

1. **Naive Bayes Example** You're stuck in a forest with nothing to eat. Suddenly, you spot a mushroom but you don't know if its poisonous. Luckily, you've studied some mushrooms as part of a class to fulfill your undergraduate requirements. Your previous knowledge is summarized by the following chart:

Sample #	IsColorful	IsSmelly	IsSmooth	IsSmall	IsPoisonous
1	0	0	0	1	1
2	0	0	0	0	0
3	1	0	1	1	1
4	1	0	0	0	1
5	0	0	1	0	0
6	0	0	1	0	0
7	1	1	0	0	1
8	1	1	1	0	1
9	0	1	1	0	?

- (a) Build a Naive Bayes classifier to classify the unknown mushroom.

(b) Repeat (a) with Laplace smoothing.

## 2. Discriminative v.s. Generative

So far, we have learned two approaches for binary classification in class. The generative approach model the prior  $P(C_i)$  and class conditional distribution  $P(x|C_i)$ . The discriminative approach model  $P(C_i|x)$  directly. Taking the Naive Bayes classifier for binary feature and label as an example. It model the class prior as a biased coin and model the class conditional distribution for each feature and each class also as a biased coin. From page 122 of the book *A Course in Machine Learning*, we learned that to make a decision, we can use  $\text{sign}(w^T x + b)$  for some  $w$  and  $b$ . Learning  $w$  and  $b$  is then a discriminative approach!

- (a) What is  $w$  and  $b$  in terms of the parameters of Naive Bayes classifier?
  
  
  
  
  
  
  
  
  
  
- (b) Suppose we have  $D$  features, how many parameters does the Naive Bayes classifier have? How many parameters does the linear model have?
  
  
  
  
  
  
  
  
  
  
- (c) Can you compare discriminative approach with generative approach given the above example?

3. More about Discriminative v.s. Generative

Let  $p(x|C_1) \sim 0.4\mathcal{N}(0.2, 0.1) + 0.6\mathcal{N}(0.5, 0.1)$ . Let  $p(x|C_2) \sim \mathcal{N}(0.7, 0.1)$ . In MATLAB, plot the two class conditional distribution and find the decision boundary. Let  $P(C_1) = P(C_2) = 0.5$ , what is the equation to find the posterior distribution for  $C_1$  and  $C_2$ . Find and plot the posterior distribution for  $C_1$  and  $C_2$ .

Find the maximum likelihood decision boundary using both the class conditional distribution and the posterior distribution. Comment on your observation.