## ECE113: Digital Signal Processing

## Homework 3 Due: Jan 26 11:00pm, 2022

Instructor: Prof Abeer Alwan

#### Instructions

1. Read Chapters 5 and 6.

## Chapter 5

# Impulse Response Sequence

#### 1. Problem 5.11.

Which of the following LTI systems are FIR or IIR?

(a) 
$$h(n) = u(n) - u(n - 10)$$

(b) 
$$h(n) = (\frac{1}{2})^n u(n-3)$$

(c) 
$$\{y(n) = \frac{1}{2}y(n-1) + x(n), relaxed\}$$

#### 2. Problem 5.17.

A system is described by the input-output relation

$$y(n) = x(3n - 1)\cos\left(\frac{\pi}{3}n\right)u(n + 5)$$

Is the system linear? causal? time-invariant? BIBO stable?

#### 3. Problem **5.31**.

Find a difference equation to describe the input-output relation of the LTI system whose impulse response sequence is given by

$$h(n) = \delta(n-1) + \frac{1}{3}\delta(n-2) - \frac{1}{4}\delta(n-3)$$

- (a) What is the response of the system to  $x(n) = e^{j\frac{\pi}{3}n}u(n)$ ?
- (b) What is the response of the system to  $x(n) = 2\cos\left(\frac{\pi}{6}n + \frac{\pi}{4}\right)u(n)$ ?

# Chapter 6

## **Linear Convolution**

- 4. Problem 6.3. Evaluate the convolution sums:
  - (a)  $u(n) \star (\frac{1}{2})^n u(n-1)$
  - (b)  $u(-n) \star (\frac{1}{2})^n u(n-1)$
  - (c)  $u(2n) \star (\frac{1}{2})^n u(n)$
- 5. Problem 6.11. Evaluate

$$\left[\frac{1}{2}\delta(n+1) - \frac{1}{3}\delta(n)\right] \star \left(\frac{1}{2}\right)^{n-1} \cdot u(n) \star \left(\frac{1}{3}\right)^{n} \cdot u(n-2)$$