

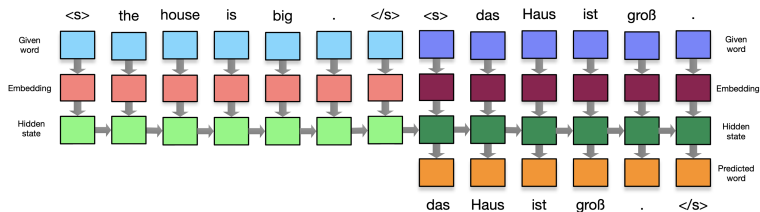
Attention is All You Need

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Recap: Encoder-Decoder Models



- ▶ **Encoders:** Give the source sentence meaning
- ▶ **Decoders:** Emit a variable-length sequence
- ▶ **Seq2Seq** models rely on propagating the hidden state for generation

How can we improve this model?

- ▶ Add an **alignment model** to force the model to 'attend' and 'read' different parts of the input
- ▶ Gives the decoder direct access to the encodings to make generations
- ▶ Known as a **context vector**

What are Context Vectors?

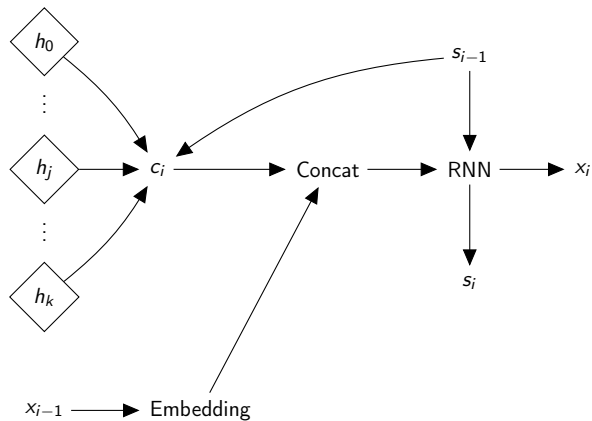
$$c_i = \sum_j \alpha_{ij} \cdot h_j$$

- ▶ A **context vector** c_i is the weighted sum of the encodings for the i -th iteration of the decoder
- ▶ s_{i-1} is the previous hidden state of the decoder
- ▶ h_j is the encoding for the j -th input word
- ▶ α_{ij} is the weight associated for the j -th input word for the i -th decoding iteration

How to use Context Vectors?

- ▶ No general rule
- ▶ Usually, **concat** the token embedding with context vector c_i
- ▶ Pass this as the input to the RNN, along with the previous decoder state s_{i-1} as the hidden state

Visual



(Simple) Attention Mechanisms

Mean Attention

$$\alpha_{ij} = \frac{1}{S}$$
$$c_i = \frac{1}{S} \sum_j^S h_j = \sum_j \alpha_{ij} \cdot h_j$$

- ▶ Very simple and naive approach is to apply uniform weights to each encoding h_j
- ▶ Fancy way of saying average
- ▶ S is the length of the source sentence

Location Based: Laplace

$$\alpha_{ij} = f(j \mid i, b) = \frac{1}{2b} \exp\left(-\frac{|j-i|}{b}\right)$$

$$c_i = \sum_j \alpha_{ij} \cdot h_j$$

- ▶ Weighted by location in sequence
 - ▶ Center a Laplace at $\mu = i$, scale b
 - ▶ Weight is the probability of position j relative to i
- ▶ Penalizes elements away from the diagonal
- ▶ Heavier tail than a Gaussian

Location Based: Gaussian

$$\alpha_{ij} = f(j \mid i, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(j-i)^2}{2\sigma^2}\right)$$

$$c_i = \sum_j \alpha_{ij} \cdot h_j$$

- ▶ Weighted by location in sequence
 - ▶ Center a Gaussian at $\mu = i$, scale σ
 - ▶ Weight is the probability of position j relative to i
- ▶ Smoother distribution closer to the diagonal
- ▶ Smaller tail than Laplace, so outliers are penalized more

Review: Laplace and Gaussian



Visualizing Location-Based Distributions

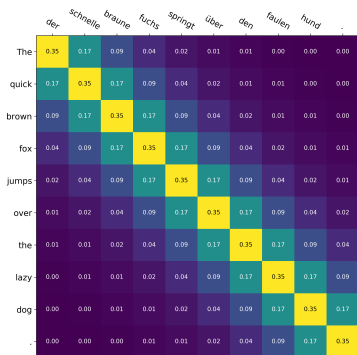


Figure: Laplace

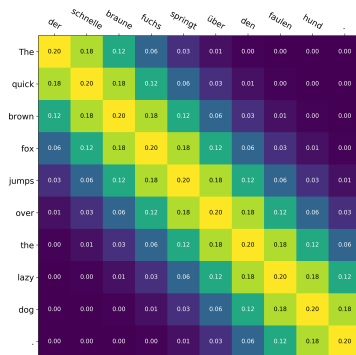


Figure: Gaussian

(Parameter-based) Attention Mechanisms

Parameter-based Attention

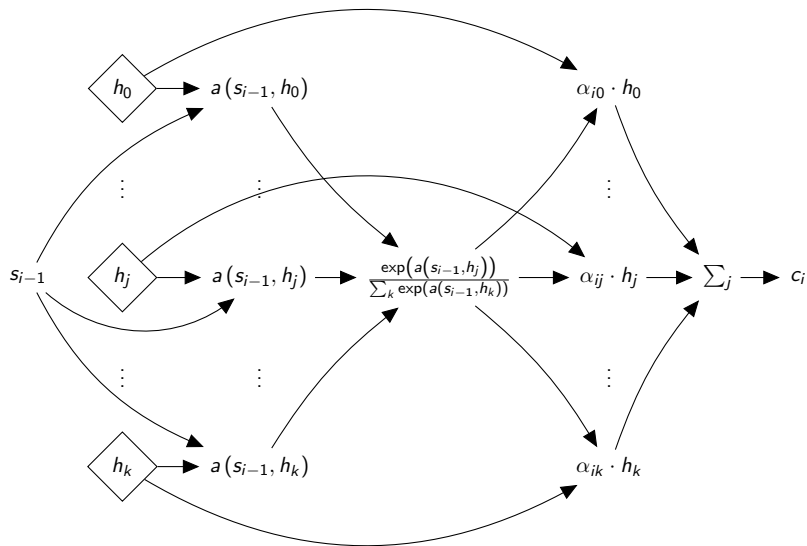
- ▶ Why not use learnable weights to effectively mix the encodings?
- ▶ Let deep learning figure out the alignment
- ▶ We now define a scoring function conditioned on the previous decoder state s_{i-1} and input encodings h_j

$$a(s_{i-1}, h_j) = ?$$

- ▶ In order to constrain the weights to a valid distribution, we softmax

$$\alpha_{ij} = \frac{\exp(a(s_{i-1}, h_j))}{\sum_k \exp(a(s_{i-1}, h_k))}$$
$$c_i = \sum_j \alpha_{ij} \cdot h_j$$

Attention Computation Graph

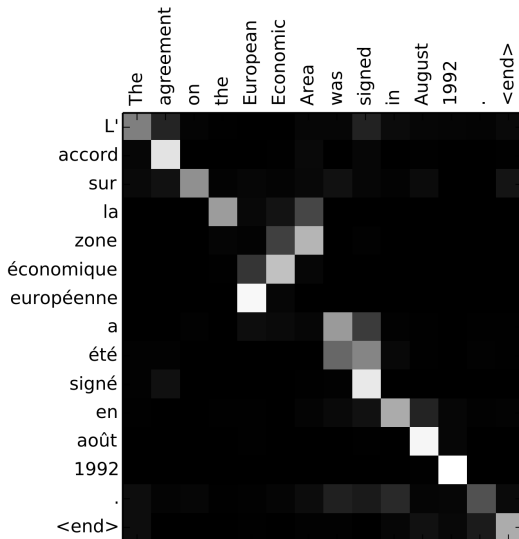


Bahdanau Attention

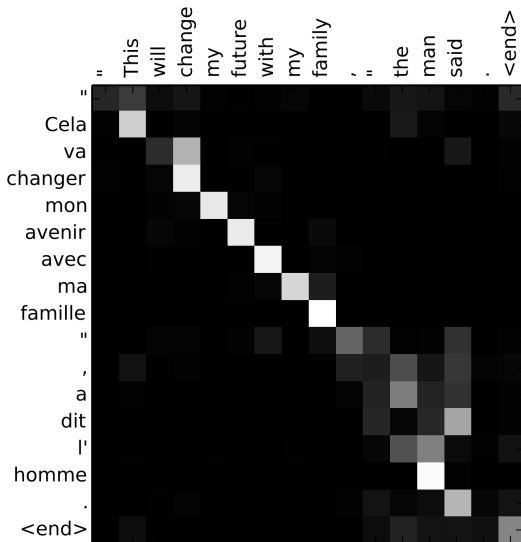
$$a(s_{i-1}, h_j) = v_a^T \tanh(W_a s_{i-1} + U_a h_j + b)$$

- ▶ W_a , U_a , are learnable matrices
- ▶ v_a , b are learnable vectors
- ▶ Output is a scalar value
- ▶ AKA: Additive Attention, Concat Attention

Bahdanau Attention Visual



Bahdanau Attention Visual



Luong Attention: Dot Product

$$a(s_{i-1}, h_j) = s_{i-1}^T h_j$$

- ▶ Notice: No Learnable Parameters
- ▶ Simple dot product between decoder state and encoding
- ▶ Output is a scalar value

Luong Attention: Scaled Dot Product

$$a(s_{i-1}, h_j) = \frac{1}{\sqrt{|h_j|}} s_{i-1}^T h_j$$

- ▶ Rescale the dot product according to the dimensionality of the vectors
- ▶ **Why?** Because for large dimensionality, the dot-product is large in magnitude, resulting in small gradients from the softmax
- ▶ Output is a scalar value

Luong Attention: General

$$a(s_{i-1}, h_j) = s_{i-1}^T W_a h_j$$

- ▶ Allow a learnable matrix W_a inbetween the states
- ▶ AKA a Bilinear Layer: $x_0^T A x_1$
- ▶ Output is a scalar value

Luong Attention: Location Attention

$$a(s_{i-1}, h_j) = W_a s_{i-1}$$

- ▶ An approach to reweight exclusively on the decoder state
- ▶ Single learnable matrix W_a
- ▶ Output is vector of fixed-length
- ▶ **Footnote:** For short sentences, only use the top part of the vector. For long sentences, ignore words near the end.
- ▶ **Note:** Implies that this only works for fixed-length sentences!

Luong Attention Visual

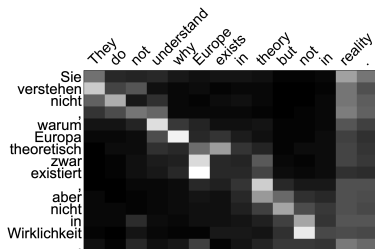


Figure: Luong Attention

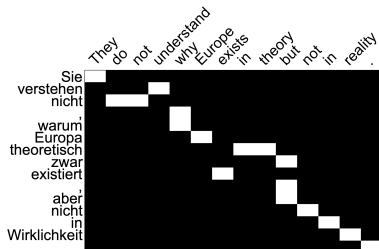


Figure: Gold Alignments

(Advanced) Attention Mechanisms

Luong Attention: Local Attention

- ▶ What if we focused on a window instead of all the vectors?
- ▶ This approach is known as *local* attention
- ▶ Before, we were using *global* attention

Luong Attention: Local Attention

- ▶ Define a window \mathcal{W} of size $2D$ at alignment point p_t :

$$\mathcal{W} = [p_t - D, p_t + D]$$

- ▶ Our context vector is now an average over this window

$$c_i = \sum_{j \in \mathcal{W}} \alpha_{ij} \cdot h_j$$

Luong Attention: Local Attention

- ▶ How do we select p_t , the alignment position?
- ▶ **Monotonic** alignment - set $p_t = t$
 - ▶ Assumes src and trg are roughly monotonically aligned
- ▶ **Predictive** alignment - predict the aligned position

Luong Attention: Local Predictive Attention

$$p_t = S \cdot \sigma \left(v_p^T \tanh(W_p \cdot s_{i-1}) \right)$$

- ▶ **Predictive** alignment allows for learnable positions
- ▶ S is the length of the source sentence
- ▶ W_p and v_p are learnable
- ▶ Sigmoid enforces the constraint $p_t \in [0, S]$

Luong Attention: Local Predictive Attention

$$a_p(s_{i-1}, h_j) = a(s_{i-1}, h_j) \cdot \exp\left(-\frac{(j - p_t)^2}{2\sigma^2}\right)$$

- ▶ Use a gaussian penalty to favor words near p_t
- ▶ Note: $p_t \in \mathbb{R}, j \in \mathbb{Z}$
- ▶ j is the *integer* position of the encoding within the window
- ▶ Empirically set $\sigma = \frac{D}{2}$
- ▶ $a(s_{i-1}, h_j)$ is any previous attention mechanism

Luong Attention Visuals

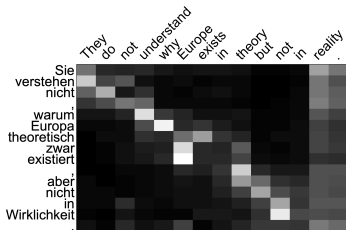


Figure: Global Attention

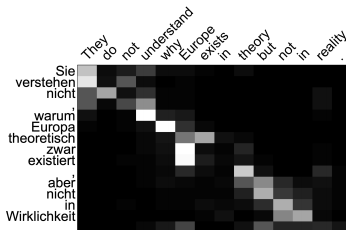


Figure: Local-M

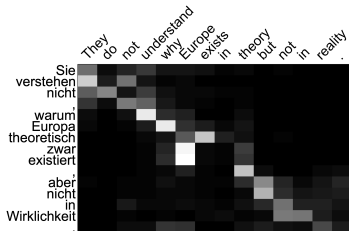


Figure: Local-P

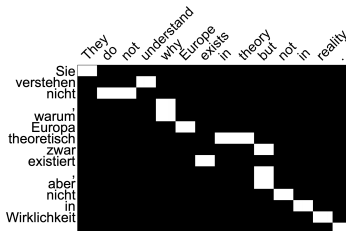


Figure: Gold Alignments

Fine-Grained Attention

$$a^k(s_{i-1}, h_j) = \text{FF}^k(s_{i-1}, h_j)$$

$$\alpha_{ij}^d = \frac{\exp(a^d(s_{i-1}, h_j))}{\sum_k \exp(a^d(s_{i-1}, h_k))}$$

$$c_i = \sum_j \alpha_{ij} \odot h_j$$

- ▶ What's different?
- ▶ Instead of a scalar scoring function, have it output a weight *per* dimension
- ▶ Now a weighted average on the feature dimension *instead* of the entire encoding

Fine-Grained Attention

$$c_i = 0.64 \cdot \begin{bmatrix} 0.17 \\ 0.53 \\ -0.22 \end{bmatrix} + 0.12 \cdot \begin{bmatrix} 1.34 \\ 0.39 \\ 0.45 \end{bmatrix} + 0.24 \cdot \begin{bmatrix} -0.08 \\ -1.39 \\ 1.21 \end{bmatrix}$$

$$c_i = \begin{bmatrix} 0.59 \\ 0.18 \\ 0.16 \end{bmatrix} \odot \begin{bmatrix} 0.17 \\ 0.53 \\ -0.22 \end{bmatrix} + \begin{bmatrix} 0.09 \\ 0.36 \\ 0.74 \end{bmatrix} \odot \begin{bmatrix} 1.34 \\ 0.39 \\ 0.45 \end{bmatrix} + \begin{bmatrix} 0.32 \\ 0.46 \\ 0.10 \end{bmatrix} \odot \begin{bmatrix} -0.08 \\ -1.39 \\ 1.21 \end{bmatrix}$$

Multi-Headed Attention

$$\alpha_{ij}^k = \frac{\exp(a^k(s_{i-1}, h_j))}{\sum_k \exp(a^k(s_{i-1}, h_k))}$$

- ▶ Why not have K attention weights?

$$c_i^k = \sum_j \alpha_{ij}^k \cdot h_j$$

$$c_i = \frac{1}{K} \sum_k c_i^k$$

- ▶ *Multi-Headed Attention* is just aggregating several attended representations of the encodings
- ▶ Fancy way of ensembling attention mechanisms

Multi-Headed Attention

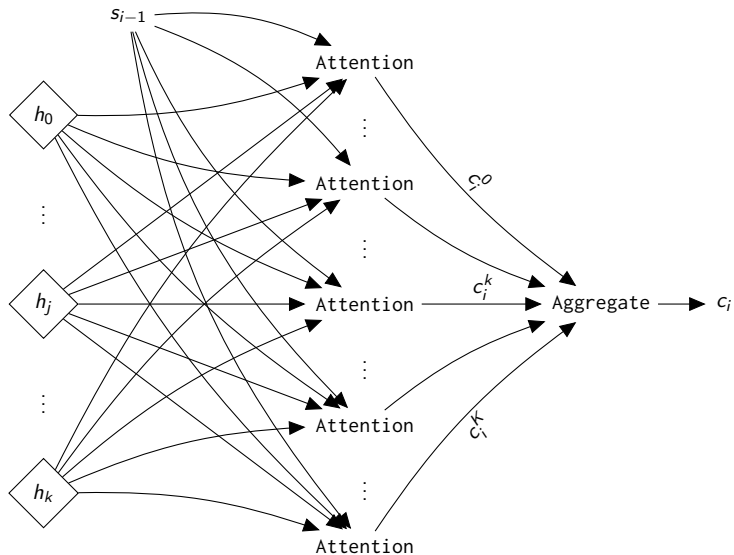
$$\alpha_{ij}^d = \frac{\exp(a^d(s_{i-1}, h_j))}{\sum_k \exp(a^d(s_{i-1}, h_k))}$$

$$c_i^k = \sum_j \alpha_{ij}^k \cdot h_j$$

$$c_i = \begin{bmatrix} c_i^0 \\ \vdots \\ c_i^k \\ \vdots \\ c_i^K \end{bmatrix} W_a$$

- ▶ **Alternative:** Concat each context vector and use a linear layer to reduce the dimensionality
- ▶ Weighted Average of K 'attended' context vectors!

Multi-Headed Attention



Self-Attention: Generalized

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right) V$$

- ▶ Query Q , Key K , and Value V
- ▶ d_k is the dimensionality of the query and keys
- ▶ **Note** that this implies that we can re-mix the encodings via linear layers before attending
- ▶ **Note** the similarity to Luong's Scaled Dot Attention

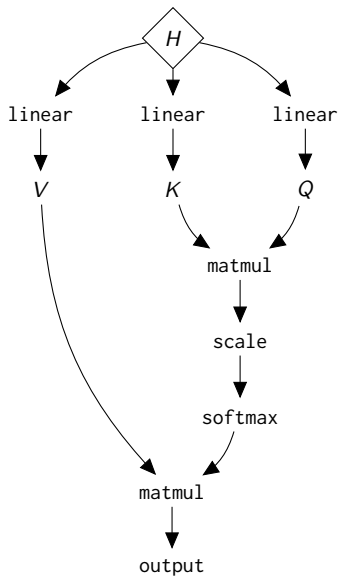
Self-Attention: What are Queries, Keys, and Values?

Self-Attention: Packing the Encodings

- ▶ To create Queries, Keys, and Values, we must pack the encodings
- ▶ Create a matrix $H \in \mathbb{R}^{S \times d}$
- ▶ S is sequence length, d is the dimensionality of the vectors

$$H = \begin{bmatrix} \leftarrow h_0 \rightarrow \\ \vdots \\ \leftarrow h_j \rightarrow \\ \vdots \\ \leftarrow h_k \rightarrow \end{bmatrix}$$

Self-Attention: Computation Graph



Practical Considerations

Masking

Which one to use?

- ▶ Trend seems to be moving towards **Transformers**
- ▶ AKA a series of Self-Attentions inside Multi-headed Attentions
- ▶ Ideally, experiment and go crazy

Mixing and Matching

- ▶ Remember! You can always mix and match!
- ▶ Different attention mechanisms under MHA
- ▶ Etc, etc

Tools, References, and Further Reading

Papers

- ▶ Bahdanau et al., Neural Machine Translation by Jointly Learning to Align and Translate
- ▶ Luong et al., Effective Approaches to Attention-based Neural Machine Translation
- ▶ Vaswani et al., Attention is All You Need
- ▶ Dyer et al., A Simple, Fast, and Effective Reparameterization of IBM Model 2