Untitled

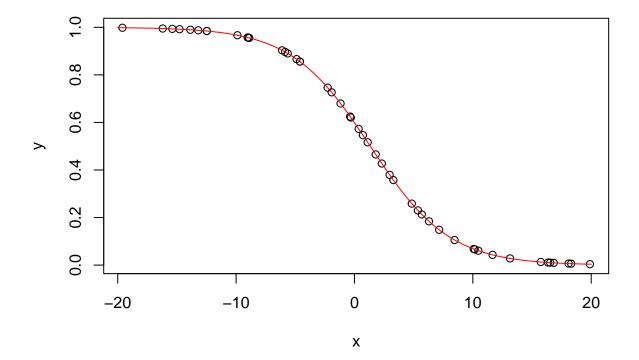
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2/5/2022

```
rm(list = ls())
library(rstanarm)
library(arm)
```

14.1:

```
x <- runif(n = 50, min = -20, max = 20)
y <- invlogit(0.4 - 0.3 * x)
plot(x, y)
curve(invlogit(0.4 - 0.3 * x), xlim = c(-20, 20), from = -20, to = 20, col = "red", add = T)</pre>
```



14.6:

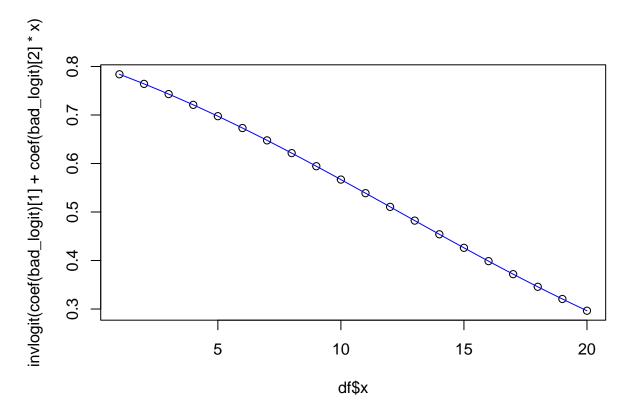
```
y \leftarrow sample(c(0,1), 20, replace = TRUE)
df <- data.frame(cbind(x,y))</pre>
bad_logit <- stan_glm(y ~ x, family = binomial(link = "logit"), data = df)</pre>
##
## SAMPLING FOR MODEL 'bernoulli' NOW (CHAIN 1).
## Chain 1:
## Chain 1: Gradient evaluation took 2.1e-05 seconds
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.21 seconds.
## Chain 1: Adjust your expectations accordingly!
## Chain 1:
## Chain 1:
## Chain 1: Iteration:
                        1 / 2000 [ 0%]
                                            (Warmup)
## Chain 1: Iteration: 200 / 2000 [ 10%]
                                            (Warmup)
## Chain 1: Iteration: 400 / 2000 [ 20%]
                                            (Warmup)
## Chain 1: Iteration: 600 / 2000 [ 30%]
                                            (Warmup)
## Chain 1: Iteration: 800 / 2000 [ 40%]
                                            (Warmup)
## Chain 1: Iteration: 1000 / 2000 [ 50%]
                                            (Warmup)
## Chain 1: Iteration: 1001 / 2000 [ 50%]
                                            (Sampling)
## Chain 1: Iteration: 1200 / 2000 [ 60%]
                                            (Sampling)
## Chain 1: Iteration: 1400 / 2000 [ 70%]
                                            (Sampling)
## Chain 1: Iteration: 1600 / 2000 [ 80%]
                                            (Sampling)
## Chain 1: Iteration: 1800 / 2000 [ 90%]
                                            (Sampling)
## Chain 1: Iteration: 2000 / 2000 [100%]
                                            (Sampling)
## Chain 1:
## Chain 1: Elapsed Time: 0.010361 seconds (Warm-up)
## Chain 1:
                           0.01096 seconds (Sampling)
## Chain 1:
                           0.021321 seconds (Total)
## Chain 1:
## SAMPLING FOR MODEL 'bernoulli', NOW (CHAIN 2).
## Chain 2:
## Chain 2: Gradient evaluation took 8e-06 seconds
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.08 seconds.
## Chain 2: Adjust your expectations accordingly!
## Chain 2:
## Chain 2:
## Chain 2: Iteration:
                        1 / 2000 [ 0%]
                                            (Warmup)
## Chain 2: Iteration: 200 / 2000 [ 10%]
                                            (Warmup)
## Chain 2: Iteration: 400 / 2000 [ 20%]
                                            (Warmup)
## Chain 2: Iteration:
                        600 / 2000 [ 30%]
                                            (Warmup)
## Chain 2: Iteration: 800 / 2000 [ 40%]
                                            (Warmup)
## Chain 2: Iteration: 1000 / 2000 [ 50%]
                                            (Warmup)
## Chain 2: Iteration: 1001 / 2000 [ 50%]
                                            (Sampling)
## Chain 2: Iteration: 1200 / 2000 [ 60%]
                                            (Sampling)
## Chain 2: Iteration: 1400 / 2000 [ 70%]
                                            (Sampling)
## Chain 2: Iteration: 1600 / 2000 [ 80%]
                                            (Sampling)
## Chain 2: Iteration: 1800 / 2000 [ 90%]
                                            (Sampling)
## Chain 2: Iteration: 2000 / 2000 [100%]
                                            (Sampling)
```

```
## Chain 2:
## Chain 2: Elapsed Time: 0.010311 seconds (Warm-up)
## Chain 2:
                           0.01214 seconds (Sampling)
## Chain 2:
                           0.022451 seconds (Total)
## Chain 2:
##
## SAMPLING FOR MODEL 'bernoulli', NOW (CHAIN 3).
## Chain 3:
## Chain 3: Gradient evaluation took 3e-06 seconds
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.03 seconds.
## Chain 3: Adjust your expectations accordingly!
## Chain 3:
## Chain 3:
## Chain 3: Iteration:
                          1 / 2000 [ 0%]
                                            (Warmup)
## Chain 3: Iteration: 200 / 2000 [ 10%]
                                            (Warmup)
                        400 / 2000 [ 20%]
## Chain 3: Iteration:
                                            (Warmup)
## Chain 3: Iteration: 600 / 2000 [ 30%]
                                            (Warmup)
## Chain 3: Iteration: 800 / 2000 [ 40%]
                                            (Warmup)
## Chain 3: Iteration: 1000 / 2000 [ 50%]
                                            (Warmup)
## Chain 3: Iteration: 1001 / 2000 [ 50%]
                                            (Sampling)
## Chain 3: Iteration: 1200 / 2000 [ 60%]
                                            (Sampling)
## Chain 3: Iteration: 1400 / 2000 [ 70%]
                                            (Sampling)
## Chain 3: Iteration: 1600 / 2000 [ 80%]
                                            (Sampling)
## Chain 3: Iteration: 1800 / 2000 [ 90%]
                                            (Sampling)
## Chain 3: Iteration: 2000 / 2000 [100%]
                                            (Sampling)
## Chain 3:
## Chain 3: Elapsed Time: 0.009912 seconds (Warm-up)
## Chain 3:
                           0.011224 seconds (Sampling)
## Chain 3:
                           0.021136 seconds (Total)
## Chain 3:
##
## SAMPLING FOR MODEL 'bernoulli' NOW (CHAIN 4).
## Chain 4:
## Chain 4: Gradient evaluation took 4e-06 seconds
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.04 seconds.
## Chain 4: Adjust your expectations accordingly!
## Chain 4:
## Chain 4:
## Chain 4: Iteration:
                          1 / 2000 [ 0%]
                                            (Warmup)
## Chain 4: Iteration: 200 / 2000 [ 10%]
                                            (Warmup)
                                            (Warmup)
## Chain 4: Iteration: 400 / 2000 [ 20%]
## Chain 4: Iteration: 600 / 2000 [ 30%]
                                            (Warmup)
## Chain 4: Iteration: 800 / 2000 [ 40%]
                                            (Warmup)
## Chain 4: Iteration: 1000 / 2000 [ 50%]
                                            (Warmup)
## Chain 4: Iteration: 1001 / 2000 [ 50%]
                                            (Sampling)
## Chain 4: Iteration: 1200 / 2000 [ 60%]
                                            (Sampling)
## Chain 4: Iteration: 1400 / 2000 [ 70%]
                                            (Sampling)
## Chain 4: Iteration: 1600 / 2000 [ 80%]
                                            (Sampling)
## Chain 4: Iteration: 1800 / 2000 [ 90%]
                                            (Sampling)
## Chain 4: Iteration: 2000 / 2000 [100%]
                                            (Sampling)
## Chain 4:
## Chain 4: Elapsed Time: 0.011103 seconds (Warm-up)
## Chain 4:
                           0.010776 seconds (Sampling)
## Chain 4:
                           0.021879 seconds (Total)
```

Chain 4:

```
print(bad_logit)
```

```
## stan_glm
                  binomial [logit]
##
    family:
   formula:
##
                  y ~ x
    observations: 20
##
    predictors:
                  2
##
               Median MAD_SD
##
##
   (Intercept)
                1.4
                       1.0
               -0.1
                       0.1
##
  Х
##
##
## * For help interpreting the printed output see ?print.stanreg
## * For info on the priors used see ?prior_summary.stanreg
#graph the
plot(df$x, invlogit(coef(bad_logit)[1] + coef(bad_logit)[2]*x))
curve(invlogit(coef(bad_logit)[1] + coef(bad_logit)[2]*x), add=TRUE, col = "blue")
```



I randomly sampled from a vector containing values of 0/1, so there was approximately a 50% chance of a given x's value being 0 or 1. As you can see from the graph, the curve does not move with the data, because I designed the y values to have no relationship with the predictors, and to just be generated randomly.