排序演算法

合併排序、快速排序……

nevikw39

點石學園

August 27, 2021

- 1 Abstract
 - Bubble Sort
- 2 Implementation
 - Merge Sort
 - Inversion
 - Quicksort
 - Quickselect
- 3 Easy-to-use built-in functions
 - std::sort()
- 4 Appendix

Section 1

Abstract

- Abstract
 - Bubble Sort
- 2 Implementation
 - Merge Sort
 - Quicksort
- 3 Easy-to-use built-in functions
- (4) Appendix



Introduction to Sorting

Definition (Sort)

Rearrange elements in an array into a sort of order.

- Monotonicity
- Permutation of original array

Introduction to Sorting

Definition (Sort)

Rearrange elements in an array into a sort of order.

- Monotonicity
- Permutation of original array

Reason

- Ranking
- Prerequisite of other algorithms such as binary search, greedy, \dots

Naïve Approach: Bubble Sort

```
procedure Bubble Sort(\{a_0, a_1, ..., a_{n-1}\})

for i \in [0, n-1) do

for j \in [0, n-1-i) do

if a_j > a_{j+1} then

SWAP(a_j, a_{j+1})

end if

end for

end for

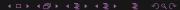
return a

end procedure
```

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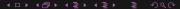


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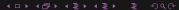


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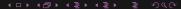
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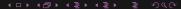
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Section 2

Implementation

- Abstract
 - Bubble Sort
- 2 Implementation
- Merge Sort
 - Inversion
 - Quicksort
 - Quickselect
- 3 Easy-to-use built-in functions
- 4 Appendix



分治三部曲:

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Divide Split original problem into several subproblems

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Conquer Recur to each subproblem until it could be easily solved

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Combine Merge the results of subproblems

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時間複雜度: Master Theorem

分治三部曲:

Divide Split original problem into several subproblems

Conquer Recur to each subproblem until it could be easily solved

Combine Merge the results of subproblems

時間複雜度: Master Theorem

$$T(n) = aT(\frac{n}{b}) + O(n^d) = \begin{cases} O(n^d), & d > \log_b a \\ O(n^d \log n), & d = \log_b a \\ O(n^{\log_b a}), & d < \log_b a \end{cases}$$

合併排序

Divide Split array into left and right subarrays (b = 2, O(1))

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合併排序

Divide Split array into left and right subarrays (b = 2, O(1))Conquer Sort two subarrays recursively (a = 2)

August 27, 2021

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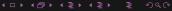
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合併排序

Divide Split array into left and right subarrays (b = 2, O(1))

Conquer Sort two subarrays recursively (a = 2)

Combine Merge two sorted subarrays in O(n)



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Given two sorted subarrays left, right, how could we combine them to a sorted array efficiently??

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合併

Given two sorted subarrays *left*, *right*, how could we combine them to a sorted array efficiently??

Let **itr**, **jtr** point to the begin of *left*, *right* respectively.

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合併

Given two sorted subarrays *left*, *right*, how could we combine them to a sorted array efficiently??

Let itr, jtr point to the begin of *left*, *right* respectively.

If $itr \neq the$ end of $left \land jtr \neq the$ end of right, then we choose the min one and forward the pointer.

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Given two sorted subarrays *left*, *right*, how could we combine them to a sorted array efficiently??

Let **itr**, **jtr** point to the begin of *left*, *right* respectively.

If $\mathbf{itr} \neq \text{the end of } left \land \mathbf{jtr} \neq \text{the end of } right$, then we choose the min one and forward the pointer.

Else if $\mathbf{itr} \neq \text{the end of } left \lor \mathbf{jtr} \neq \text{the end of } right$, then we choose the pointer and forward it.

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Given two sorted subarrays left, right, how could we combine them to a sorted array efficiently??

Let **itr**, **jtr** point to the begin of *left*, *right* respectively.

If itr \neq the end of $left \land jtr \neq the$ end of right, then we choose the min one and forward the pointer.

Else if **itr** \neq the end of *left* \vee **jtr** \neq the end of *right*, then we choose the pointer and forward it.

Repeat until **itr** = the end of $left \land jtr = the$ end of right.

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procedure Merge Sort(*begin, *end)

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```
procedure MERGE SORT(*begin, *end)
  if end - begin = 1 then
    return
  end if
```

 \triangleright 0. Recursion boundary

```
procedure Merge Sort(*begin, *end)
                                                             \triangleright 0. Recursion boundary
    if end - begin = 1 \text{ then}
         return
    end if
    mid \leftarrow \frac{begin + end}{2}, left \leftarrow [begin, mid), right \leftarrow [mid, end) \triangleright 1. Divide
```

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```
procedure MERGE SORT(*begin, *end)

if end - begin = 1 then \Rightarrow 0. Recursion boundary

return

end if

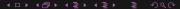
mid \leftarrow \frac{begin + end}{2}, left \leftarrow [begin, mid), right \leftarrow [mid, end) \Rightarrow 1. Divide

MERGE SORT(left.begin(), left.end()) \Rightarrow 2. Conquer

MERGE SORT(right.begin(), right.end())
```

```
procedure Merge Sort(*begin, *end)
    if end - begin = 1 then
                                                         \triangleright 0. Recursion boundary
        return
    end if
    mid \leftarrow \frac{begin + end}{2}, left \leftarrow [begin, mid), right \leftarrow [mid, end) \triangleright 1. Divide
    MERGE SORT(left.begin(), left.end())
                                                                         \triangleright 2. Conquer
    MERGE SORT(right.begin(), right.end())
    itr \leftarrow left.begin(), jtr \leftarrow right.begin()
    while begin \neq end do
                                                                         \triangleright 3. Combine
        if itr \neq left.end() \land (jtr = right.end() \lor *itr < *jtr) then
             *begin ++ \leftarrow *itr ++
        else
             *begin ++ \leftarrow *itr ++
        end if
    end while
```

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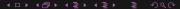
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類題演練

- AtCoder Beginner Contest 154 p. C Distinct or Not
- LeetCode 0004. Median of Two Sorted Arrays (Hard!?)

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Distinct or Not

AtCoder Beginner Contest 154 p. C

Problem

Determine if each element in the array is unique.



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Distinct or Not

AtCoder Beginner Contest 154 p. C

Problem

Determine if each element in the array is unique.

Idea

Use nested loop??



Distinct or Not

AtCoder Beginner Contest 154 p. C

Problem

Determine if each element in the array is unique.

Idea

Use nested loop??

Algorithm

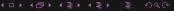
In **combine** process of MERGE SORT, we could check whether ***itr** == ***jtr**.

Median of Two Sorted Arrays

LeetCode 0004 (Hard!?)

Definition (Median)

For an sorted array a whose size is n, if n is odd, then its median is $a_{n/2}$; otherwise, it is $\frac{a_{n/2}+a_{n/2-1}}{2}$



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Median of Two Sorted Arrays

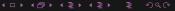
LeetCode 0004 (Hard!?)

Definition (Median)

For an sorted array a whose size is n, if n is odd, then its median is $a_{n/2}$; otherwise, it is $\frac{a_{n/2}+a_{n/2-1}}{2}$

Algorithm

Obviously, all we have to do is to perform **combine** process of MERGE SORT.



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Definition (Inversion)

Given a sequence S. If $i < j \iff S_i > S_j$, then (i, j) or (S_i, S_j) is called a **inversion** of S.

16/38

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Definition (Inversion)

Given a sequence S. If $i < j \iff S_i > S_j$, then (i,j) or (S_i, S_j) is called a inversion of S.

Idea

$$\forall i \in [0, |S|), \forall j \in [i, |S|), \text{ count whether } i < j \iff S_i > S_j??$$

16/38

nevikw39 (點石學園) 排序演算法

Definition (Inversion)

Given a sequence S. If $i < j \iff S_i > S_j$, then (i,j) or (S_i, S_j) is called a inversion of S.

Idea

$$\forall i \in [0, |S|), \, \forall j \in [i, |S|), \, \text{count whether} \,\, i < j \iff S_i > S_j ??$$

Algorithm

When **combining** two sorted subarrays, if *itr > *jtr, then a inversion exists, and *(itr + 1), ... are also greater than *jtr with a smaller index.

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類題演練

- AtCoder Beginner Contest 190 p. F Shift and Inversions
- UVa 10810: Ultra-QuickSort
- UVa 11858: Frosh Week

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AtCoder Beginner Contest 190 p. F

 $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.

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AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\}, \text{ there are 4 inversions: } (1, 0), (2, 0), (3, 0), (4, 0)$

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AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\}, \text{ there are 4 inversions: } (1, 0), (2, 0), (3, 0), (4, 0)$
- $v = \{2, 3, 4, 0, 1\}$, there are 6 inversions: (2, 0), (3, 0), (4, 0), (2, 1), (3, 1), (4, 1)



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AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\}, \text{ there are 4 inversions: } (1, 0), (2, 0), (3, 0), (4, 0)$
- $v = \{2, 3, 4, 0, 1\}$, there are 6 inversions: (2, 0), (3, 0), (4, 0), (2, 1), (3, 1), (4, 1)
- $v = \{3, 4, 0, 1, 2\}$, there are 6 inversions: (3, 0), (3, 1), (4, 0), (4, 1), (3, 2), (4, 2)



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nevikw39 (點石學園) 排序演算法

AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\}, \text{ there are 4 inversions: } (1, 0), (2, 0), (3, 0), (4, 0)$
- $v = \{2, 3, 4, 0, 1\}$, there are 6 inversions: (2, 0), (3, 0), (4, 0), (2, 1), (3, 1), (4, 1)
- $v = \{3, 4, 0, 1, 2\}, \text{ there are 6 inversions:}$ (3, 0), (3, 1), (4, 0), (4, 1), (3, 2), (4, 2)
- $v = \{4, 0, 1, 2, 3\}, \text{ there are 4 inversions: } (4, 0), (4, 1), (4, 2), (4, 3)$



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AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\}, \text{ there are 4 inversions: } (1, 0), (2, 0), (3, 0), (4, 0)$
- $v = \{2, 3, 4, 0, 1\}$, there are 6 inversions: (2, 0), (3, 0), (4, 0), (2, 1), (3, 1), (4, 1)
- $v = \{3, 4, 0, 1, 2\}$, there are 6 inversions: (3, 0), (3, 1), (4, 0), (4, 1), (3, 2), (4, 2)
- $v = \{4, 0, 1, 2, 3\}, \text{ there are 4 inversions: } (4, 0), (4, 1), (4, 2), (4, 3)$
- When removing a from the front of the array, the number of inversion would decrease by a for a is the a-th smallest element in the array.

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AtCoder Beginner Contest 190 p. F

- $v = \{0, 1, 2, 3, 4\}$, there are 0 inversions.
- $v = \{1, 2, 3, 4, 0\},$ there are 4 inversions: (1, 0), (2, 0), (3, 0), (4, 0)
- $v = \{2, 3, 4, 0, 1\}$, there are 6 inversions: (2,0),(3,0),(4,0),(2,1),(3,1),(4,1)
- $v = \{3, 4, 0, 1, 2\}$, there are 6 inversions: (3,0),(3,1),(4,0),(4,1),(3,2),(4,2)
- $v = \{4, 0, 1, 2, \overline{3}\}\$, there are 4 inversions: $(4, 0), \overline{(4, 1)}, \overline{(4, 2)}, \overline{(4, 3)}$
- When removing a from the front of the array, the number of inversion would decrease by a for a is the a-th smallest element in the array.
- In like manner, when appending a to the back of the array, the number would increase by N-1-a because a is less than N-1-a elements in the array.

快速排序

Divide Select a *pivot* value and separate the array into *less* partition and *greater* partition (b = 2, O(n))

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快速排序

Divide Select a pivot value and separate the array into less partition and greater partition (b = 2, O(n))

Conquer Sort two partitions recursively (a = 2)



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快速排序

Divide Select a *pivot* value and separate the array into *less* partition and *greater* partition (b = 2, O(n))

Conquer Sort two partitions recursively (a = 2)

Combine Nothing to do, the array have been sorted. (O(1))



原地分割 (In-place Division)

How could we separate the array into *less* partition and *greater* partition??

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How could we separate the array into *less* partition and *greater* partition??

Suppose two partitions are [begin, itr) and [itr + 1, end).

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How could we separate the array into less partition and greater partition??

Suppose two partitions are [begin, itr) and [itr + 1, end).

Initially, $itr \leftarrow begin$, $pivot \leftarrow end - 1$.



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nevikw39 (點石學園) 排序演算法

How could we separate the array into *less* partition and *greater* partition??

Suppose two partitions are [begin, itr) and [itr + 1, end).

Initially, $itr \leftarrow begin, pivot \leftarrow end - 1$.

We traverse from begin through pivot with jtr.



How could we separate the array into *less* partition and *greater* partition??

Suppose two partitions are [begin, itr) and [itr + 1, end).

Initially, $itr \leftarrow begin, pivot \leftarrow end - 1$.

We traverse from begin through pivot with jtr.

If *jtr < *pivot, then we put it to *itr and forward itr.



How could we separate the array into *less* partition and *greater* partition??

Suppose two partitions are [begin, itr) and [itr+1, end).

Initially, $itr \leftarrow begin$, $pivot \leftarrow end - 1$.

We traverse from begin through pivot with jtr.

If *jtr < *pivot, then we put it to *itr and forward itr.

Finally, swap *itr and *pivot.



The choice of *pivot* plays a significant role when it comes to the efficiency of QUICKSORT.

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The choice of *pivot* plays a significant role when it comes to the efficiency of QUICKSORT.

In classical textbook "Introduction to Algorithm", C., S., L., R. chose the last element to be pivot.

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The choice of *pivot* plays a significant role when it comes to the efficiency of QUICKSORT.

In classical textbook "Introduction to Algorithm", C., S., L., R. chose the last element to be *pivot*.

Nevertheless, fixed pivot may run into troubles because if unfortunately pivot is minimum or maximum every time, the time complexity would decline to $O(n^2)$.

21/38

The choice of *pivot* plays a significant role when it comes to the efficiency of QUICKSORT.

In classical textbook "Introduction to Algorithm", C., S., L., R. chose the last element to be *pivot*.

Nevertheless, fixed *pivot* may run into troubles because if unfortunately *pivot* is minimum or maximum every time, the time complexity would decline to $O(n^2)$.

With an eye to avoiding this, we can pick *pivot* randomly or use the median of $\{*begin, *(\frac{begin+end}{2}), *(end-1)\}$.

procedure QUICKSORT(*begin, *end)



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```
 \begin{aligned} \mathbf{procedure} \ & \mathrm{QUICKSORT}(*begin, *end) \\ & \mathbf{if} \ end - begin \leq 1 \ \mathbf{then} \\ & \mathbf{return} \\ & \mathbf{end} \ \mathbf{if} \end{aligned}
```

 \triangleright 0. Recursion boundary

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```
procedure Quicksort(*begin, *end)
   if end - begin < 1 then
       return
   end if
   itr \leftarrow begin, pivot \leftarrow end - 1
   for jtr \leftarrow begin; jtr \neq pivot; jtr ++ do
       if *jtr < *pivot then
           SWAP(*itr++,*jtr)
       end if
   end for
   SWAP(*itr, *pivot)
```

 \triangleright 0. Recursion boundary

 \triangleright 1. Divide

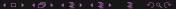
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```
procedure Quicksort(*begin, *end)
   if end - begin < 1 then
                                                   \triangleright 0. Recursion boundary
       return
   end if
    itr \leftarrow begin, pivot \leftarrow end - 1
                                                                    ▶ 1. Divide
   for jtr \leftarrow begin; jtr \neq pivot; jtr +++ do
       if *jtr < *pivot then
           SWAP(*itr++,*jtr)
       end if
   end for
   SWAP(*itr, *pivot)
    Quicksort (begin, itr)
                                                                 \triangleright 2. Conquer
    Quicksort(itr + 1, end)
```

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```
procedure Quicksort(*begin, *end)
   if end - begin < 1 then
                                                    \triangleright 0. Recursion boundary
        return
   end if
    itr \leftarrow begin, pivot \leftarrow end - 1
                                                                    ▶ 1. Divide
   for jtr \leftarrow begin; jtr \neq pivot; jtr +++ do
        if *jtr < *pivot then
           SWAP(*itr++,*jtr)
        end if
   end for
   SWAP(*itr, *pivot)
    Quicksort (begin, itr)
                                                                  \triangleright 2. Conquer
    Quicksort(itr + 1, end)
                                                                  \triangleright 3. Combine
end procedure
```

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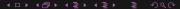


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Problem

Find the k-th element in the array.



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快速選擇 Quickselect

Problem

Find the k-th element in the array.

Idea

Sort the array??



快速選擇 Quickselect

Problem

Find the k-th element in the array.

Idea

Sort the array??

Algorithm

When **dividing** array into *less* and *greater* parts in QUICKSORT, we could know the size of them. If k < |less|, we only need to recur to less part and greater one could be ignored; vice versa.

Note that if we recur to greater part, we should update k to k - |less| - 1 because the k-th element in the original array is k - |less| - 1-th element in the greater part.



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類題演練

- LeetCode 0215. Kth Largest Element in an Array (Medium)
- AtCoder Beginner Contest 161 p. C Popular Vote

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Kth Largest Element in an Array

LeetCode 0215 (Medium)

非常單純的模板題,我們以此來示範 pivot 之選擇。

Always last 40ms, beats 17.10% submissions

Randomly 8ms, faster than 75.44% codes



Section 3

Easy-to-use built-in functions

- 1 Abstract
 - Bubble Sort
- 2 Implementation
 - Merge Sort
 - Quicksort
- 3 Easy-to-use built-in functions
 - std::sort()
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std::merge()

```
void merge sort (vector < int >:: iterator begin,
   vector < int > :: iterator end)
    // 0. recursion boundary
    if (end - begin == 1)
        return:
    // 1. Divide
    auto mid = begin + ((end - begin) >> 1); // equal to
        begin + (end - begin)/2
    vector < int > left (begin, mid), right (mid, end);
    // 2. Conquer
    merge sort(left.begin(), left.end());
    merge sort(right.begin(), right.end());
    // 3. Combine
    merge(left.begin(), left.end(), right.begin(),
        right.end(), begin);
```

std::partition()

```
int pivot;
bool cmp_partition(int x) { return x < pivot; }
void quicksort (vector < int >:: iterator begin,
   vector < int > :: iterator end)
    // 0. recursion boundary
    if (end - begin \ll 1)
        return:
    // 1. Divide
    pivot = *(end - 1);
    auto itr = partition (begin, end -1, cmp partition);
    swap(*itr, *(end - 1));
    // 2. Conquer
    quicksort (begin, itr);
    quicksort(itr + 1, end);
    // 3. Combine
    // Nothing to do
```

std::nth_element()

```
nth\_element(v.begin(), v.begin() + 2, v.end());
cout << "\n2-nd_element_(0-indexed)_is_" <<
   *(v.begin() + 2) << '\n';
```

std::sort()

```
sort(v.begin(), v.end());
for (const int &i : v)
    cout << 'u' << i;</pre>
```

std::sort() with std::string and other...

```
string s = "hello_world_QWERIY_QAZ_QSC_QQ_wasd";
cout << '\n' + s << '\n';
sort(s.begin(), s.end());
cout << s << '\n';</pre>
```

std::sort() using custom comparator

```
bool cmp_sort(int lhs, int rhs) // result be like: {1,
   3. 5. 4. 2. 0
    if (lhs & 1 ^ rhs & 1) // if l\%2 != r\%2
        return lhs & 1; // return true if l is odd
            otherwise return false
    else
        return lhs & 1 ? lhs < rhs : lhs > rhs; // if l,
            r are both odd then return l < r else return
            l > r
    sort(v.begin(), v.end(), cmp sort);
    for (const int &i : v)
        cout << ',,' << i:
```

Section 4

Appendix

- 1 Abstract
 - Bubble Sort
- 2 Implementation
 - Merge Sort
 - Quicksort
- 3 Easy-to-use built-in functions
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Stable sorts vs. Unstable sorts

Definition (Stability)

For non-distinct elements, whether they are outputted in the same order they inputted.

排序演算法

Comparison sorts vs. Distribution sorts

Bubble sort, merge sort, Quicksort and ... are called *Comparison sorts* because all of them are based on a binary boolean relation (oft <) and aimed at swapping all inversions. On the other hand, there are other means.

Age sort UVa 11462

There are up to 2×10^6 people aging between [1, 100] in the country. Our goal is to sort them by their age.

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Counting sort

If the range of input is small enough, then we could record the occurrence of for all element in the range.