# APPENDIX

**NOMENCLATURE**

**Indices and sets**

|  |  |
| --- | --- |
| *Bk*, *Wk*, *Dk* | Sets of gas procurement, wind farms, and electrical load nodes in UIES*k* |
| *Hk*, *Mk* | Sets of heat load, gas load, and equipment in nodes UIES*k* |
|  | Sets of wind farm, generator, and electrical load nodes in TS |
| *wt*, *wu* | Indices of wind farms in TS and UIES*k* |

**Parameters**

|  |  |
| --- | --- |
|  | Efficiencies of EB, GB, waste heat boiler (WHB), and GT |
|  | Upper and lower bounds of electrical load curtailment in UIES*k* |
|  | Coefficients in cost function of generator *tm* |
|  | Generation shift distribution factors |
| , | Predictive electrical loads in TS and UIES*k* |
|  | Power flow limit of line *l* |
|  | Resistance and reactance of distribution line *ij* |
| , | Upper and lower voltage limits of distribution node *j* |

**Variables**

|  |  |
| --- | --- |
| , | Wind curtailments in TS/UIES*k* |
| , | Dispatched electrical loads in TS and UIES*k* |
|  | Power input of EB |
|  | Active power of distribution line *ij* |
|  | Power injection of distribution node *j* |
| , | Dispatched wind power in TS and UIES*k* |

## Specific Expression of the (6)[[1]](#footnote-1)



 is the day-ahead/intraday corresponding penalty coefficient of each item.

In the optimization model, inspired by the linearization of the absolute value method [1], we decompose conventional unit power changes into positive and negative parts (&). The intra-day power can thus be represented as:. At the same time, the objective function contains the sum of positive and negative power (). Therefore, the optimization objective value is minimized only when at least one of the positive and negative powers is zero. This choice avoids the introduction of 0-1 variables, ensuring the continuity and theoretical convergence of the model.

[1] Bisschop, Johannes. *AIMMS optimization modeling*. Lulu. com, 2006.

## Day-ahead Constraints of TS

TS's day-ahead constraints include power balance constraint , power generation correlation constraint , wind farm constraint , load planning constraint , DC current security constraint , TS and UIES tie-line constraint .













## Specific Expression of the (9)



'eq' represents the general notation for all types of equipment symbols in the system, with .  denotes the day-ahead/intraday corresponding penalty coefficient for each item.

## UIESk Day-Ahead Distribution Network Constraints

The constraints mainly consist of distribution network constraints and load-related constraints .







 indicates that gas turbine *m* is connected to node *j.*  represents the set of starting nodes with node *j* as the end node branch, while  denotes the set of terminal nodes with node *j* as the starting node branch.

## UIESk Day-Ahead Equipment Constraints

This part includes constraints on conversion equipment and production equipment . The equipment that converts primary energy into secondary energy is referred to as energy production equipment (GT and GB), which satisfies upper and lower limits of output, ascent and descent slopes. Equipment then used convert secondary energy to secondary energy is categorized as energy conversion equipment (WHB and EB).





‘tra’ is the unified representation of energy conversion equipment. ‘pro’ is the unified representation of energy production equipment, ‘*v*’ is the corresponding equipment number. ‘LNG’ is the calorific value of natural gas. Specifically, the WHB’s input heat power generates heat for GT operation.

## MP and SP of the (30)

**MP:**

**SP:**

Here, ***L*** and ***l*** represent the constraints related to the TS’ SP. ***M*** and ***m*** stand for the constraints related to the UIES*k*’ SP. The SPs are independent of each other without coupled variable constraints, so they can be solved in parallel by each ESO.

Using TS as an example, the MP simultaneously optimizes variables such as the thermal power unit plan and wind power plan for both day-ahead and intraday scheduling phases. These optimized values are passed to the SP. The SP revolves solely around the day-ahead plan given in the MP and optimizes it for various scenarios during the intraday phase. Once optimized, the adverse distribution and its corresponding constraints are added back to the MP.

## Comparison of Different Robust methods

Table Comparison of three methods

|  |  |  |  |
| --- | --- | --- | --- |
| Cost($) | Approach | | |
| DRO | RO | SO |
| Phase I | 67983.7 | 67995.0 | 67982.2 |
| Phase II | 8467.4 | 10452.4 | 8395.1 |
| Total | 76451.1 | 78447.4 | 76377.3 |

1. [↑](#footnote-ref-1)