



$$(\vec{k}_i + \vec{Q})^2 = \vec{k}_f^2$$

$$|\vec{k}_i|^2 + |\vec{Q}|^2 + 2|\vec{k}_i||\vec{Q}|\cos\alpha = |\vec{k}_f|^2$$

$$\cos\alpha = \frac{|\vec{k}_i|^2 + |\vec{Q}|^2 - |\vec{k}_f|^2}{2 \cdot |\vec{k}_i| \cdot |\vec{Q}|}$$

$$E_i = 20 \text{ meV}$$

$$k_i = k_f = 3 \cdot 10^7 \text{ A}^{-1}$$

test: $|\vec{Q}| = 3 \cdot 10^7$



$$\alpha = 60^\circ$$

$$|\vec{Q}| = 2$$

$$\alpha = \arccos\left(\frac{4}{2 \times 3 \cdot 10^7 \times 2}\right) = 71.225^\circ$$