

By Euler's formula:

$$e^{i\theta} = \cos(\theta) + i \sin(\theta)$$

$$e^{-i\theta} = \cos(\theta) - i \sin(\theta)$$

$$\therefore \sin(\theta) = \frac{e^{i\theta} - e^{-i\theta}}{2i}$$

$$\text{let } \sin(\theta) = x$$

$$2ix = e^{i\theta} - e^{-i\theta}$$

$$2ixe^{i\theta} = (e^{i\theta})^2 - 1$$

$$(e^{i\theta})^2 + (-2ix)e^{i\theta} - 1 = 0$$

$$e^{i\theta} = \frac{-(-2ix) \pm \sqrt{(-2ix)^2 - 4(-1)}}{2} = ix \pm \sqrt{1 - x^2}$$

$$i\theta = \ln(ix \pm \sqrt{1 - x^2})$$

$$\theta = -i \ln(ix \pm \sqrt{1 - x^2})$$

$$\therefore \arcsin(\theta) = -i \ln(i\theta \pm \sqrt{1 - \theta^2})$$