

例 14.1.5

例 14.1.7

习题 14

2.
$$f(x, y) = \begin{cases} 0, & x \text{ 与 } y \text{ 至少有一个是有理数} \\ 1, & \text{otherwise.} \end{cases}$$

$$\lim_{\Delta x \rightarrow 0} \frac{f(x, 0) - f(x, 0)}{\Delta x} = \lim_{\Delta x \rightarrow 0} \frac{0}{\Delta x} = 0 \quad \text{偏导数存在.}$$

$$\lim_{\Delta y \rightarrow 0} \frac{f(0, y) - f(0, y)}{\Delta y} = 0$$

3 (1) $-2, \cos 1$

(2) -2

4. (12) $\frac{\partial u}{\partial x} = z \cdot \left(\frac{x}{y}\right)^{z-1} \cdot \frac{1}{y} = \frac{z}{x} \cdot \left(\frac{x}{y}\right)^z$

$$\frac{\partial u}{\partial y} = z \cdot \left(\frac{x}{y}\right)^{z-1} \cdot \left(-\frac{x}{y^2}\right) = -\frac{z}{y} \left(\frac{x}{y}\right)^z$$

$$\frac{\partial u}{\partial z} = \left(\frac{x}{y}\right)^z \ln \frac{x}{y}.$$

(13).
$$\frac{\partial u}{\partial x_i} = \frac{x_i}{\sum_{j=1}^n x_j^2 + \sqrt{\sum_{j=1}^n x_j^2}}$$

8. $r = (\cos \theta, \sin \theta)$

$$\frac{\partial u}{\partial r} = \frac{\partial u}{\partial x} \cdot \frac{\partial x}{\partial r} + \frac{\partial u}{\partial y} \cdot \frac{\partial y}{\partial r} = \cos \theta \cdot \frac{\partial u}{\partial x} + \sin \theta \cdot \frac{\partial u}{\partial y}.$$

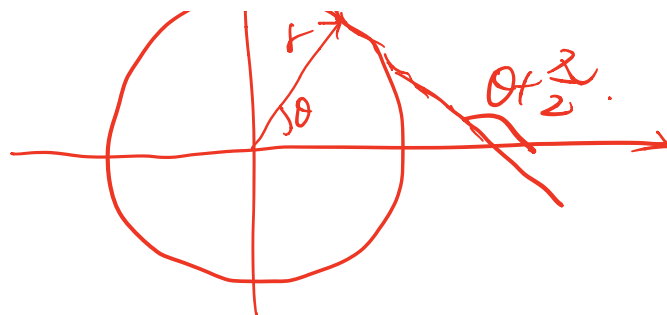
$$\frac{\partial u}{\partial \theta} = \left(\frac{\partial u}{\partial x}, \frac{\partial u}{\partial y} \right) \cdot (-\sin \theta, \cos \theta) = -\frac{\partial u}{\partial r}.$$

同理 2 式.

为 充 分



12.5.11



9. 见讲义.