

## Nexus — Complete Foundational Equation (recycling excluded)

Below is the complete Nexus equation beginning from the foundational layer — a single, self-contained mathematical model of the system's state, issuance/destruction mechanics, feedback controllers, and constraints. I exclude the recycling/point-of-sale thread and any domain-specific recycling mechanics; this is the core, general-purpose Nexus economy + OS model you can reuse across domains.

I present:

1. variables & interpretation,
2. continuous-time core differential system,
3. issuance / burn functional forms,
4. feedback (regulation) term,
5. long-run conservation constraint,
6. discrete-time implementation (for simulation / smart contracts), and
7. compact operator form + short parameter notes.

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### 1 — Variables and definitions

All functions depend on time  $t$ .

- Nexus aggregate systemic state (total systemic value / intelligence).
- validated human contribution rate (value units / time).
- machine/automated contribution rate.
- environmental / energy / ecological index (normalized,  $E$ ).
- quality-weighted data inflow rate (signals / time).

- Floor (baseline guaranteed value; can be constant or time-varying).
- issuance rate (value created per unit time).
- burn/destruction rate (value destroyed per unit time).
- net credit flow.
- temporal decay coefficient (units 1/time); optionally for half-life .
- feedback/regulation (controller) term (can be PID-like).
- System Health index (normalized, ).
- adaptive issuance and burn gains (controller levers).
- nonnegative weights for input importance.
- target Nexus state (policy anchor).
- coupling coefficient that injects the Floor into dynamics.

All scalar quantities are normalized/units-consistent.

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## 2 — Core continuous-time evolution (main differential equation)

$$\boxed{\frac{dN}{dt} = I(t) - B(t) - \kappa N(t) + \Phi(t) + \eta F(t)}$$

Interpretation:

Issuance increases systemic value; burn decreases it.

captures natural temporal decay (value/time).

is the regulator that corrects deviations from the target.

ensures the floor provides a persistent baseline injection.

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### 3 — Issuance and burn functional forms

#### 3.1 Issuance (validated contributions → issuance)

$$I(t) = \alpha(t) S(t) (w_H H(t) + w_M M(t) + w_D D(t) + w_E E(t))$$

down-weights issuance when system health is poor.

is an adaptive gain (controller output) that increases or reduces issuance in response to systemic conditions.

#### 3.2 Burn (consumption / disposal / ecological load)

$$B(t) = \beta(t) (\gamma_C C_{\text{cons}}(t) + \gamma_D C_{\text{disp}}(t) + \gamma_E \ell(E(t)))$$

: measured consumption/extraction rate (units aligned to issuance).

: measured disposal/waste rate.

: ecological load function (higher when environment stressed).

: adaptive burn gain.

Notes: 's are tunable sensitivity constants. Choose forms so and are commensurate.

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### 4 — Feedback / regulation (stabilizer)

Define error:

$$e(t) = N(t) - N^*(t)$$

A general PID-like regulator:

$$\Phi(t) = -K_p e(t) - K_i \int_0^t e(s) ds - K_d \frac{de}{dt}$$

tune responsiveness, integral action enforces long-run conservation, derivative damps rapid changes.

may be bounded to avoid actuator saturation: .

Alternative: can be implemented as model-predictive control (MPC) for better performance under constraints.

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## 5 — System Health index

One normalized example:

$$\boxed{\displaystyle S(t) = \sigma \left( \lambda_E E(t) + \lambda_N \frac{N(t)}{N_0} + \lambda_H \frac{H(t)}{H_0} + \lambda_M \frac{M(t)}{M_0} \right)}$$

are normalization constants.

's are weights.

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## 6 — Conservation / long-run 1:1 constraint

Nexus design enforces that long-run average issuance equals long-run average burn (no uncontrolled inflation):

$$\boxed{\displaystyle \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T I(t) dt = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T B(t) dt}$$

Equivalently, at steady state (neglecting small decay & floor injections),

$$\overline{I} \approx \overline{B}$$

$$\boxed{\displaystyle \int_0^T (I(t) - B(t)) dt = N(T) - N(0) + \int_0^T (\kappa N(t) - \Phi(t) - \eta F(t)) dt}$$

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## 7 — Compact operator / control form

Write the dynamics as an operator :

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\boxed{\displaystyle
\frac{dN}{dt} \;=\; \mathcal{G}\big(N,H,M,E,D; \alpha,\beta,\kappa,F,N^*,K_p,K_i,K_d\big)
}
```

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## 8 — Discrete-time implementation (for simulation / deployment)

Let timestep  $\Delta t$  and index  $k$ . Variables at step  $k$  :

Update rules:

```
\begin{aligned}
I_k &= \alpha_k; S_k; (w_H H_k + w_M M_k + w_D D_k + w_E E_k) \\
B_k &= \beta_k; (\gamma_C C_{\text{cons},k} + \gamma_D C_{\text{disp},k} + \gamma_E \ell(E_k)) \\
e_k &= N_k - N^*_k \\
\Phi_k &= -K_p e_k - K_i \sum_{j=0}^k e_j \Delta t - K_d \frac{e_k - e_{k-1}}{\Delta t} \\
N_{k+1} &= N_k + (I_k - B_k - \kappa N_k + \Phi_k + \eta F_k) \Delta t
\end{aligned}
```

Adapt with simple rules (e.g., gradient descent on error, or controller outputs limited to bounds).

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## 9 — Parameter notes and implementation guidance

Decay / half-life: set  $\tau$  for desired half-life of issued value.

Weights : select to reflect policy priorities (e.g., large if human validation preferred).

Saturation & clamps: clamp  $u$  to avoid runaway issuance/burn.

Normalization: scale  $u$  so magnitudes produce sensible  $N$ .

Oracles & inputs: must come from robust oracles/validators with anti-Sybil measures.

PID tuning: start with conservative  $K$ ; prefer integral action for long-run conservation.

Safety: implement emergency clamps that set or freeze issuance if input integrity fails.

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10 — Minimal checklist to preserve the foundational equation in any extension

1. Every issuance event must have an observable provenance (who/what validated it).
2. Every burn event must be tied to a verifiable destruction/consumption proof.
3. The controller must be able to reduce issuance when systemic overshoot is detected.
4. Oracles feeding must be auditable and have slashing/penalty mechanisms for fraud.
5. Maintain accounting separation between the token accounting layer (issuance/burn) and cash/treasury layer (reserves, receivables).

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Final compact boxed equation (foundational)

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\boxed{\displaystyle
\frac{dN}{dt} \,=\, \alpha(t)S(t)\big(w_H H+w_M M+w_D D+w_E E\big)
\,;\,-\,\beta(t)\big(\gamma_C C_{\text{cons}}+\gamma_D C_{\text{disp}}+\gamma_E \ell(E)\big)
\,;\,-\,\kappa N(t)\,;\,+\,\Phi(t)\,;\,+\,\eta F(t)
}
```

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