

# Angular Gap: Reducing the Uncertainty of Image Difficulty through Model Calibration

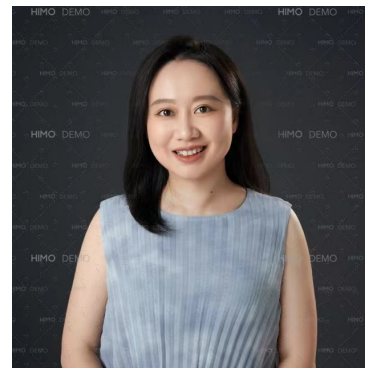
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1. Imperial College London

2. Samsung Research



**Imperial College**  
London

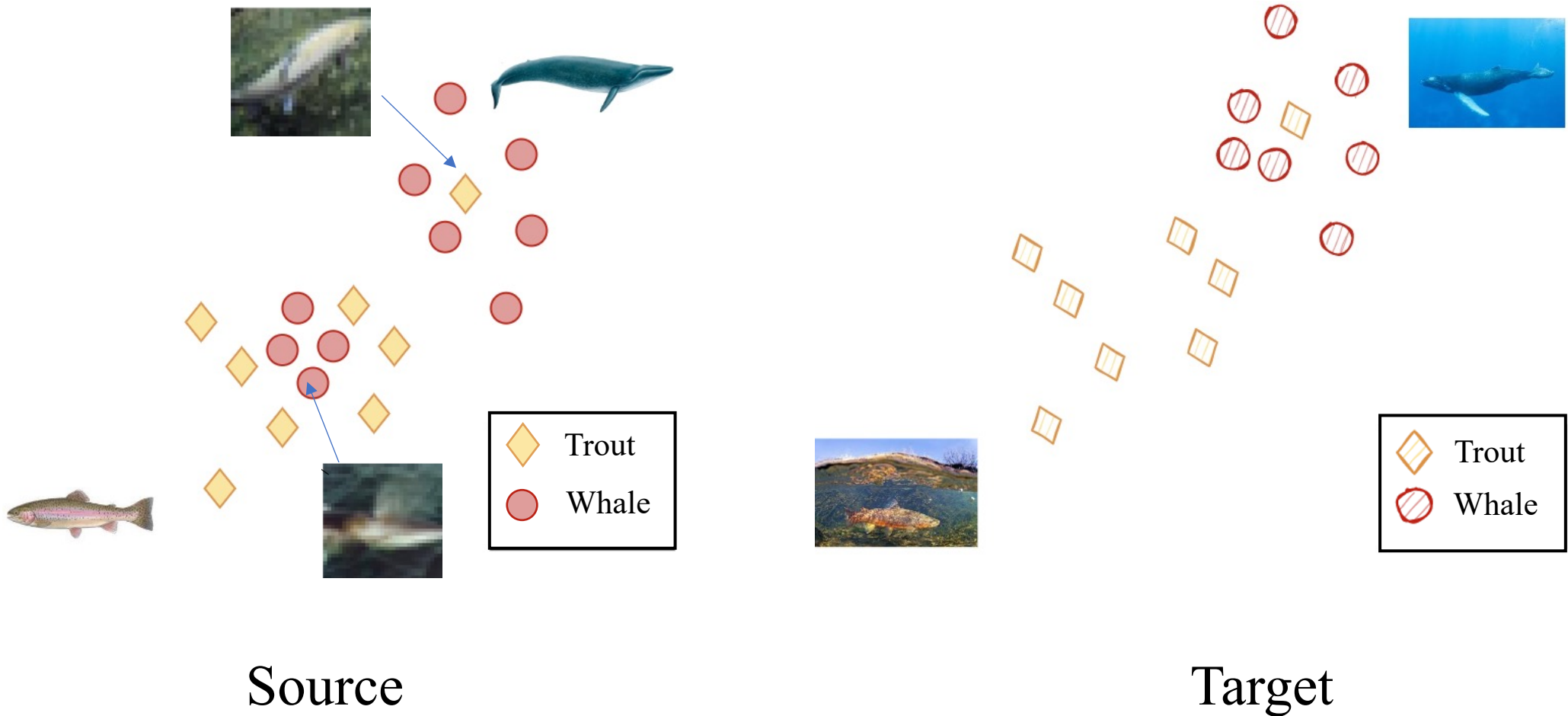
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# Outline

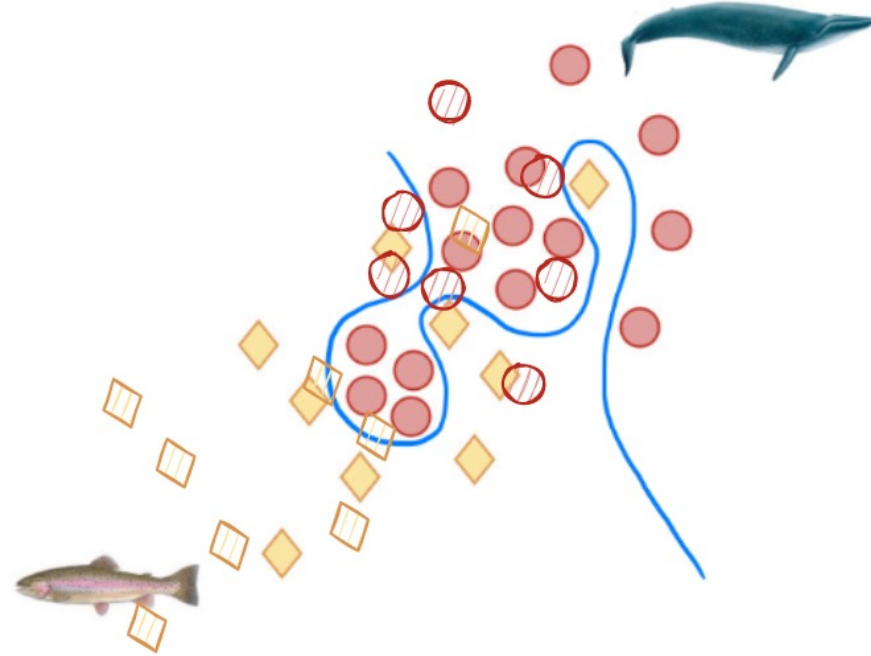
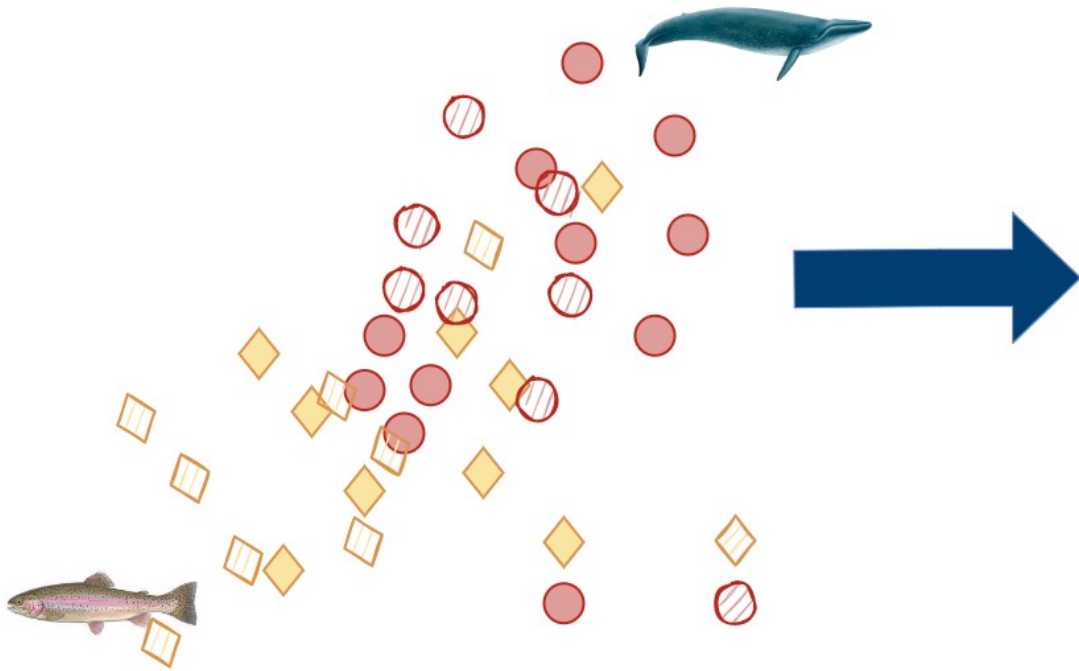
- Motivation
- Angular Gap framework
- Image difficulty estimator
- Curricula for domain adaptation
- Experiments
- Conclusion

# Motivation

Capturing **image difficulty** & designing **curricula** for unsupervised **domain adaptation**



# Motivation

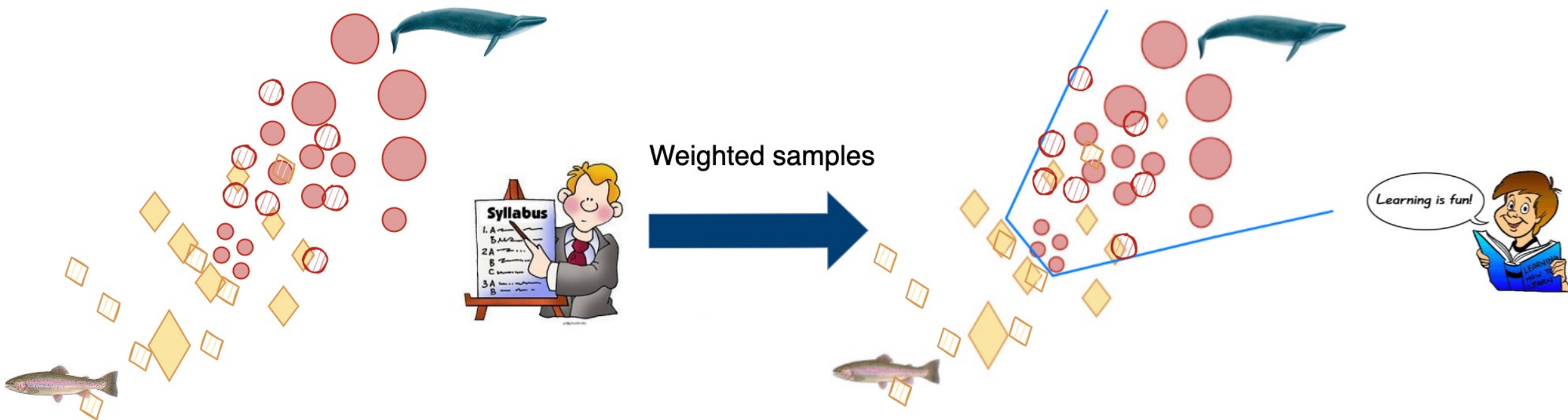


**Memorization**



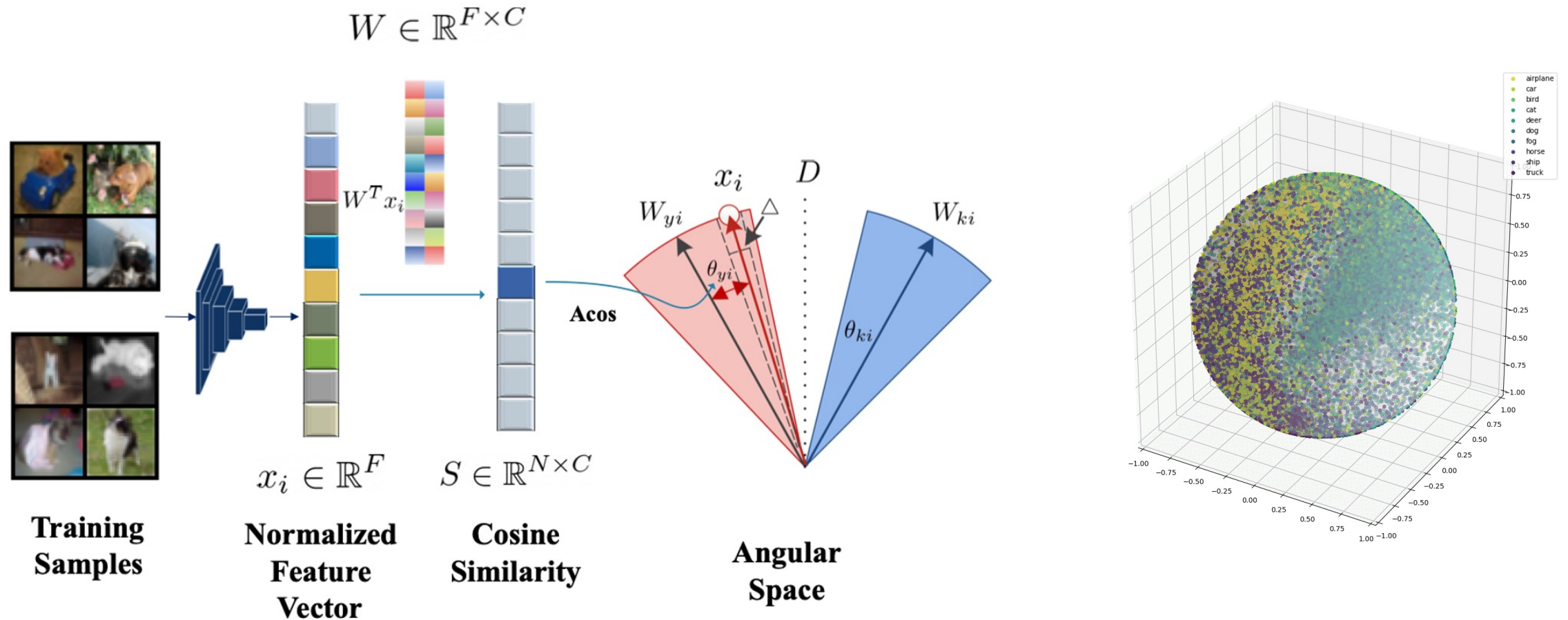
# Motivation

Learning with a **curriculum** to improve model **generalization**



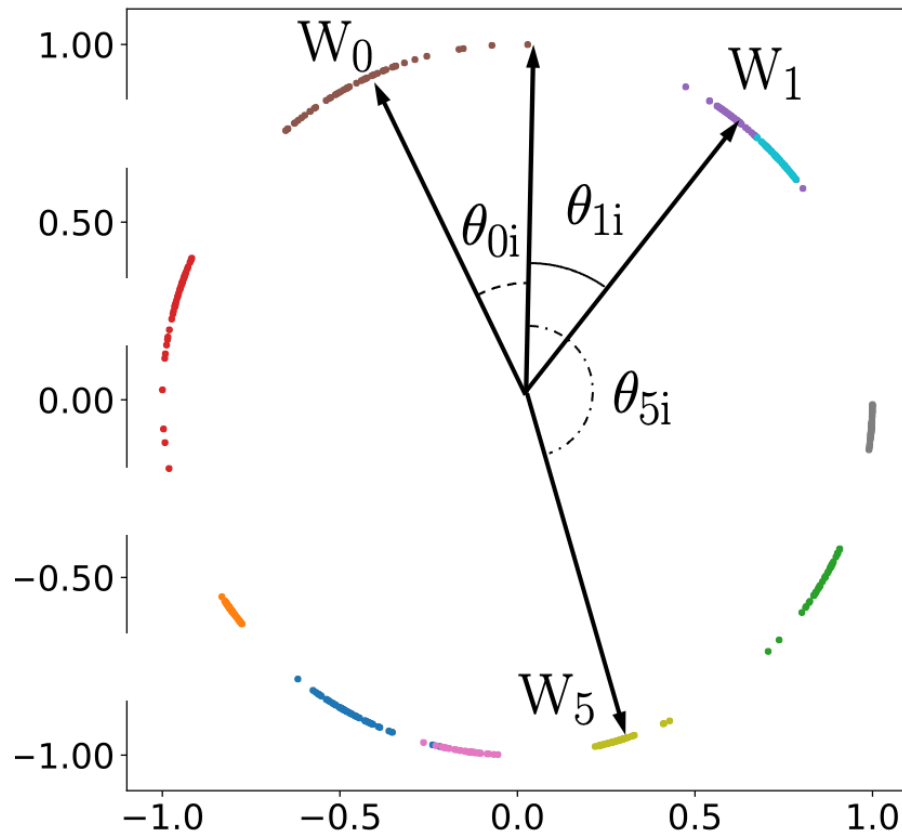
# How to represent image difficulty?

- Hyperspherical Learning (Liu, et al 2017), Angular Visual Hardness (Chen, 2020)

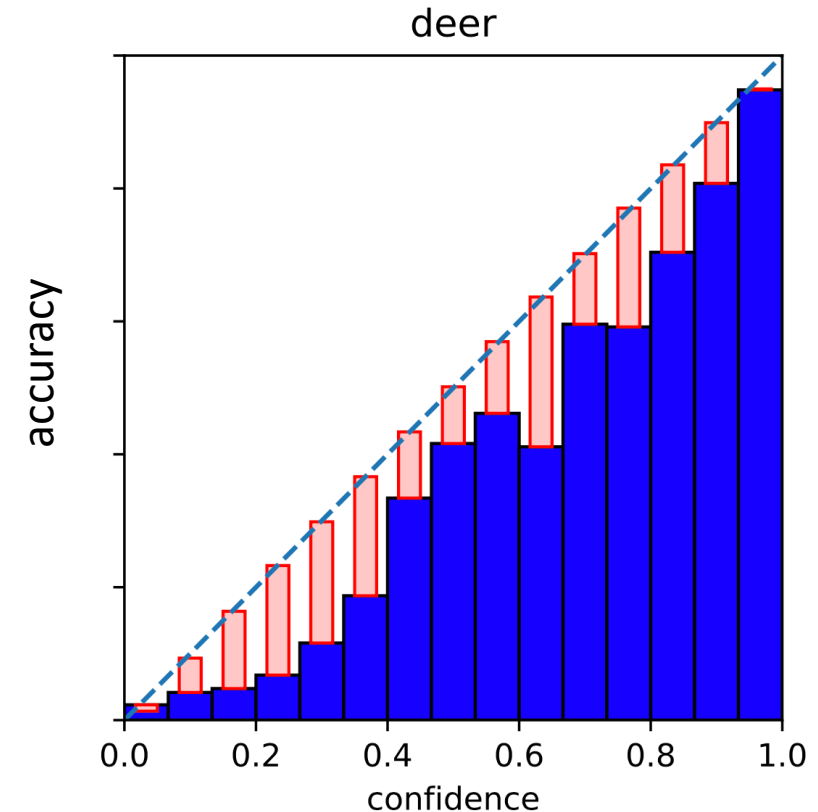


# How to reduce uncertainty in difficulty estimation?

- Uncertain difficulty scores will ruin curriculum learning.



- airplane
- car
- bird
- cat
- deer
- dog
- fog
- horse
- ship
- truck



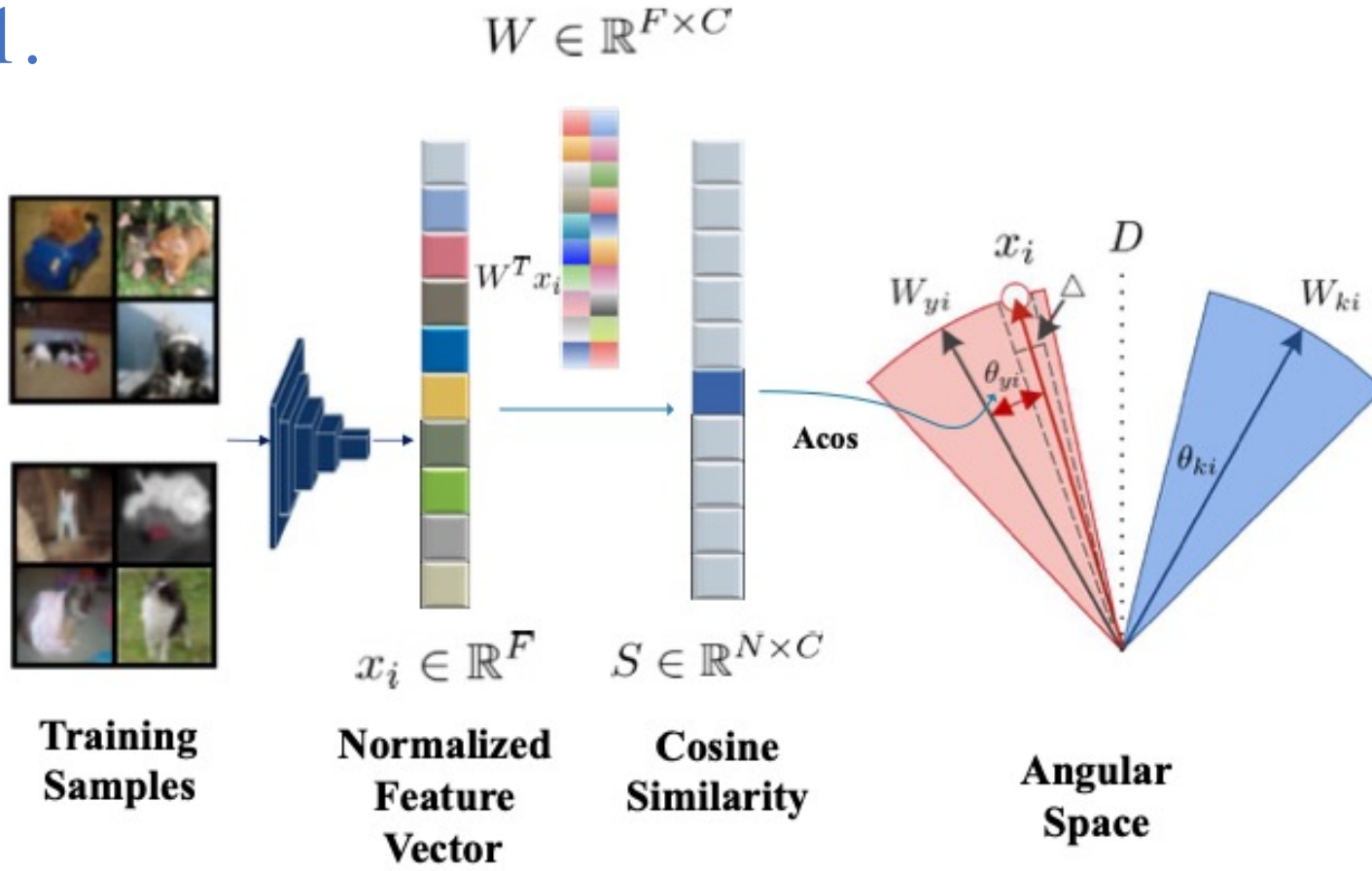
# Main research questions:

1. How to properly define image difficulty?
2. Will calibration techniques reduce uncertainty and improve downstream tasks with curriculum learning?
3. Can we automatically find a curriculum for domain adaptation tasks?



# Angular Gap based curriculum learning

1.

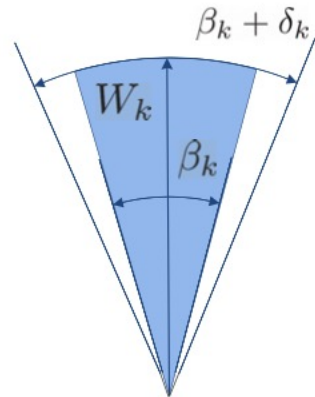


2.

**Calibration Map**

**Uncalibrated Angular Gap**

**Calibration Loss Function**



3.

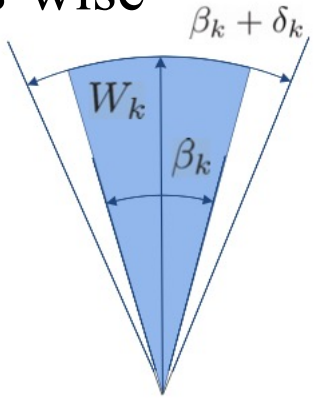
**Calibrated Angular Gap**

**Curriculum Learning**

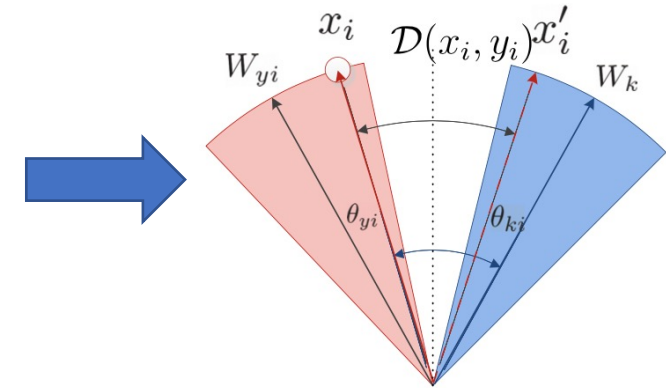
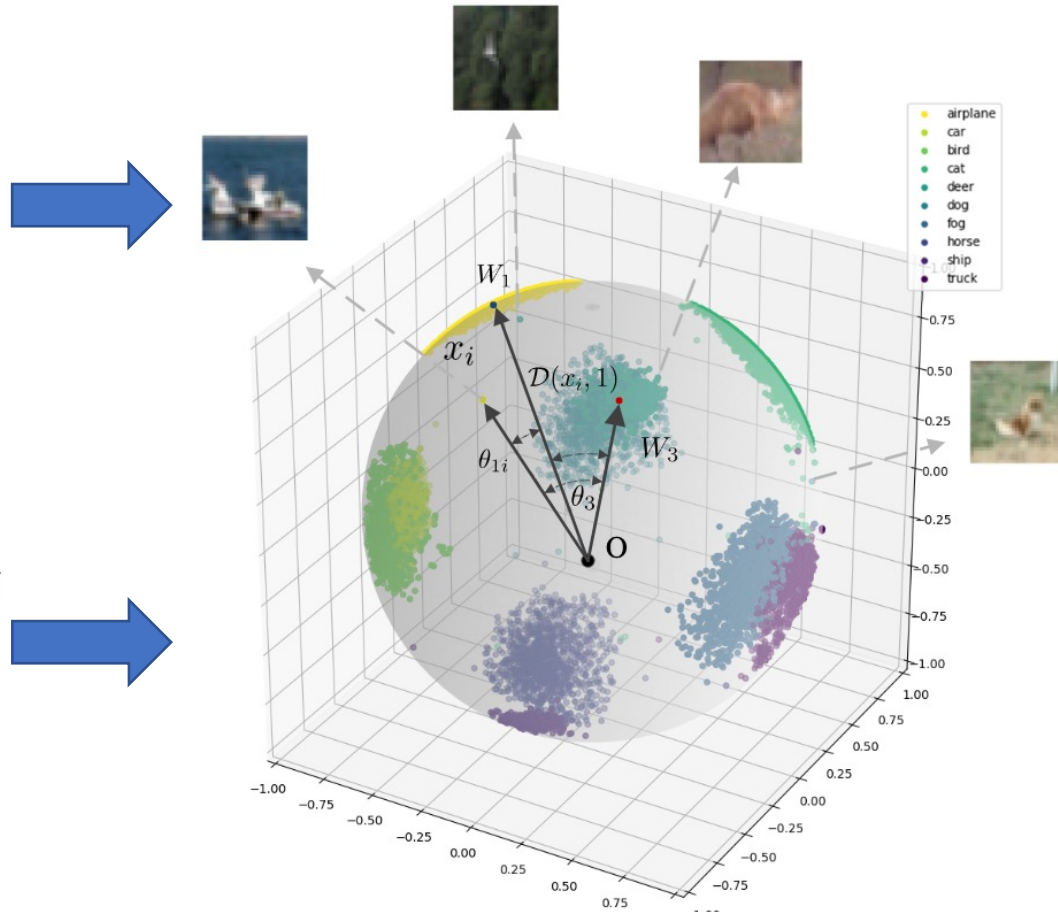
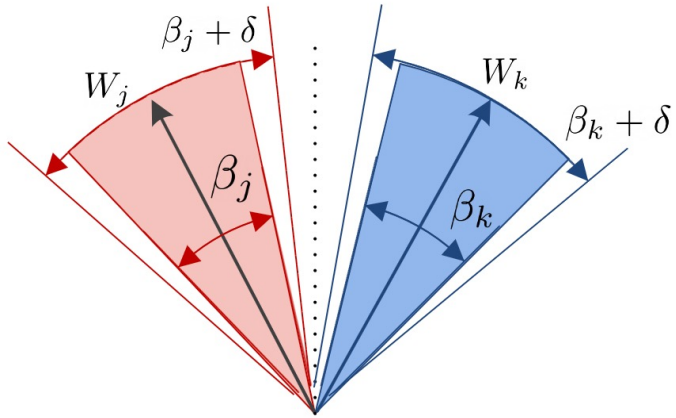
**Curricular CST**

## 2. Multilevel model calibration

class-wise



global

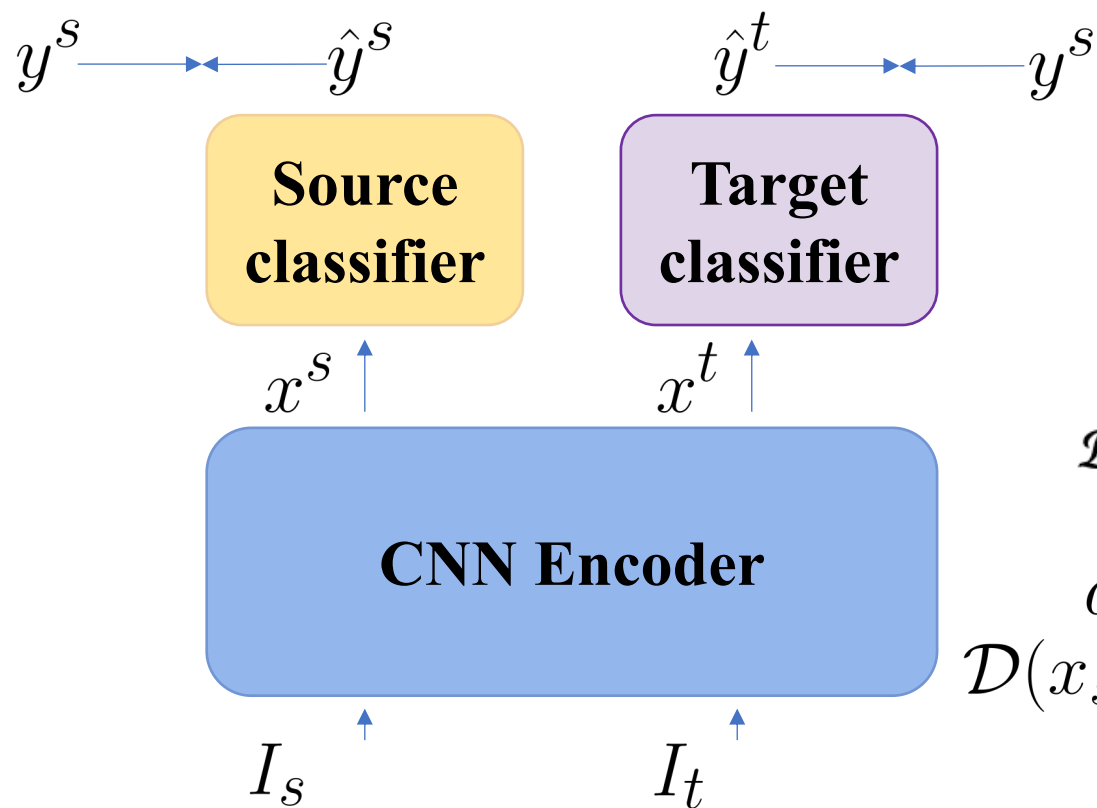


$$\mathcal{D}(\mathbf{x}, \mathbf{y}) = \text{sim}(\mathbf{x}, \mathbf{w}_y) - \arg \max_{k \neq y} \text{sim}(\mathbf{x}, \mathbf{w}_k)$$

$$\text{sim}(\mathbf{x}, \mathbf{w}_k) = \cos \theta_k = \frac{\mathbf{x}_i^T \mathbf{w}_k}{\|\mathbf{x}\| \|\mathbf{w}_k\|},$$

### 3. Find the curriculum $d_s$ for distributional shift

Reducing cross-domain discrepancy with a curriculum for CST (Hong Liu, et al 2021)



$$L_{rev} \triangleq \sum_{s \in S} \sum_{t \in T} d_s \| \text{sim}(x_s, x_t) \hat{y}_t - y_s \|^2$$

$$d_s = \sigma(\lambda \cdot \mathcal{D}(x_s, y_s)),$$

$$\mathcal{D}(\mathbf{x}_s, \mathbf{y}_s) = \text{sim}(\mathbf{x}_s, \mathbf{w}_y) - \arg \max_{k \neq y} \text{sim}(\mathbf{x}_s, \mathbf{w}_k)$$

$d_s$  is the curriculum found by grid search.  
 $\mathcal{D}(x_s, y_s)$  is the class-wise calibrated Angular Gap of the source domain samples.

# Experiments

- HSF datasets (**limited resource**)

- CIFAR10-H (Battleday, etc 2020)
- ImageNetV2 (BenjaminRecht, etc 2019)

- Domain adaptation datasets

- Office31 (Saenko, etc 2010)
- VisDA2017 (Peng, etc 2017)

- Intrinsic Evaluation

- Spearman rank correlation analysis ([Charles Spearman](#))
- Kendall Tau correlation analysis ([Maurice Kendall](#) 1938)
- Expected Calibration Error (ECE)

- Extrinsic Evaluation

- classification accuracy on CIFAR10
- Performance on domain adaptation

# Evaluation

**Table1. Correlation analysis of example difficulties and HSF on CIFAR10-H.  
Performance of corresponding curriculum learning.**

Methods	Spearman's rank	Kendall's Tau	ECE	Top-5 acc.	Top-1 acc.
Maximum Confidence	0.266±0.006	0.148±0.004	11.3±0.2	94.5±0.3	74.8±2.1
Maximum Confidence <sub>TS</sub>	0.273±0.004	0.145±0.004	9.1±0.2	94.5±0.3	75.3±2.1
Classification Margin[39]	0.279±0.006	0.142±0.004	11.3±0.2	94.6±0.3	75.3±2.0
Classification Margin <sub>TS</sub>	0.283±0.006	0.242±0.004	9.0±0.2	94.9±0.3	75.7±1.3
MC-Dropout[10]	0.256±0.007	0.176±0.006	9.4±0.4	95.7±0.3	77.0±0.5
AVH[5]	0.368±0.006	0.258±0.004	8.2±0.2	98.2±0.3	81.2±1.0
AVH <sub>Global</sub>	0.376±0.003	0.263±0.003	7.5±0.2	98.6±0.2	81.3±0.7
AVH <sub>Class-wise</sub>	0.377±0.003	0.265±0.002	7.4±0.2	98.6±0.2	81.4±0.6
Forgetting Events[39]	0.260±0.003	0.187±0.002	11.5±0.5	98.0±0.4	78.9±1.2
C-score[18]	0.316±0.001	0.243±0.001	9.8±0.3	99.0±0.1	82.4±0.4
Prediction Depth[1]	0.290±0.001	0.183±0.001	9.8±0.3	98.5±0.2	81.2±0.4
Angular Gap (Ours)	0.378±0.003	0.265±0.003	8.2±0.2	98.6±0.2	82.0±0.6
Angular Gap <sub>Global</sub>	0.382±0.003	0.268±0.002	7.5±0.2	98.8±0.2	82.3±0.4
Angular Gap <sub>Class-wise</sub>	0.384±0.002	0.269±0.002	7.4±0.2	98.9±0.2	82.4±0.4

# Evaluation

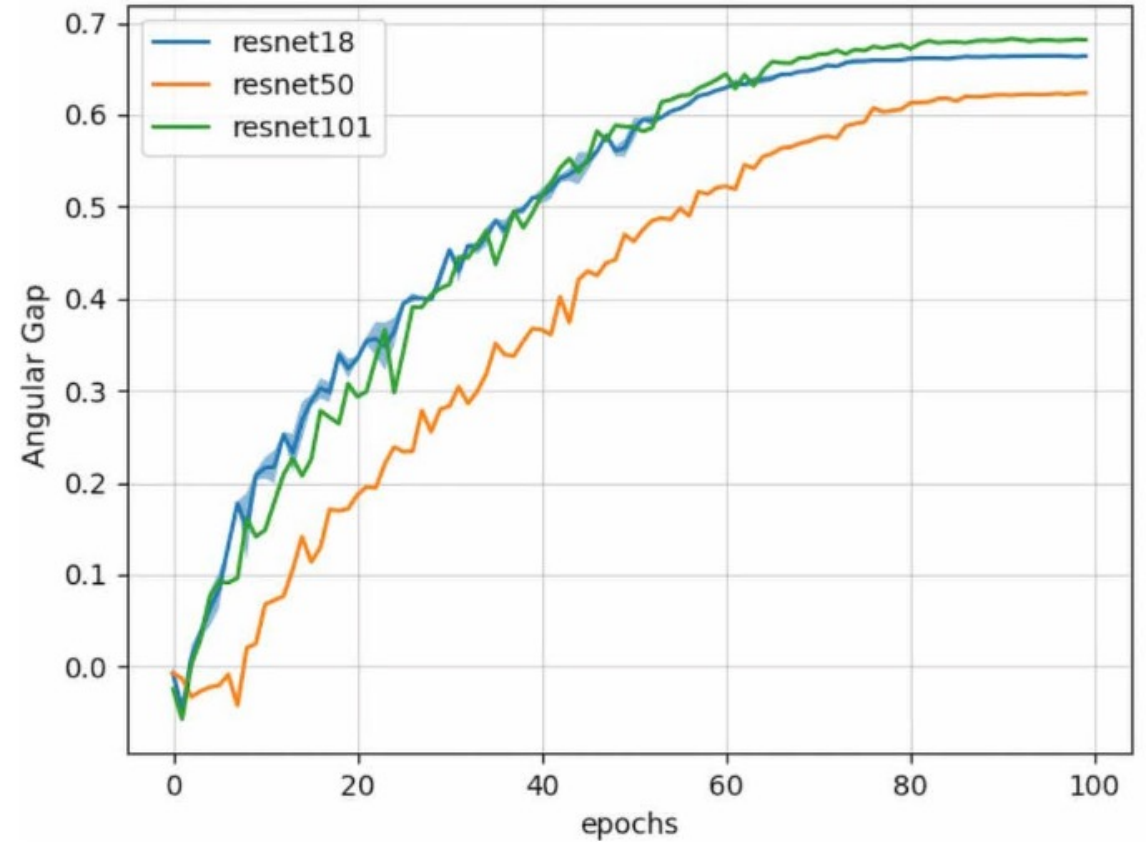
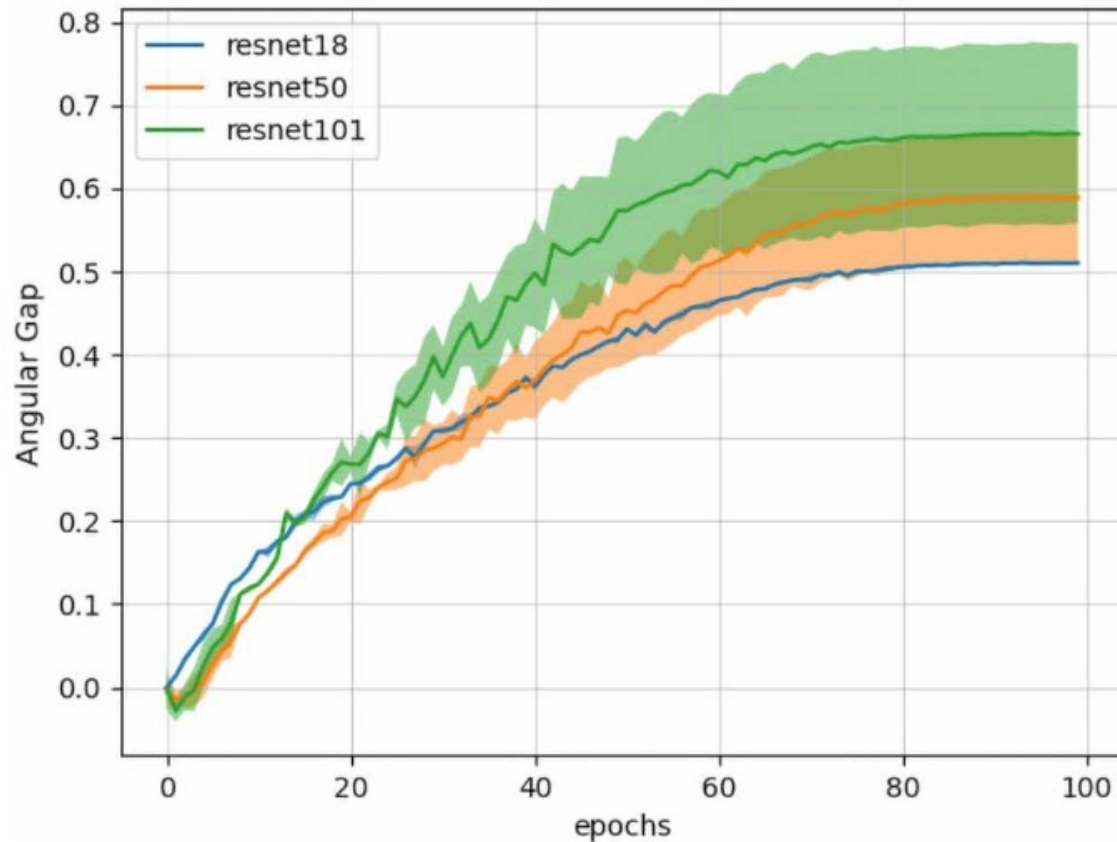
**Table 2: Accuracy (%) for sythetic-to-real on VisDA2017**

Method	Acc.		Method	Acc.
DANN[11]	55.3		CBST[46]	76.4
DAN[27]	61.1		CRST[47]	78.1
MSTN[43]	65.0		FixMatch[38]	76.7
JAN[28]	65.7		CST[25]	79.9
DSAN[45]	74.8		FixBi[29]	<u>87.2</u>
Curricular DSAN	75.4		Curricular CST	<b>88.1</b>

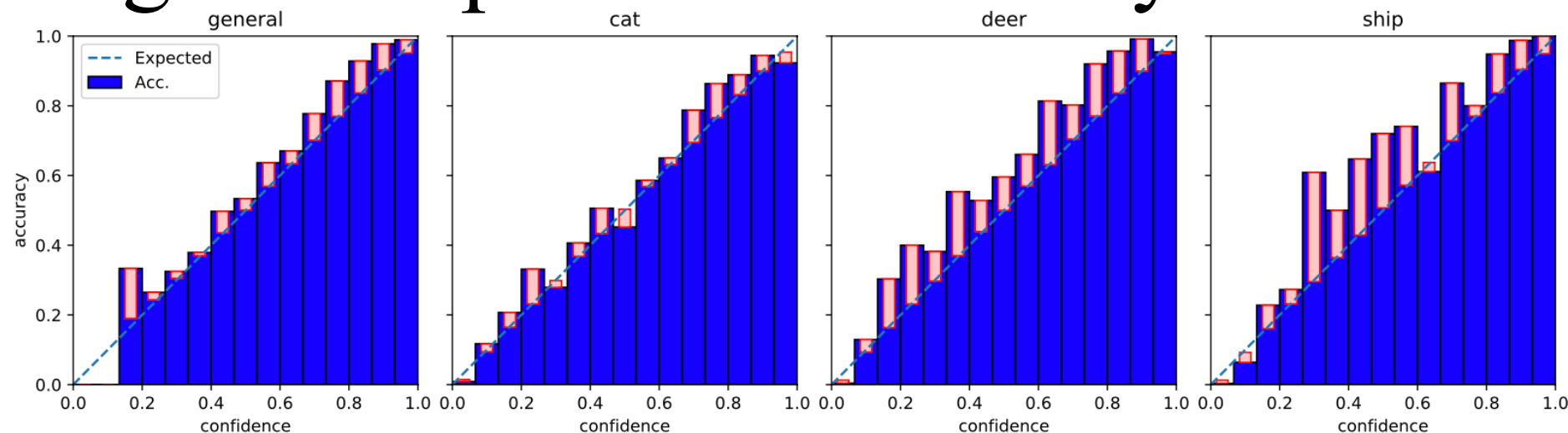


# Why does calibrated Angular Gap work?

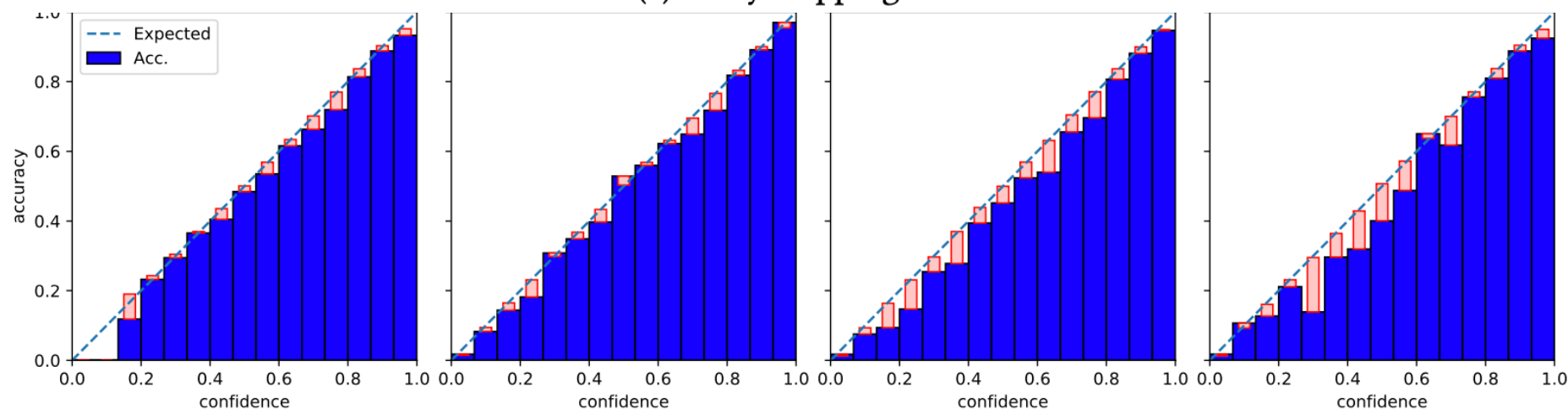
Model calibration reduces the uncertainty and improves robustness of image difficulty estimation.



# Angular Gap uses trustworthy similarities



(a) Early stopping



(b) Class-wise calibration with FN



# Conclusion

- We propose Angular Gap to estimate image difficulty and reduce its uncertainty with class-wise calibration.
- Our results benefit from feature normalization of hyperspherical learning.
- We build an Angular Gap based curriculum with CST for UDA.
- Model calibration benefits image difficulty estimation. Simply scaling up the model leads to unstable difficulty estimation.

Thank you