## The two curvatures

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31 Aug 2020

#### Abstract

There is published evidence that follicles curve during follicle development and that the presence of hard collagen in the lower dermis at this time interferes with the developing follicle downgrowth causing follicles to grow in a curve. There is also evidence of a strong association between fibre diameter, ortho/para cortical segmentation and general follicle size.

Conventional view of fibre curvature is that it is caused by differences in the ortho and para cortex. It is proposed that this may not be correct, and that both fibre curvature and microstructure difference between ortho and para cortex are caused by the fibre growing inside a curved follicle.

It is proposed that follicle curvature has two components. Firstly, all follicles in all breeds of sheep are slightly curved and the degree of this component of curvature is related to fibre diameter. Secondly, if a sheep has the type of collagen that is associated with wrinkles, it also has some additional follicle curvature which is caused by collagen interfering with follicle development.

Some data and analyses are presented to support this 'two curvatures' hypothesis. In order for the two curvatures hypothesis to have a feasable mechanism it is necessary to assume that follicle curvature causes fibre curvature. We are able to present some data to support this auxiliary assertion.

### 1 Introduction

Some time ago there was a wool industry which possessed a reasonable working definition of wool quality that was universally understood among producers, traders, and processors. They even went so far as to put a number on it, and to link it to spinning performance. Quality numbers or 'Counts' ranged from 100's to 32's, the number referring to the number of hanks of yarn (each 560 yards long) which could be spun from 1 pound (0.454Kg) of clean wool, at the spinning limit. The concept is obviously tied to particular processing technologies. What is of interest here is the way quality number was assessed. It was a visual appraisal of crimp frequency, with a correction for abnormal handle.

Then it was found that fibre fineness (ie diameter) was a major determinant of spinning performance and softness or handle. There was a period of agonising

over the relationship between crimp frequency and fibre diameter. We show some of these investigations in Figure 1 because they are relevant to our current arguments regarding curvature.

Notice that the crimp/diameter relationship is quite steep at low crimp frequencies, but flattens out as one approaches the higher crimp frequencies of fine Merino wools. We are going to argue that the crimp/diameter relationship was historically quite satisfactory for non Merino wools, and that quality numbers as originally used for British sheep breeds were probably an adequate diameter indicator and therefore did indeed relate to spinning performance. It is the Merino wools for which the quality number system breaks down. We will present new data making this clear; the above published material has an inadequate range, and is just what originally pointed us to the concept of crimp frequency relating to diameter for coarse wools but not for Merino.

Eventually measured fibre diameter replaced subjective quality numbers as a descriptor of wool sold in Australia, and elsewhere. The industry settled down to a period of about 20 years using fibre diameter alone. Then Paul Swan's thesis appeared defining fibre curvature and establishing a basic measurement method for fibre snippets and showing the importance of measurement conditions in ensuring that the fibre was relaxed for measurement (Swan(1993) [12]). Fibre specification eventually became a dual parameter affair, with fibre diameter and fibre curvature both specified, but there is some doubt regarding the validity of the measurement conditions for fibre curvature with both Laserscan and OFDA measurement methods.

In the middle of these market specification upheavals, sheep breeders also moved from quality numbers to fibre diameter, acknowledging that breeding of fine Merinos towards higher and higher quality numbers had not led to finer fibre diameters. Breeders also became interested, following the work of Nay(1966) [9], in follicle curvature. Follicle curvature was shown to be genetically correlated with staple crimp frequency, wrinkle score, and bulk compression measurement. The curvature of a follicle was always thought to be the same thing as the intrinsic curvature of a properly relaxed fibre, because it corresponded to the curvature with which the fibre emerged from the follicle. This was never proven. A formula converting follicle curvature scores to intrinsic radius of curvature was established by Jackson and Watts(2016) [8].

The focus of this document is on what causes follicles and fibres to be curved. There are two schools of thought on causation

classic view fibres curve because of their internal structure. In sheep like fine Merinos with a bilateral ortho/para cortical structure, the paracortex is always on the inside of the curve. It is asserted that the paracortex contracts more during keratinization and thus causes the fibre to curve. The follicle passively follows what happens to the fibre. In coarser wooled sheep without bilateral cortical structure this is less clear, but Hynd et al. (2009) [5] assert there is asymmetry in mitotic activity and keratinisation.

follicle view fibres curve because they form inside a curved follicle. The spatial environment in which the bulb cells differentiate influences their develop-

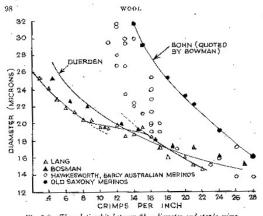
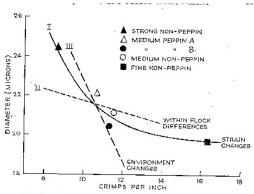


Fig. 5.3 The relationship between fibre diameter and staple crimp in merino woods as summarised by Roberts and Dunlop

#### (a) Reviewed by Roberts and Dunlop



CRIMPS PER INCH

Fig. 5.4 Summary of fineness-crimp relations for Australian strains of merino studied by Roberts and Dunlop. Curve I represents the changes in diameter per unit change of crimp as different strains are studied in the same environment. The slope of line II represents the rate of change of diameter with crimp within any one age group in one flock of one strain. The slope of line III represents the change of fineness associated with unit change of crimp resulting from changes of environment upon any one flock of one strain

(b) Roberts and Dunlop's own data from CSIRO Strain  $\operatorname{Trial}$ 

Figure 1: Crimp frequency fibre diameter relationships from Roberts and Dunlop(1957) [11]. Figures reproduced from Onions(1962) [10]

ment leading to a different internal structure on the inside and outside of curves and a curved fibre shape. The observed differences in internal fibre structure are just a side-effect of forming inside a curved follicle, and are not the cause of curvature. To find the cause of fibre curvature we have to look for what causes follicles to curve.

This document takes the follicle view and attempts to uncover the causes of follicle curvature. It emerges that there is more than one causal factor, and that all are related to skin development, not to fibre structure.

### 2 Causation and association

Everyone u54nderstands that observing a correlation does not prove causation. So what experiments and analyses can one do to establish causation? There are several ways, and we list them

- Do a designed experiment. If the factors studied are the only difference between treatment groups, and there is proper randomization, then one can conclude the factors are responsible for the differences observed.
- Establish a time sequence. If A occurs before B, then it is not possible for B to cause A.
- Find a mechanism. If there is a feasable way in which A could cause B, then it is at least possible for A to cause B. Theories about how things work are very useful here.
- Strong correlation. There has to be some association observable between cause and effect. Observing association is a necessary step to establishing a cause, but it is not definitive.
- Regression with chosen independent X values. This is like a designed factorial experiment.
- Repeatability. If a relation is causal it will always be present.
- Coherence. If a proposed causal relation fits in with other things known and generally accepted in an area, it is likely to be causal. If it is in disagreement, one has to be careful.

Behind most of these points is the concept of confounding. Designed experiments attempt to study factors in isolation. In the real world, especially in biology, we are often forced to study traits varying simultaneously. Causal analysis in this situation is difficult. One approach is to fit a model corresponding to one's theory of causation and to show that it is a good fit to the data.

## 3 Which comes first follicle or fibre curvature?

Evidence on the time sequence of follicle and fibre curvatures is not readily found. There is a photomicrograph in the classic study of Hardy and Lyne (1956) [3] which shows developing follicles in vertical section before the fibre growth has commenced. This photomicrograph is important so we reproduce it here in Figure 2

The fibre does not start to form before stage F4 and does not emerge from the follicle until stage F8. The first three photomicrographs, ie before stage F4, and the developing follicles show some curvature, especially in the second Figure. The fourth Figure shows branching follicles at day 102. This is hardly convincing evidence. The degree of curvature is slight. It is suspected that the Hardy and Lyne used a strong wooled Merino, as this would have been easier material to study vertical sections.

## 4 Follicle curvature and collagen

As part of a study of association of collagen amount and type with wrinkle, it was observed that sheep in two groups chosen as wrinkle-free or wrinkled differed in amount and type of collagen in the lower dermis (Watts et al. (2020) [13], but also differed in follicle curvature. The group means for follicle curvature, and for fibre diameter, are shown in Table 1

Table 1: Means for follicle curvature, fibre diameter and integrated collagen optical density for wrinkled and wrinkle-free groups of sheep

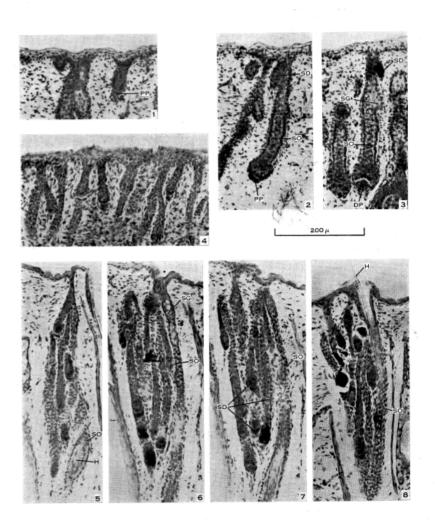
	Wrinkle-free	Wrinkled
Follicle curvature (score 1-7)	2.16	4.44
Fibre diameter (micron)	17.26	18.15
Integrated collagen density (OD)	280851	362991

The groups were chosen to differ in wrinkle. It has been proposed that the observed collagen difference is the cause of the difference in wrinkle (Watts et al. (2020) [13]). We are wondering whether the collagen difference is not also the cause of the difference in follicle curvature.

What we propose is that presence of hard collagen in foetal skin during follicle development causes developing follicles to bend. There is visual evidence of this occuring. Dreyer et al. (1983) [2] published a photomicrograph of Karakul sheep foetal skin in vertical section at 128 days. We reproduce it here in Figure 3

We quote Dreyer et al

"The impression gained was that owing to the vigour of the follicle bulb, the constituent collagen fibres of the hypodermis were displaced in some cases, but no real piercing of that tissue took place. In other cases it would appear theat the follicle bulb and the papilla



### (a) Plate I from Hardy and Lyne(1956) [3]

### EXPLANATION OF PLATES 1 AND 2

All figures are of sections through skin from the trunk of Merino foctuses. The staining is with haemalum, eosin, and picric acid, except Plate 1, Fig. 4, which is without picric acid. DP, dermal papilla; G, stratum germinativum; H, hair; HN, hair cone; P, periderm; PP, prepapilla; S, stratum spinosum; SD, derived secondary follicle; SG, sebaceous gland; SO, original secondary follicle.

(b) Caption from Hardy and Lyne(1956) [3]

Figure 2: Follicles at some early stages of development

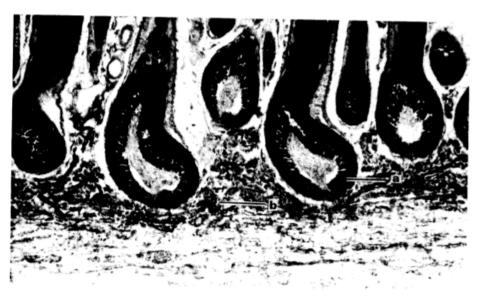


Figure 14b Deflected follicle bulbs on hypodermal layer. Pipe curl. Vertical section. Tail position. 128 days pre-natal. Magn. 114×. a. Follicle bulb. b. Hypodermis.

Figure 3: Photomicrograph of foetal skin from Dreyer et al. (1983) [2] showing follicle bulbs deflecting on contact with the collagen layer. Karakul sheep at  $128~\mathrm{days}$ 

were undergoing some degree of flattening due to growth pressure on the barrier layer......This barrier effect could also explain the deflection of the bulb to any side as it reacts to the force exerted by downward growth"

This clearly establishes that the dark stained collagen layer in Figure 3 acts as a barrier to downward growth of follicles. If the follicles continue to grow, they must deflect sideways, and this will result in a curved follicle.

## 5 Follicle curvature without collagen

All follicles in non-Merino breeds of sheep have a slight degree of curvature, and their fibres or staples have a range of crimp frequencies less than one up to about 4 crimps per cm. We may have to exclude Downs wool breeds, here because they have very curved and tangled follicles, and I suspect they have hard collagen induced follicle curvature like Merinos.

We have to consider what causes the curvature of follicles in sheep which do not have hard collagen? The first thing to note is it appears to be quite strongly related to fibre diameter. There are data supporting this in Figure 1 and in the subsection below.

Follicles have an inherant asymmetric design. They have a thicker inner and outer root sheath on the ental side (side to which the muscle is attached in primary follicles), and this side is usually the outside of the curve. The bulb sometimes deflects toward this side. Larger follicles tend to be less curved, hence the connection between curvature and fibre diameter, because larger follicles tend to grow larger fibres (Henderson(1964 a [4]).

# 5.1 Data supporting proposal that curvature relates to diameter in non-Merino breeds, but not in Merino

The breed survey data of Carter(1968) [1] offer some support. There are no follicle or fibre curvature measurements, but there is crimp frequency and diameter. So we shall look at the crimp/diameter relationship across breeds in particular comparing non-Merino with Merino data. Figure 4 plots breed means of fibre diameter against crimp frequency

There is a clear straight line relationship for crimp frequencies up to about 4 crimps per cm. In the Merino range ( 4 to 8 crimps per cm) there is no relationship at all, and there is one outlier Downs wool breed mean in that range.

These data have limitations. There are not enough replicate points. We are using crimp frequency as a proxy for follicle curvature. Each point is a mean of about 20 sheep sampled from one flock representing the breed. The only positive is that it extends Figure 1 into the non-Merino breeds.

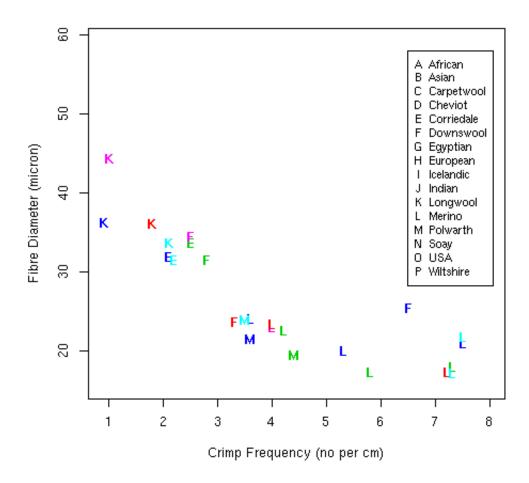


Figure 4: Crimp frequency fibre and diameter breed means from Carter(1968) [1]. Each point is mean of about 20 sheep from one flock representing a breed.

## 6 Can we separate two causes for curvature?

We are proposing that there is one follicle curvature, that all sheep have, that is related to fibre diameter and follicle size, and that there is a second follicle curvature that only Merinos have, that is caused by presence of hard Type I collagen in the lower dermis.

Can we separate these *two curvatures* by analysing data? I propose that we can use regression analysis to remove the diameter related part of follicle curvature variation, and then study the remaining variation and see if it relates to collagen measurements.

# 6.1 Does diameter corrected follicle curvature relate to collagen measurements?

The only available data that include collagen measurements, follicle curvature and fibre diameter are from the collagen/wrinkle experiments reported by Watts et al. (2020) [13]. Taking all available data from this experiment, we look first at the regression of follicle curvature on mean fibre diameter. This is shown in Figure 5

Figure 5 shows all data points, the regression line (Fc - 7.68 + 0.621 \* D) and the product moment correlation (0.61). So part of the follicle curvature of these sheep is clearly diameter related. The problem is this observed relationship is positive - the finer fibre diameter are *less* curved. According to our hypothesis (which is supported by the Carter(1968) [1] data), this relationship should be negative.

THIS IS A SERIOUS ISSUE WHICH PUTS A QUESTION OVER THE HYPOTHESIS THAT PART OF FIOLLICLE CURVATURE IS DIAMETER RELATED. IT WAS THOUGHT THAT THE CARTER DATA IN Figure 4 SUPPORTED A DIAMETER-RELATED EFFECT ON CURVATURE. THAT MAY BE WRONG. WE NEED TO PAUSE AND DO 3 THINGS: 1. LOOK AT A LARGER DATA SET (THE PRESENT SMALL DATA SET MAY BE BIASED FOR SOME REASON) and 2. THINK WHETHER OUR INTER-PRETATION OF Figure 4 IS CORRECT, and 3. SEE IF WE CA ANALYSE THIS SMALL DATASET ANOTHER WAY

#### 6.2 Follicle curvature and fibre diameter in Merinos

The relationship of follicle curvature with fibre diameter can be checked from published estimates. Table 2 presents published estimates of phenotypic, genetic and environmental correlation. Standard errors can be obtained from the sources, they are a distraction here.

The correlations are all positive. So we conclude the small dataset above is not atypical or biased. Follicle curvature really does have a positive relationship with mean fibrte diameter in Merino sheep.

Now what about diameters of primary and secondary fibres? Estimates of correlations of follicle curvature with Dp and Ds are given in Table 3

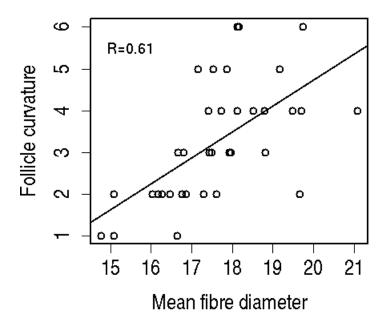


Figure 5: Scatterplot of follicle curvature against mean fibre diameter for 35 sheep in the trial of Watts et al. (2020) [13]. Line is the fitted regression (Fc - 7.68 + 0.62 \* D), and correlation is shown as R = 0.61.

Table 2: Published estimates of phenotypic, genetic and environmental correlation between follicle curvature score and mean fibre diameter

Reference	Phenotypic cor-	Genetic correla-	Environmeltal
	relation	tion	correlation
Jackson Nay and Turner	0.26	0.32	0.22
(1975) [7]			
Jackson(2017) [6]	0.35	0.13	0.62

Table 3: Estimates of phenotypic, genetic and environmental correlation between follicle curvature score and mean fibre diameter of primary and secondary fibres (Jackson(2017) [6]

Traits	Phenotypic cor-	Genetic correla-	Environmeltal
	relation	tion	correlation
Fc x Dp	-0.02	-0.32	0.25
Fc x Ds	0.33	0.72	0.03

This is more complicated. At least at the genetic level, follicle curvature is negatively correlated with Dp, but positively correlated with Ds. So our hypothesis of a D related curvature component works for primary fibres, but not for secondary fibres. That partly explains Carter's data shown in Figure 4 - In the non-Merino breeds where there is this negative crimp frequency x diameter relation, primary fibres are a much larger proportion of the fibre population. It may be that the negative relationship obtained for primary fibres also applies to So ( secondary original fibres), because , as with primary fibres, So fibres form at initiation sites. P and So fibres would be all the fibres in non-Merino breeds.

It is conceivable that follicle curvature in Sd fibres is different, and that would explain why Merinos have a different  $Fc \times D$  relationship. One way in which curvature of Sd follicles could be different is that Sd follicles are formed at the same time as collagen is formed , at around 100 days of gestation. So collagen may only interfere with the curvature of Sd fibres.

## 6.3 Does Dp corrected follicle curvature relate to collagen measurements?

We attempt to repeat the above rejected analysis, using Dp to remove the follicle size effect on follicle curvature, instead of D.

Table 6 shows follicle curvature plotted against primary fibre diameter for the data from the collagen/wrinkle experiment of Watts et al.(2020) [13].

The correlation is positive, and almost identical to the correlation of Fc x D. So this dataset is different from the large datasets from which published estimates of correlation were reported in Section 6.2.

We can not proceed with the use of Dp to adjust Fc in this small dataset.

# 6.4 Can we do the stepwise analysis in reverse order, adjusting follicle curvature first for collagen?

This is a last ditch desperate approach. We are trying to prove that collagen affects follicle curvature. The diameter effect on follicle curvature is the nuisance relationship which should be adjusted out first. But that is proving difficeult, so we can try adjusting out the collagen effect on curvature, and see what variation remains.

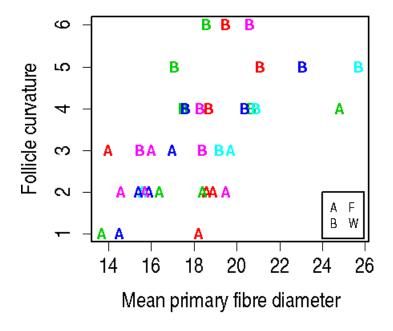


Figure 6: Scatterplot of follicle curvature against mean primary fibre diameter for 35 sheep in the trial of Watts et al. (2020) [13]. The correlation is R=0.59.

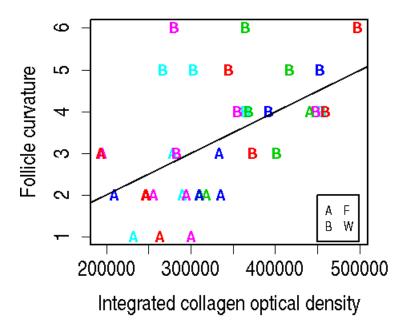


Figure 7: Scatterplot of follicle curvature against integrated collagen optical density for 35 sheep in the trial of Watts et al. (2020) [13]. Line is the fitted regression ( $Fc \ 0.96 + 0.00584 * C$ ), and correlation is R = 0.55. The point labels (A,B) represent wrinkle-free (F) and wrinkled (W) sheep respectively.

Figure 7 shows the plot of follicle curvature against collagen measurement. The correlation is positive (0.55), as expected. The regression line was Fc~0.9601 + 5.843e - 03\*C. The wrinkled sheep (labelled B) have more collagen and a higher follicle curvature, so the difference between the wrinkled and wrinkle-free groups is contributing to the correlation and the regression.

We can now look to see what variation remains in Fc|C, by computing the residuals for follicle curvature in Figure 7. These residuals are shown as a histogram in Figure 8.

The mean in Figure 7 is zero because the regression fit takes out the mean of Fc as well as its regression on C. There is still a considerable amount of variation in Fc remaining after adjusting for collagen. The variance of Fc is 2.104. The variance of Fc|C is 1.470. The collagen explains about 30 percent of the variance of Fc, but 70 percent remains unexplained. This unexplained 70 percent of Fc contains measuring errors and the mysterious-supposedly-diameter-related-part-of-Fc.

## Histogram of resid(curvanal.lm5)

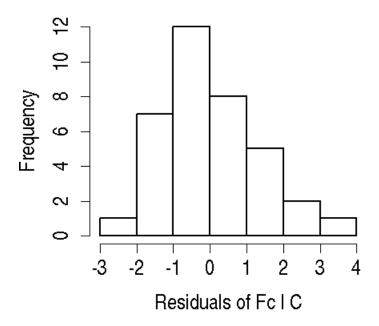


Figure 8: Histogram of residual variation in follicle curvature after adjusting for regression on integrated collagen optical density

So let us see what Fc|C relates to? Table 4 shows correlatios of Fc|C with all other available traits.

Table 4: Correlations of follicle curvature adjusted for collagen optical density with other traits

Trait	Correlation
Fibre diameter	0.51
Primary fibre diameter	0.29
Secondary fibre diameter	0.58
Follicle density	-0.54
S/P ratio	-0.57
Collagen integrated optical density	0.00

There is a positive correlation of Fc|C with fibre diameter. Since this positive relation is what we find perplexing, we look closely at scatterplot (Figure 9

We see that most of the correlation comes from the group difference between wrinkled and wrinkle-free sheep. However the correlation within each group is still positive. We can therefore conclude that while the group difference introduces a potential bias in the correlation, it does not change the sign. There is a bigger issue here than a bit of bias in this rather limited dataset.

We have to find another way of splitting Fc into two components. No amount of fiddling of this small dataset will produce a result which supports our hypothesis of a negative diameter related curvature component. It does support existence of a positive collagen related curvature component.

#### 6.5 Follicle curvature analysis in a large Merino dataset

There are plenty of large follicle curvature datasets on Merinos. The problem is none of them have collagen measurements. What we propose to do is to use wrinkle score as a *proxy* for collagen. Either raw wrinkle score, or perhaps wrinkle score adjusted for S/P ratio (this would hopefully represent the part of wrinkle reflecting collagen amount and type).

### 7 Mechanisms

## References

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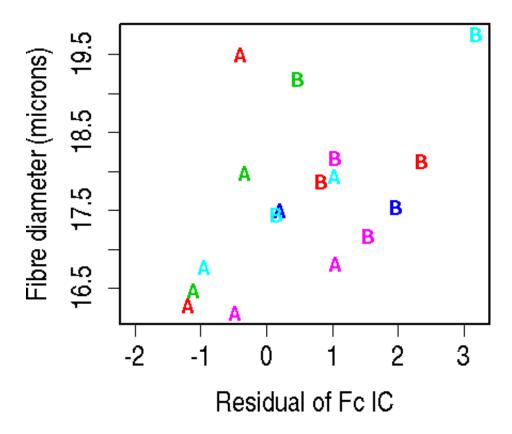


Figure 9: Scatterplot of follicle curvature adjusted for integrated collagen optical density against fibre diameter for 17 sheep in the trial of Watts et al. (2020) [13]. The correlation is shown as R=0.56. The point labels (A,B) represent wrinkle-free (F) and wrinkled (W) sheep respectively.

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