



2.6.2)  $S \rightarrow x | x^* | x^* x^* | x^* x^* x^*$   
 $\rightarrow x \rightarrow x^* | x^* x^* | x^* x^* x^*$   
 $T \rightarrow x^* | x^* x^* | x^* x^* x^*$

2.1a) all strings of the form  $a^n b^n$   
 where  $n \geq 1$   
 $L(a) = \{ \text{all strings of form } a^n b^n \}$   
 $S \rightarrow a^* b^* \Sigma$

2.27) Prove G ambiguous for str.  
 if cond then  
 if cond then  
 $a := 1$   
 else  
 $a := 0$

stmt  $\rightarrow$  if then  
 $\rightarrow$  if cond then stmt  
 $\rightarrow$  if cond then if then else  
 $\rightarrow$  if cond then if cond then stmt else stmt  
 $\rightarrow$  if cond then if cond then assign else stmt  
 $\rightarrow$  if cond then if cond then  $a := 1$  else assign  
 $\rightarrow$  if cond then if cond then  $a := 1$  else  $a := 0$

stmt  $\rightarrow$  if then else  
 $\rightarrow$  if cond then stmt else stmt  
 $\rightarrow$  if cond then if then else stmt  
 $\rightarrow$  if cond then if cond then else stmt  
 $\rightarrow$  if cond then if cond then  $a := 1$  else stmt  
 $\rightarrow$  if cond then if cond then  $a := 1$  else assign  
 $\rightarrow$  if cond then if cond then  $a := 1$  else  $a := 0$

2.27.4) Unambiguous.

$S \rightarrow A | \Sigma$   
 $S' \rightarrow A | E$   
 $E \rightarrow a S' b S$   
 $A \rightarrow C$

2.28) ambiguous  $S \rightarrow a S b | a S | \epsilon$   
 unambiguous  $S \rightarrow a S b | a S | T | \epsilon$   
 $T \rightarrow a T | a$

$S \rightarrow \epsilon | S' | S''$   
 $S' \rightarrow P | P S' | a P | P S''$   
 $S'' \rightarrow O | Q S'$   
 $P \rightarrow a S | a P b | a P P | a P P P$   
 $Q \rightarrow b a | b a a | b a a a | a Q a Q$

6.  $W = \text{str w/ equal \# a's}$   
 $\exists$  more substrs of  $W$  had equal #a's but substrs of  $W$  has more or are than other

each step is grammar  
 $S \rightarrow a b S$   
 $S \rightarrow b a S$   
 $S \rightarrow \epsilon$   
 if  $a \neq b$  more by same amount  
 so not can't have  $\#a \neq \#b$

by induction & contradiction, scanner only generates strings of equal #a's & b's

7. DFA D assume one state = NT.  
 line state  $q_0$  = start var.  
 transition = terminal symbol  
 added to one state  
 add 2 accepting states  
 every reg lang is CFL.

