

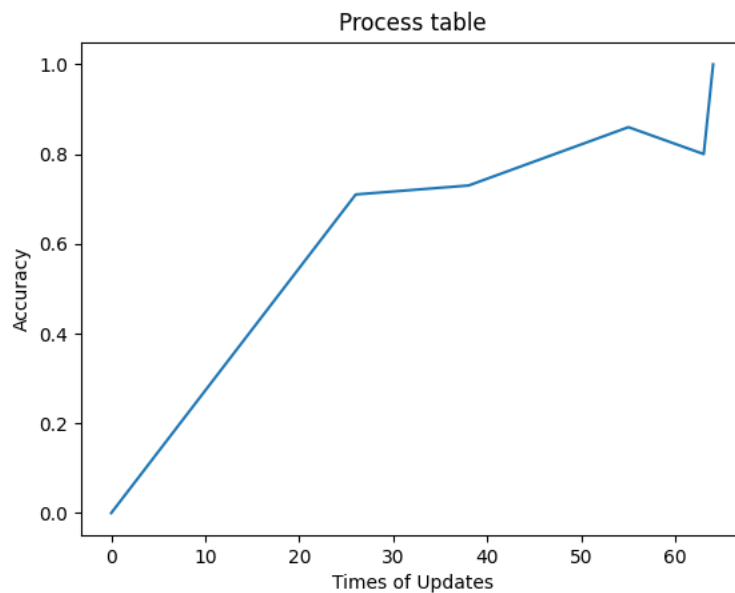
## Report

All definition for the terms are listed in README.txt, except for “delta”.

Definition of Delta: If the dataset is linear separable, there exists a positive real number, delta, such that for all data vectors,  
 $\text{true\_classification} \cdot \text{dot\_product}(\text{data\_vector}, \text{weights\_of\_linear\_separator})$  is greater than delta.

Therefore, I calculated every  $\text{delta}^2$ 's lower bond based on convergence theorem for dataset that is linear separable.

### 1. linearSmoke.dat:



```
cheng@chen-System-Product-Name:~/Desktop/csc246_Project1$ ls
data linearSmoke.dat perceptronProject.pdf perceptron_starter.py test.py
cheng@chen-System-Product-Name:~/Desktop/csc246_Project1$ python3 perceptron_starter.py --train_file data/linearSmoke.dat --iterations 2000

find it!
it uses 0.0014283670000001525sec

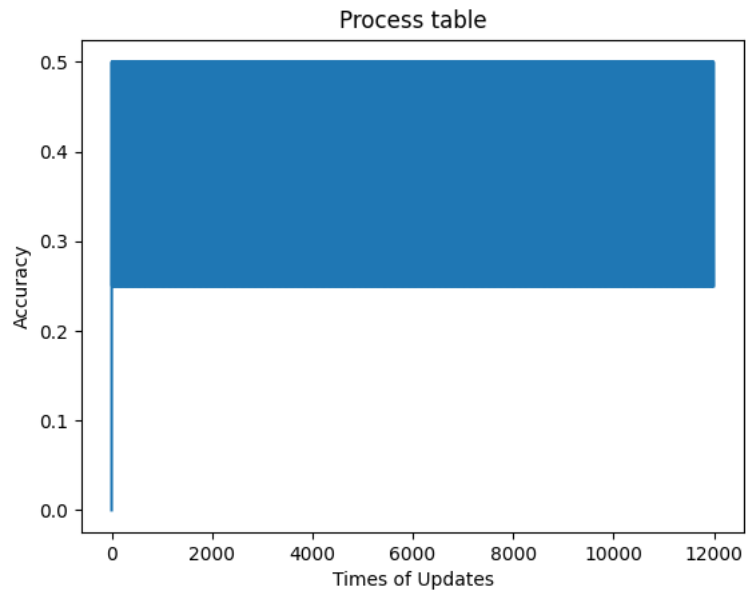
All data vectors are bounded by R= 1.746803700427691
it uses 64 steps(updates) and 5 iterations
Since it converges, we can calculate out  $\text{delta}^2 > 0.04767692449731054$ 

Final accuracy: 1.0
Max accuracy: 1.0

Feature weights (bias last): 4.536181279855713 2.5594303280244404 -5.426706309429592 -2.0
```

Base on the 2 pictures, the accuracy quickly converges to 100% after 60 updates for weights. Therefore, it is linear separable with  $\text{delta}^2 > 0.047$ .

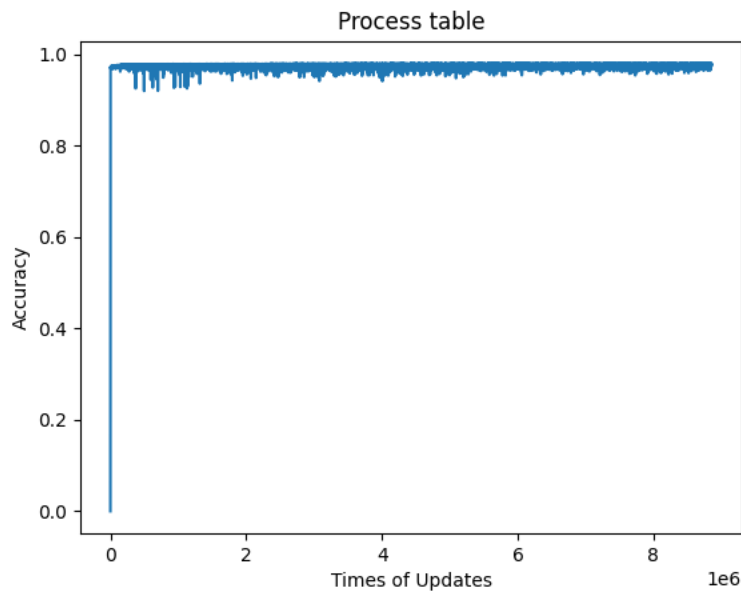
## 2. xorSmoke.dat:



```
chen@chen-System-Product-Name:~/Desktop/csc246_Project1$ python3 perceptron_starter.py --train_file data/xorSmoke.dat --iterations 2000
1000 iterations has been finished
Weights have been updated 10000 times
2000 iterations has been finished
cannot find it
it uses 0.046601212999999975sec
All data vectors are bounded by R= 1.7320508075688772
it uses 11998 steps(updates) and 2000 iterations
Final accuracy: 0.25
Max accuracy: 0.5
Feature weights (bias last): -2.0 -1.0 0.0
```

Based on 2 pics, the accuracy has no tendency to be increased beyond 50% even after 12000 updates. Thus, it is probably none-linear separable data set as expected

3.



```
cannot find it
it uses 649.399341626sec

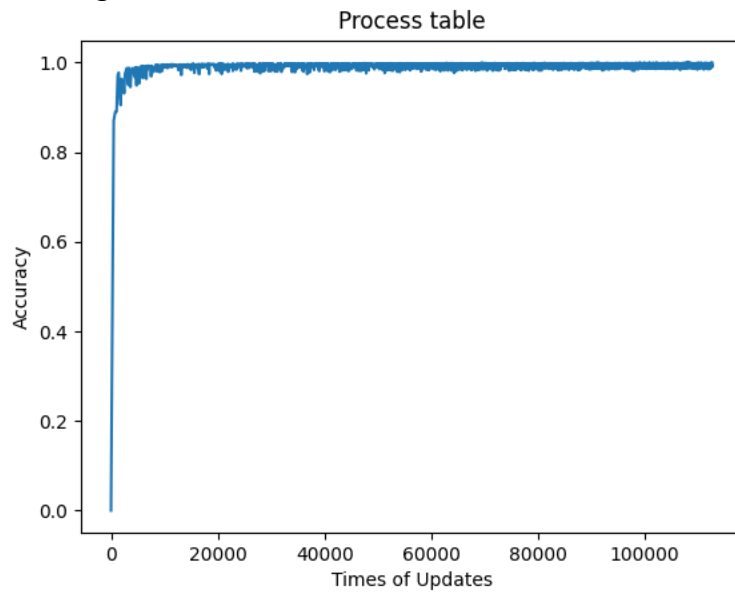
All data vectors are bounded by R= 1200.4052470355523
it uses 8855802 steps(updates) and 10000 iterations

Final accuracy: 0.9769247960665997
Max accuracy: 0.980556486758297

Feature weights (bias last): 24.296875 -196.90328743378763 29558.252531670325 -3040.0567505363647 -67.20152402196032 83.8743403739924 3988.5403605128367 -344.3561343077144 -33198.0
choudhury Custom Product Name: /Desktop/csc745-Project1$ python3 perceptron_starter.py --train_file data/challenge1.dat --iterations 10000
```

I used 10000 iterations to try to find the separator, but I could not find it. Based on the table, at the tail of the plot, it does not have an evident tendency to increase further. Since the max accuracy is 98.05%, it is probably not linear separable.

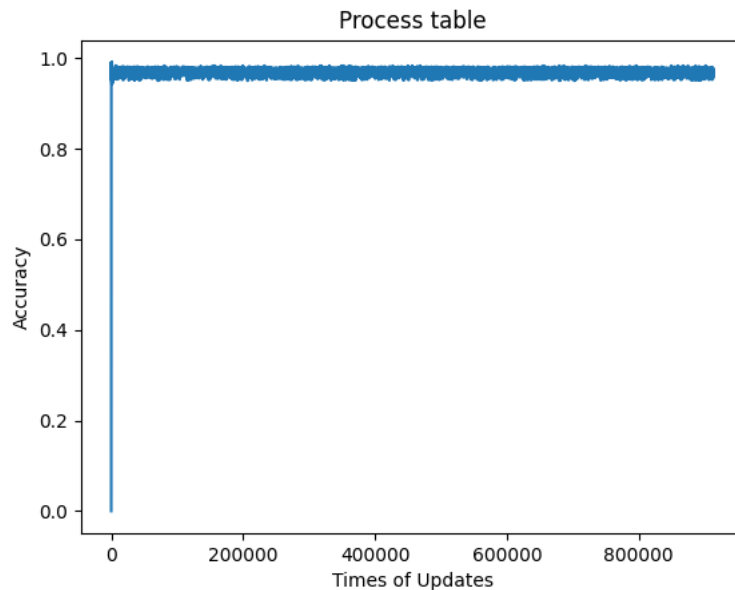
#### 4.challenge1.dat



```
find it!  
it uses 163.41351218600002sec  
  
All data vectors are bounded by  $\|x\| = 4.143379680902967$   
it uses 112599 steps(updates) and 4174 iterations  
Since it converges, we can calculate out  $\delta^2 > 0.00015246667537118072$   
  
Final accuracy: 1.0  
Max accuracy: 1.0  
  
Feature weights (bias last): -5.131662805078532 -228.56419114126376 43.362348421969436 -166.356740439428 -246.26849630493854 41.15137436917769 -72.33828212323539 171.83629895945413 -288.68588268794656 185.23478982951297 42.81688179388236 248.97477952884382 28.35045373222938  
3 69.0993463380872 -225.17233108389404 -46.85516023899328 -144.26189488159008 273.37069267189577 20.389012440166177 1.3344190626030936 -216.97007222560743 -50.752166675655985 191.3267958861096 -17.07012726894031 158.55817317318912 -130.9942662773926 191.9044262262456 -19.1  
56278171268453 -156.81558416832248 -14.896758922836326 59.0
```

Based on the information in the terminal, the linear separator is eventually found, after 112599 updates and 4174 iterations. The lower bound of  $\delta^2$  is 0.0001

## 5. challenge2.dat



```
cannot find it
it uses 1984.645919031sec

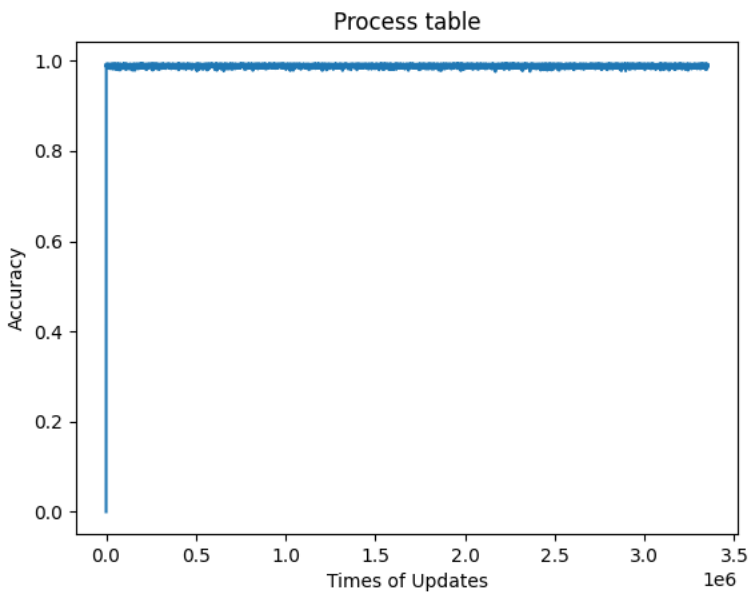
All data vectors are bounded by R= 4.12563955983977
it uses 3351864 steps(updates) and 50000 iterations

Final accuracy: 0.9915
Max accuracy: 0.994

Feature weights (bias last): -1.2293268303911562 -5.648483242634787 9.55172807517887 -7.951084724360641 -0.46934084722795333 0.41040846899411154 13.587411989576075 -6.379089614401729 1.1884858659413493 3.379789697575842 6.089789020767819 -10.089172585158282 14.6254084983765
97 -0.4950473362549459 0.42237831310590023 10.281631118142585 -0.6546382526972369 3.1936438330112287 13.456083885898488 14.186096769382816 4.188473854234272 -1.9952171262810743 -2.8867898985725876 -0.18561750866257775 -4.617178595318425 -4.069163893858266 -0.569442885799457
9 17.883427783585727 1.7282074194969343 1.7045588946648022 -2.0
```

I try to find the separator using 50000 iterations, but I could not find it even with 3351864 updates. As we can see, based on the table, all accuracy at the end is lower than 99.4%, since there is a peak at very beginning, and the max accuracy is recorded as 0.994. Thus, we can conclude that it does not have a tendency of increasing beyond even 0.994. Therefore, it is probably not a linear separable data set.

## 6.challenge3.dat



```
cannot find it
it uses 1984.645919831sec

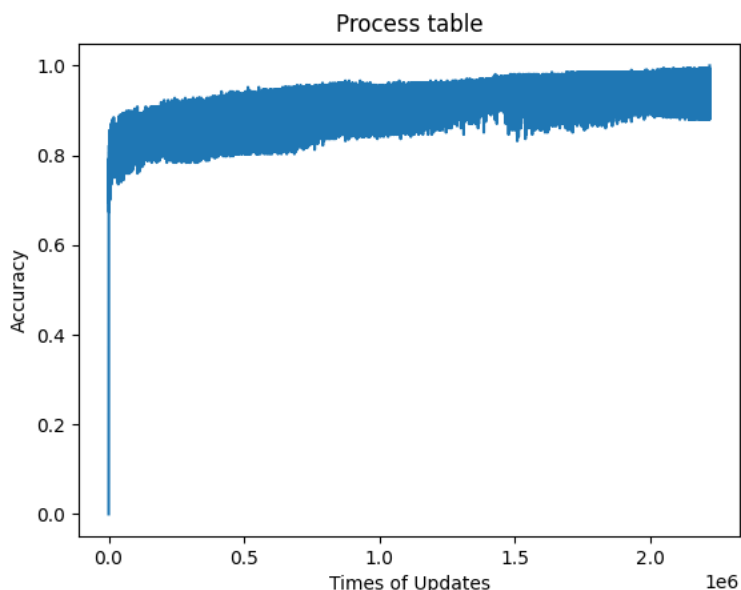
All data vectors are bounded by  $\|x\| = 4.12563955383977$ 
it uses 3351864 steps(updates) and 50000 iterations

Final accuracy: 0.9915
Max accuracy: 0.994

Feature weights (bias last): -1.2293268383911562 -5.646483242634787 9.55172807517887 -7.951004724368641 -0.46934004722795333 0.41048046899411154 13.587411989576875 -0.3798089614401729 1.1884858659413493 3.379789697573842 6.889789828767819 -10.889172585158282 14.6254684983765
97 -0.4958473362549459 0.42237831318598023 10.281631118142585 -0.6546382526972969 3.1936430338112287 13.456003805899488 14.186896769382816 4.188473854234272 -1.9952171262810743 -2.8867898985725076 -0.18561758806257775 -4.617178595318425 -4.869163893898266 -0.56944288799457
9 17.08342778385727 1.7282874194869343 1.7045568946648822 -2.0
```

Similar to challenge1, the accuracy is pretty stable between 0.99 and 1 exclusively. Thus, it does not have a tendency of being convergent to 1. Therefore, it is probably not a linear separable dataset.

## 7. challenge4.dat



```
find {t}
{t uses 533.447381649sec

All data vectors are bounded by R= 4.05347042421676
{t uses 2219731 steps(updates) and 132312 iterations
Since {t converges, we can calculate out delta^2 > 7.402078215783806e-06

Final accuracy: 1.0
Max accuracy: 1.0

Feature weights (bias last): -272.855380000088636 -98.82689999991695 687.84969999990961 -270.1176999977511 82.67138000061712 -126.39420000166005 194.65380000129971 198.42420000155908 -290.33500000142089 145.48189999959455 -123.833699999906347 -238.9679000001802 146.127800000645
2 -31.219899999528142 -120.864499999682795 163.722999999999433 118.81440000007026 -150.3934000004746 115.24319999963396 -244.80839999958557 289.8512000002951 -382.9783999994642 382.7757999998807 -291.8520000019583 132.8438999993118 38.228199999762876 -113.5895000004771 58.6701
80800348434 53.39829999978077 -270.51970000145707 351.75209999988064 -134.47660000208258 -88.322799999872333 174.51809999780265 -133.754299998306 17.440899999906472 165.5733999998199 -28.411700000214545 -158.75899999918118 285.57420000010107 -63.857000000168165 -74.9976999997
6334 -17.6709999991068 -69.64039999987698 86.3132000003237 -189.17779999902325 89.78269999988013 -379.6413000003976 -444.82509999630463 2096.528199994738 -811.2118000005743 -1346.0841000005807 -584.5802999971338 60.16300000010992 -245.59649999911372 841.54510000011638 498.
6365000047157 -538.8158000021949 -344.6101000035292 120.9595999999729 161.0
```

It used 2219731 steps and 132312 iterations to find the linear separator. The lower bound of  $\Delta^2$  is shown above.