

Complexity of computing  $R_1^{-1}$ ,  $R_2^T$ ,  $A_{21} R_1^{-1}$ .

Cholesky factor  $A_{11}$ ,  $A_{22}$  takes  $\frac{1}{3}n^3$  in going to lower  $2n^2$

$R_2^T$  takes  $\frac{1}{3}n^3$

$R_1^{-1}$  takes  $\frac{1}{3}n^3$  to find  $R_1$ ,  $R_1$  is UT

$R_1^{-1}$  is solving  $R_1 X = I$   
column by column =  $\frac{1}{3}n^3$

$A_{21} R_1^{-1} = 2n^3$   $\frac{1}{2}$   $(n \times n) (n \times n)$

Total =  $2n^3 + n^3 = \boxed{3n^3}$