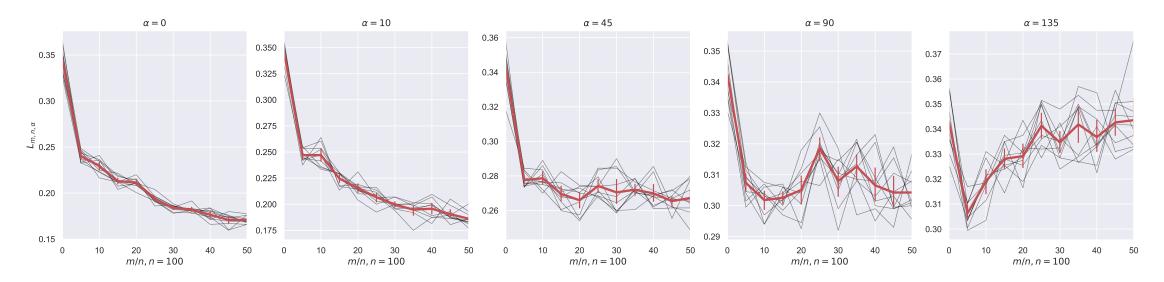
## Bird vs. Cat & $\alpha$ -Rotated Bird vs. Cat (Single-Head Network)

• Number of replicates: 10, Network: SmallConv



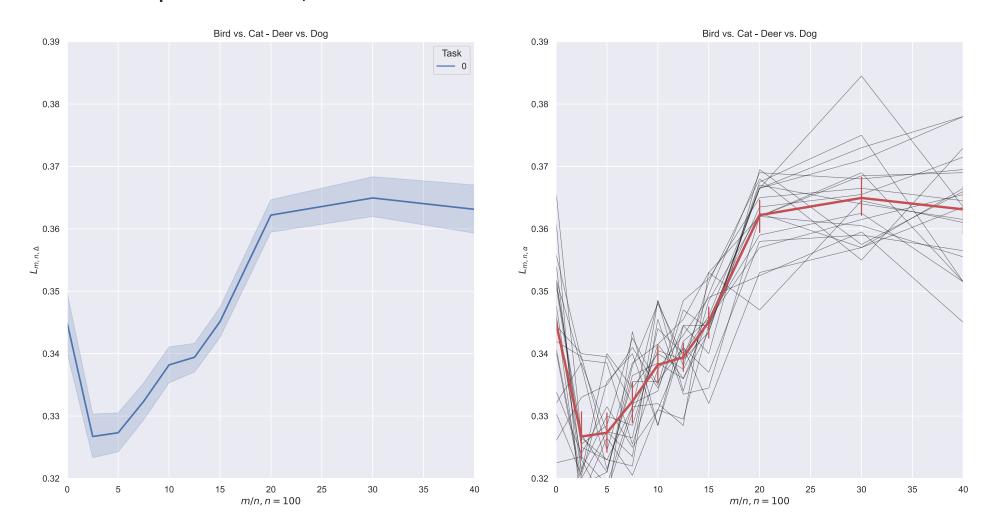
## Bird vs. Cat & $\alpha$ -Rotated Bird vs. Cat (Single-Head Network)

• Number of replicates: 10, Network: SmallConv



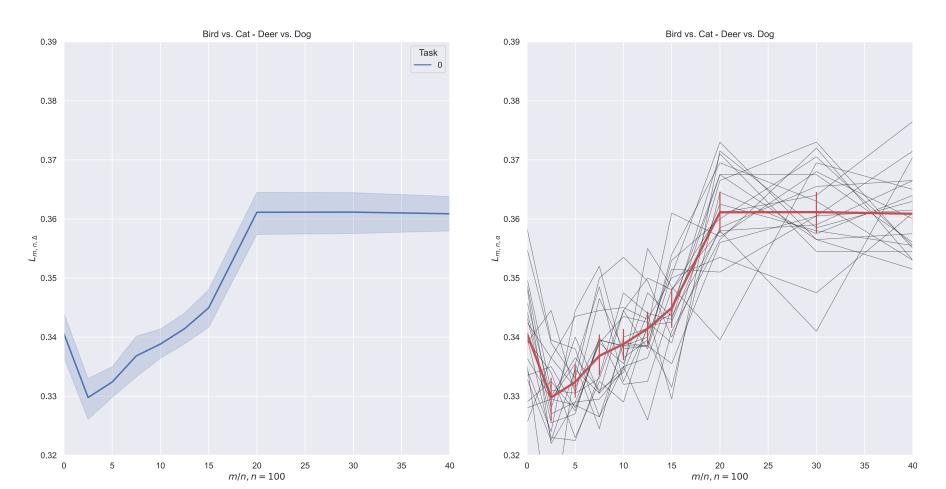
#### Task 2: Bird vs. Cat & Task 3: Deer vs. Dog (Single-Head Network)

• Number of replicates: 20, Network: SmallConv



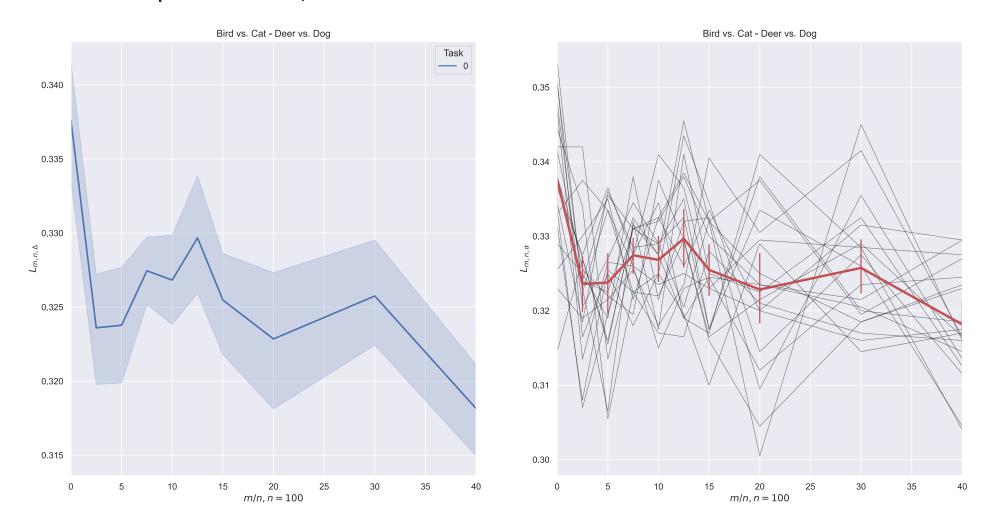
## Task 2: Bird vs. Cat & Task 3: Deer vs. Dog (Single-Head Network)

Number of replicates: 20, Network: SmallConv, each model was trained for 100 epochs



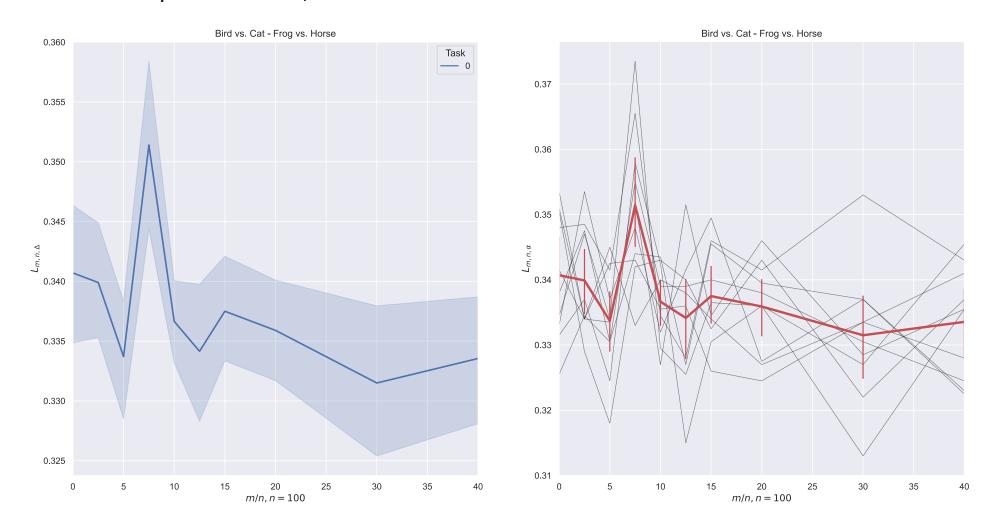
#### Task 2: Bird vs. Cat & Task 3: Deer vs. Dog (Multi-Head Network)

• Number of replicates: 20, Network: SmallConv



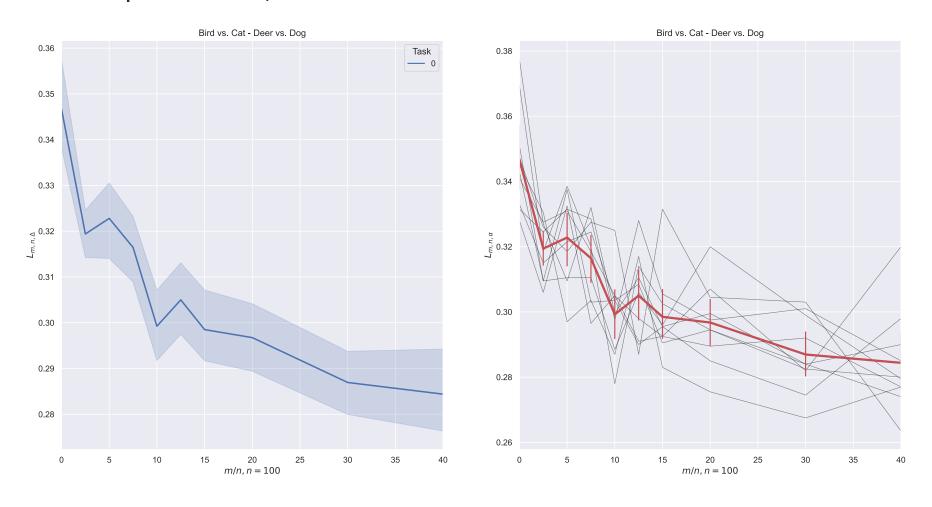
#### Task 2: Bird vs. Cat & Task 4: Frog vs. Horse (Multi-Head Network)

• Number of replicates: 20, Network: SmallConv



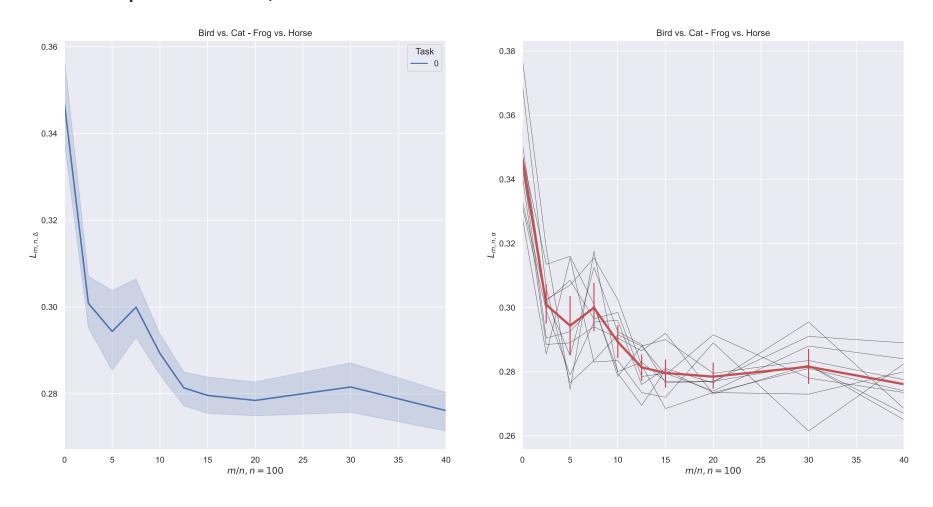
#### Task 2: Bird vs. Cat & Task 3: Deer vs. Dog (Multi-Head Network)

• Number of replicates: 10, Network: Wide Res-Net



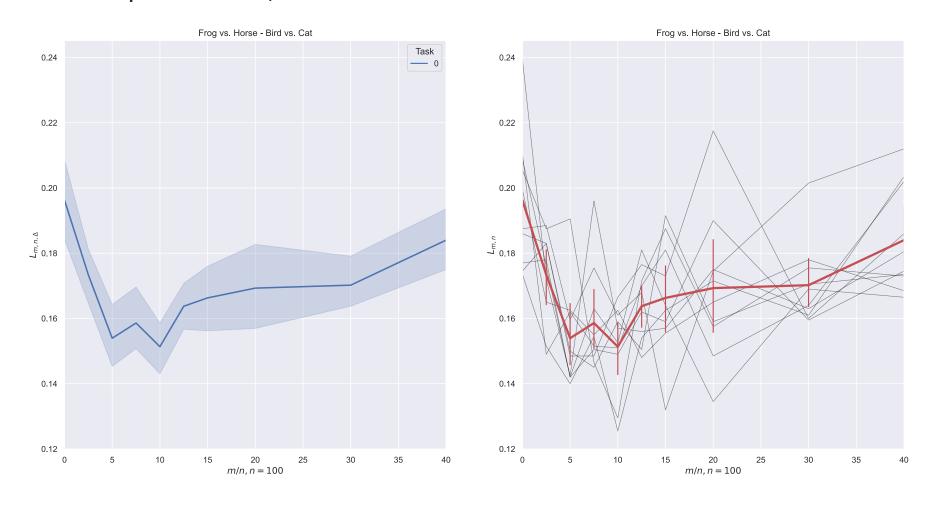
## Task 2: Bird vs. Cat & Task 4: Frog vs. Horse (Multi-Head Network)

• Number of replicates: 10, Network: Wide Res-Net

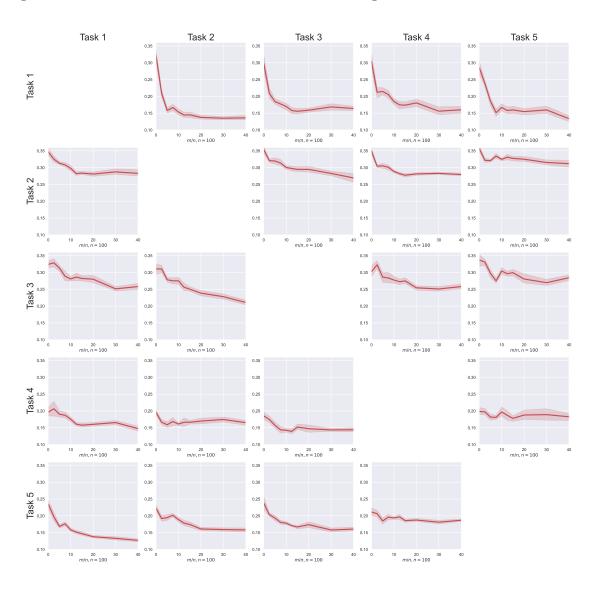


### Task 4: Frog vs. Horse & Task 2: Bird vs. Cat (Multi-Head Network)

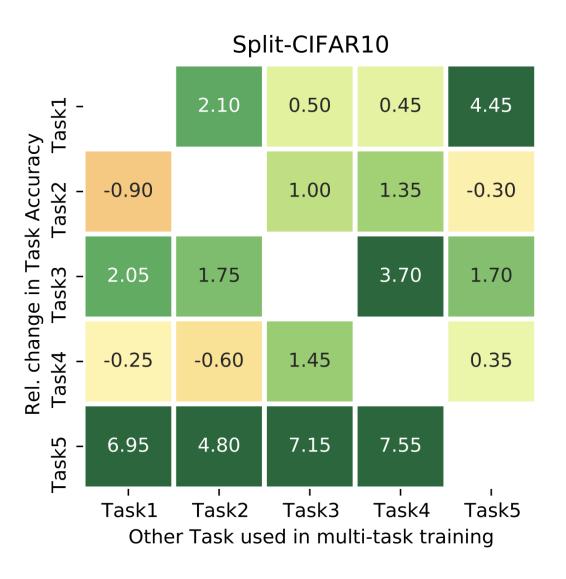
• Number of replicates: 10, Network: Wide Res-Net



## **CIFAR-10 Tasks (Multi-Head Network)**



#### **CIFAR-10 Tasks (Multi-Head Network)**



## **CIFAR-10 Tasks (Multi-Head Network)**

• Random sampling (large range of m/n values)

