b	Since um, should be orthogonal to u, for all 16[1, m]
	and llumill?=1, the new Largeonye Equation is:
	L= Umr. Summer + 2 (1- umr. umr.) + Z & umr. u;
· · · · · · · · · · · · · · · · · · ·	Now we solve this Largraye Equation: partials w.r.t each var.
	O 2 = 1-Umei Umei = 0 = D Umei Umei Umei = 1
	$\boxed{0} \cdot \frac{\partial \mathcal{I}}{\partial \alpha_i} = \mathcal{U}_{mai}^{-1} \alpha_i = 0 \qquad \qquad \frac{\partial \mathcal{I}}{\partial u_{min}} = 2 S u_{mai} = 2 \lambda u_{mai} + \sum_{i=1}^{M} \alpha_i u_i \cdot \mathcal{B}$
	multury both sides by uit
	$2u_{i}^{T}Su_{max}-2u_{i}^{T}\lambda u_{max}+\sum_{i=1}^{M}u_{i}^{T}\alpha_{i}u_{i}=0$
	2 u, summer - 2 u, to um + to ut x; u; = 0 - 2x, u, umay - 2x, u, umay - 2x, u, umay
	/ becam Su; = X; u;
	$\frac{1}{2} u_{s} \cdot \frac{1}{2} u_{s$
	= \d, \\c\ \u_0^\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
	So, $\alpha_3 = 0$ = ∇ 2 u_3 ^T Su _{ma1} = $2u_3$ ^T λu_{ma1} $0 \neq i$
· · · · · · · · · · · · · · · · · · ·	2 Sumi = 2u, 7 Sumi = 1. 1)

(a)
$$S = \frac{1}{N} \frac{2}{n_{21}} (x_{n-x}) (x_{n-x})^{T}$$

$$\frac{1}{N} \sum_{N>1} X_{N} X_{N}^{T} = \frac{1}{4} \left(\begin{bmatrix} 2 \\ 2 \\ 3 \end{bmatrix} \begin{bmatrix} 2 & 2 & 0 \end{bmatrix} - \begin{bmatrix} 0 \\ -2 \\ 2 \end{bmatrix} \begin{bmatrix} 0 & -2 & 2 \end{bmatrix} + \begin{bmatrix} -2 \\ 0 \\ -3 \end{bmatrix} \right)$$

$$\begin{bmatrix} -2 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 0 \\ -2 \end{bmatrix} \begin{bmatrix} 0 & 0 & -2 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

$$\begin{vmatrix} 2-\lambda & 1 & 0 \\ 1 & 2-\lambda & -1 \end{vmatrix} = 0 = 0 \quad (2-\lambda) \left(4-4\lambda+\lambda^2-1\right)-1(2-\lambda) + 0 = 0$$

$$(2-\lambda) \left(2-4\lambda+\lambda^2\right) = 0$$

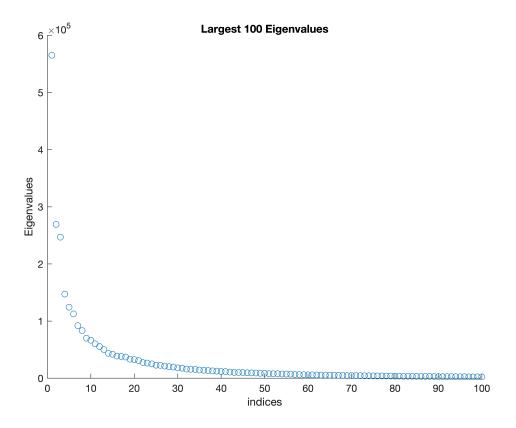
$$\lambda = 2, \quad 4\pm \sqrt{16-8} = 2\pm \sqrt{2}$$

$$\lambda = 2$$
, $\frac{4 \pm \sqrt{16-8}}{2} = 2 \pm \sqrt{2}$

arguert
$$\lambda = 2+\sqrt{3}$$
 -7 $\begin{bmatrix} -\sqrt{2} & 1 & 0 \\ 1 & -\sqrt{2} & -1 \\ 0 & -1 & -\sqrt{2} \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = 0$

Solve, to get
$$a = \frac{6}{52}$$
, $C = -\frac{5}{52}$, $b = 5$. Nometine: $N = \begin{bmatrix} 1/2 \\ 5/2 \\ -1/2 \end{bmatrix}$

```
x = readtable('MNIST5.csv');
x = x{:,:};
covar = cov(x, 1);
[V, D] = eig(covar);
[D, ind] = sort(diag(D), 'descend');
V = V(:,ind);
figure(1);
scatter(1:100, D(1:100));
ylabel('Eigenvalues');
xlabel('indices');
title('Largest 100 Eigenvalues');
```



(b)

```
figure(2);
for i = 1:4
   img = cast(rescale(reshape(V(:,i), [28, 28]), 0, 255), 'uint8');
   subplot(2,2,i);
   imshow(img);
end
title('first four eigenvectors');
```

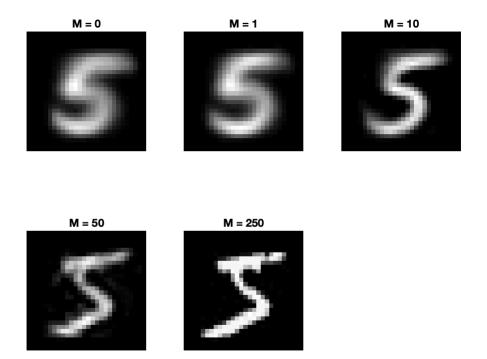








(c)

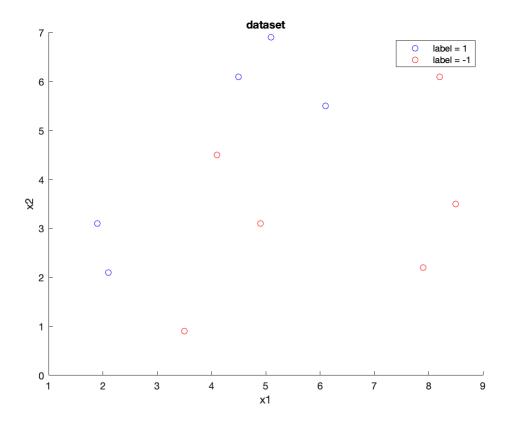


M = 250 is very clear. As M increases it looks like the quality of the image increases and the 5 becomes more distinctive.

when M = 0, it is just the mean vector of all of the test cases.

(a)

```
t = readtable('AdaBoost_data.csv');
x = t{:,1:2};
x1 = x(:,1);
x2 = x(:,2);
y = t{:,3};
figure(1);
hold on;
scatter(x1(y == 1), x2(y == 1), 'blue');
scatter(x1(y == -1), x2(y == -1), 'red');
xlabel('x1');
ylabel('x2');
legend('label = 1', 'label = -1');
title('dataset');
```



No, the data is not linearly separable. No, the data cannot be classified using a single layer decision tree.

(b)

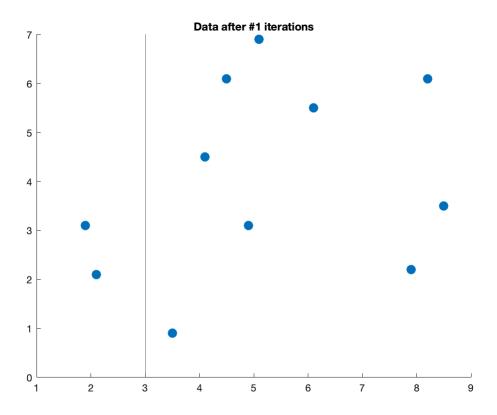
```
i = [1 1 2];
s = [-1 -1 1];
t = [Inf Inf Inf];
N = length(y);
d = zeros(K + 1, N);
d(1,:) = 1 / N * ones(1, N);
a = zeros(K, 1);
```

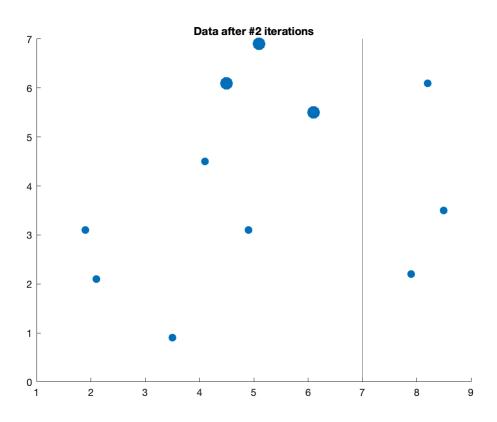
```
for k = 1:3
    xi = x(:,i(k));
    ehatk = Inf;
    yhat = [];
    for tk = floor(min(xi)):ceil(max(xi))
        yh = sign(s(k) * (xi - tk));
        ek = sum(d(k, yh \sim = y));
        if ek < ehatk</pre>
            ehatk = ek;
            t(k) = tk;
            yhat = yh;
        end
    end
    a(k) = 0.5 * log(1 / ehatk - 1);
    d(k+1,:) = d(k,:) .* exp(-a(k) * y .* yhat)';
    d(k+1,:) = d(k+1,:) / sum(d(k+1,:));
end
dvalues = array2table(d(1:3,:)', 'VariableNames', {'d0', 'd1', 'd2'})
```

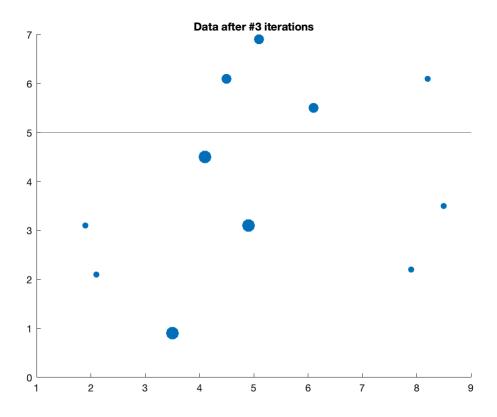
 $dvalues = 11 \times 3 table$

avarac		II'' Cabic		
	d0	d1	d2	
1	0.0909	0.0625	0.0385	
2	0.0909	0.0625	0.0385	
3	0.0909	0.1667	0.1026	
4	0.0909	0.0625	0.1667	
5	0.0909	0.0625	0.1667	
6	0.0909	0.1667	0.1026	
7	0.0909	0.0625	0.1667	
8	0.0909	0.1667	0.1026	
9	0.0909	0.0625	0.0385	
10	0.0909	0.0625	0.0385	
11	0.0909	0.0625	0.0385	

```
xline(t(k));
else
    yline(t(k));
end
```







```
f = zeros(size(y));
for k = 1:K
    f = f + a(k) * sign(s(k) * (x(:,i(k)) - t(k)));
```

```
end
final_combined_classifier = sign(f)'
```

$$acc = 100 * sum(f == y) / N$$

acc = 0