Randomized Optimization: Simulated Annealing Algorithm

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```
In [1]: # import packages needed import numpy as np import pandas as pd import matplotlib.pyplot as plt
```

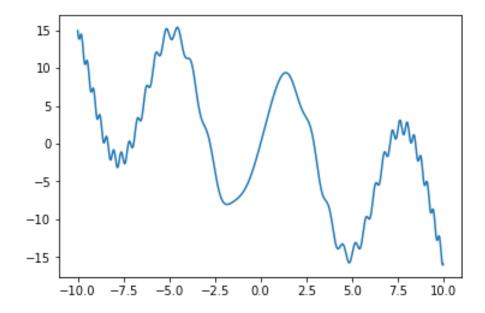
Overview

- The simulated annealing algorithm can be used to optimize a cost function given a search space. A cost function is a function that maps a search space to real values. This algorithm is useful for minimization or maximization problems. A use case for the algorithm includes finding the optimal solution to the travelling salesman problem, that is, finding the shortest distribution route.
- This stochastic algorithm start by randomly selecting a state in the search space, then takes a random walk to find the optimal value of the cost function. The algorithm is able to skip over local minima or maxima, which makes it more advantageous compared to other optimization algorithms that get stuck in local optima.
- Simulated annealing finds the optimal solution by starting off at a high 'temperature' and slowly cooling down until a solution is found, close to the crystal structure (optimal value of the cost function).
- This algorithm is inspired by the annealing technique used in metallurgy, in cooling hot metals until a stable crystal structure is obtained.

A Function with Local and Global Optima

```
In [2]: # create data with local and global optima
x_input = np.linspace(-10, 10, 1000)
def func(x):
    return np.sin((x)**2) + 10*np.sin(x) - x

y_output = func(x_input)
plt.plot(x_input, y_output)
plt.show()
```

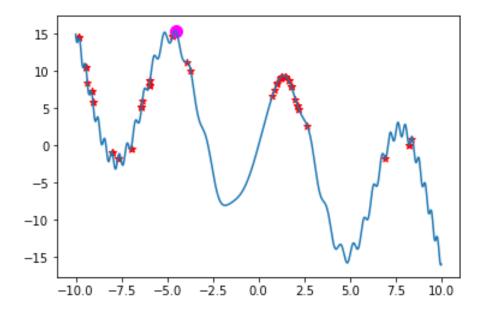


The Simulated Annealing Algorithm

```
▶ In [3]: # define the simulated annealing function
           def simulated annealing(search space, func, T=10, alpha=0.1):
               Returns the maximum value of the search space
               global search history
               global x best
               search history = []
               np.random.seed(0)
               x_current = np.random.choice(search_space)
               x best = x current
               while T > 0:
                    x next = np.random.choice(search space) # random walk
                   f_current = func(x_current)
                    f next = func(x next)
                    if f next > f current:
                       x current = x next
                        if func(x next) > func(x best):
                            x best = x next
                    elif np.exp((f_next - f_current)/T) > np.random.random():
                       x current = x next
                    T = T-alpha # reduce T
                    search history.append(x current)
                return x best, func(x best)
           simulated annealing(x input, func)
```

The Search History and the Maximum Point

```
# plot the search history and optimal point
history_output = func(np.array(search_history))
plt.scatter(search_history, history_output, marker="*", c="r")
plt.scatter(x_best, func(x_best), s=100, marker="o", c="magenta")
plt.plot(x_input, y_output)
plt.show()
```



The algorithm was able to find the maximum point (the magenta dot on the graph)

Resource

see pseudo code in https://www.lancaster.ac.uk/~varty/RTOne.pdf
(https://www.lancaster.ac.uk/~varty/RTOne.pdf)