

$$\sqrt{x} = \sqrt{x} \Rightarrow (\sqrt{x} - \sqrt{x})^2 = 0$$

$$\text{Set } \sqrt{x} = y \text{ then } (y - \sqrt{x})^2 = 0 \Rightarrow y^2 - 2 \cdot \sqrt{x} \cdot y + x = 0$$

$$\Rightarrow \sqrt{x} = \frac{y^2 + x}{2y} \Rightarrow \sqrt{x} = \frac{(y + x/y)}{2}$$

$$\text{Consider now } \sqrt{x} = z \Rightarrow z = \frac{y + x/y}{2}$$

Since $z = y = \sqrt{x}$ we want to approximate the square root ~~error~~ with an appropriate amount of decimal points.

Let's say we want accuracy of 5 decimal points, then the difference $|y - z|$ should not exceed $10^{-5} = \underbrace{0.00001}_{\text{5 decimal points}}$.

To find the solution we iterate:

$$y = z$$

$$z = (y + x/y) / 2$$

until $|y - z| > 10^{-5}$ surpasses the desired accuracy.