Biological Modeling of Neural Networks

(PAL

Week 2 – Biophysical modeling: The Hodgkin-Huxley model

Wulfram Gerstner EPFL, Lausanne, Switzerland

Reading for week 2: NEURONAL DYNAMICS - Ch. 2 (without 2.3.2 - 2.3.5)



2.1 Biophysics of neurons

- Overview
 2.2 Reversal potential
 Nernst equation
- 2.3 Hodgin-Huxley Model
- 2.4 Threshold in the Hodgkin-Huxley Model - where is the firing threshold?
- 2.5. **Detailed biophysical models** the zoo of ion channels

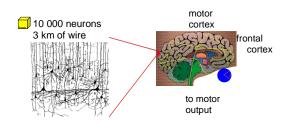
Review of week 1: Neurons and synapses

motor cortex

visual cortex

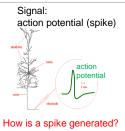
to motor output

Review of week 1: Neurons and synapses

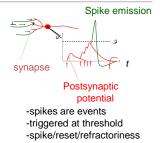


Review of week 1: Neurons and synapses





Review of week 1: Integrate-and-Fire models



Neuronal Dynamics – week 2: Biophysics of neurons

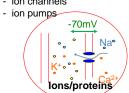
Nour viiui Dyllulliivo	MOUN 2. Diophlyolog of floations
Cell surrounded by me	embrane
Membrane contains	Signal:
 ion channels 	action potential (spike)
 ion pumps 	_ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
-70mV	dentries
/ 。。 🙆	Na+ action
	potential
\ K+•°*	
lons/prote	Ca ²⁺ /
10110/p1010	

Neuronal Dynamics – week 2: Biop	hvsics of neurons

Cell	surro	unded	by	membrane
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Membrane contains

- ion channels



Resting potential -70mV → how does it arise?

lons flow through channel → in which direction?

Neuron emits action potentials → why?

Neuronal Dynamics - 2. 1. Biophysics of neurons

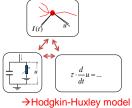
Resting potential -70mV → how does it arise?

Ions flow through channel → in which direction?

Neuron emits action potentials → why?

> → Hodgkin-Huxley model Hodgkin&Huxley (1952) Nobel Prize 1963

Neuronal Dynamics - 2. 1. Biophysics of neurons



Hodgkin&Huxley (1952) Nobel Prize 1963

Week 2 - Quiz

In a natural situation, the electrical potential inside a neuron is [] the same as outside [] is different by 50-100 microvolt [] is different by 50-100 millivolt	Neurons and cells [] Neurons are special cells because they are surrounded by a membrane [] Neurons are just like other cells surrounded by a membrane [] Neurons are not cells
lon channels are [] located in the cell membrane [] special proteins [] can switch from open to closed	If a channel is open, ions can If flow from the surround into the cell If flow from inside the cell into the surrounding liquid Multiple answers possible!

Week 2 - part 2: Reversal potential and Nernst equation

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Biological Modeling of Neural Networks

Week 2 – Biophysical modeling: The Hodgkin-Huxley model

Wulfram Gerstner EPFL, Lausanne, Switzerland 2.1 Biophysics of neurons

- Overview

2.2 Reversal potential
- Nernst equation

2.3 Hodgin-Huxley Model

2.4 Threshold in the Hodgkin-Huxley Model

- where is the firing threshold?
2.5. **Detailed biophysical models**

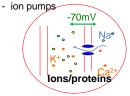
2.5. Detailed biophysical model
 the zoo of ion channels

Neuronal Dynamics – 2.2. Resting potential

Cell surrounded by membrane

Membrane contains

- ion channels



Resting potential -70mV → how does it arise?

lons flow through channel → in which direction?

Neuron emits action potentials → why?

Neuronal Dynamics - 2. 2. Resting potential

Resting potential -70mV

→ how does it arise?

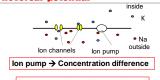
lons flow through channel

→ in which direction?

Neuron emits action potentials → why? → Hodgkin-Huxley model Hodgkin&Huxley (1952) Nobel Prize 1963

Neuronal Dynamics – <mark>2. 2.</mark>	Nernst equation
n ₁ (inside)	$\Delta u = u_1 - u_2 = \frac{-kT}{q} \ln \frac{n(u_1)}{n(u_2)}$
	Reversal potential
Concentration	difference ⇔ voltage difference

Neuronal Dynamics - 2.2. Reversal potential



Concentration difference ⇔ voltage difference

Reversal potential

Nernst equation

Week 2 - part 3: Hodgkin-Huxley Model

Neuronal Dynamics: Computational Neuroscience of Single Neurons

Week 2 - Biophysical modeling: The Hodgkin-Huxley model

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2.1 Biophysics of neurons

- Overview

2.2 Reversal potential

- Nernst equation

2.3 Hodgkin-Huxley Model

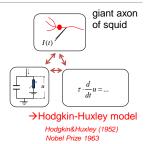
2.4 Threshold in the

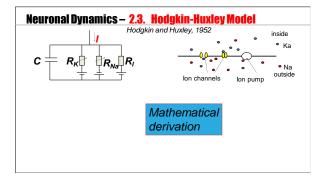
Hodgkin-Huxley Model - where is the firing threshold?

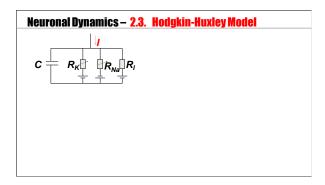
2.5. Detailed biophysical models

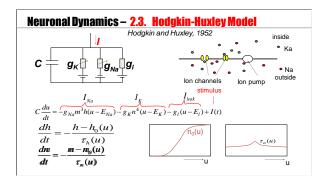
- the zoo of ion channels

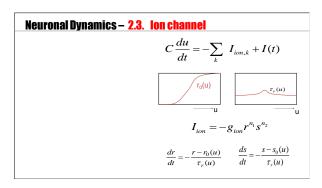
Neuronal Dynamics – 2. 3. Hodgkin-Huxley Model

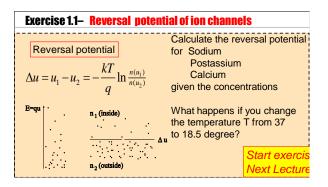


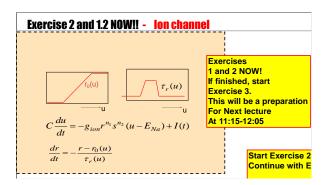












Week 2 - part 4: Threshold in the Hodgkin-Huxley Model

Biological Modeling of Neural Networks

Week 2 - Biophysical modeling: The Hodgkin-Huxley model

Wulfram Gerstner EPFL, Lausanne, Switzerland √ 2.1 Biophysics of neurons

- Overview

2.2 Reversal potential - Nernst equation

√ 2.3 Hodgin-Huxley Model

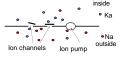
2.4 Threshold in the

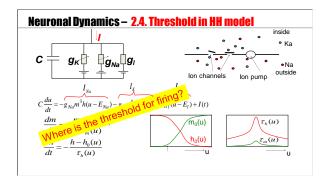
Hodgkin-Huxley Model - where is the firing threshold?

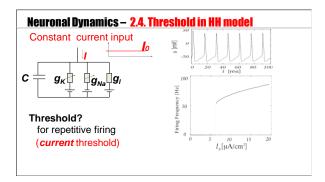
2.5. Detailed biophysical models

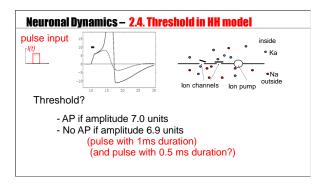
- the zoo of ion channels

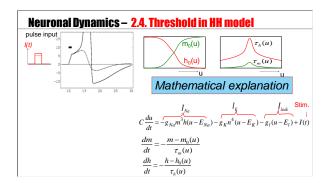
Neuronal Dynamics - 2.4. Threshold in HH model

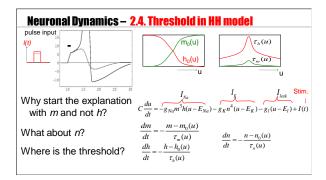


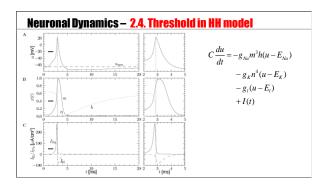












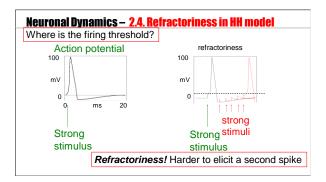
Neuronal	Dynamics –	2 / Three	hold in	Ahom HH
NGULVIIAI	- DVIIAIIIIUS	Z.4. I III GƏ	HVIU III	IIII IIIVUG

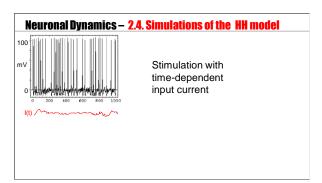
First conclusion:

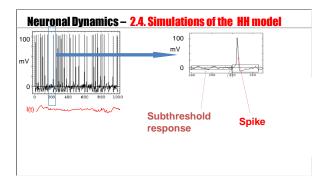
There is no strict threshold:

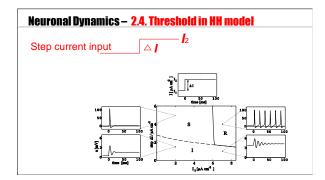
Coupled differential equations

'Effective' threshold in simulations?

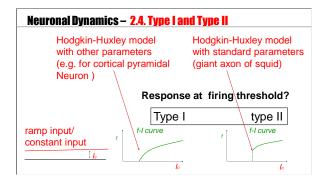








Neuronal Dynamics – 2.4. Threshold in HH model		
Where is the firing threshold?		
pulse input	There is no threshold - no current threshold - no voltage threshold	
step input^	'effective' threshold - depends on typical input	
ramp input	$C\frac{du}{dt} = -g_{Na}m^3h(u - E_{Na}) - \dots$	



Neuronal Dynamics – 2.4. Hodgkin-Huxley model

- -4 differential equations
- -no explicit threshold
- -effective threshold depends on stimulus
- -BUT: voltage threshold good approximation

Giant axon of the squid

- → cortical neurons
- -Change of parameters
- -More ion channels
- -Same framework

Exercise 3.1-3.3 – Hodgkin-Huxley – ion channel dynamics voltage step u_2 Determine ion channel dynamics $c \frac{du}{dt} = -g_K n^4 (u - E_K) + I(t)$ apply voltage step Start Exercise 3 at 11:33 Next Lecture at: 11.48 Adapted from Hodgkin-Huxley 1952

Week 2 - part 5: Detailed Biophysical Models

EPAL

Biological Modeling of Neural Networks

Week 2 – Biophysical modeling: The Hodgkin-Huxley model

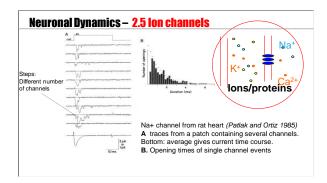
Provides flexible framework

Wulfram Gerstner EPFL, Lausanne, Switzerland

- √ 2.1 Biophysics of neurons
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- 2.5. Detailed biophysical models
 the zoo of ion channels

Neuronal Dynamics – 2.5 Biophysical models There are about 200 identified ion channels http://channelpedia.epfl.ch/ Hodgkin-Huxley model

Individual ion channels can be measured. Opening and closing is stochastic



Neuronal Dynamics – 2.5 Biophysical models			
Hodgkin-Huxley: -Cambridge lab -Plymouth lab	Ion channels Ion pump outside		
	Hodgkin-Huxley model provides flexible framework		
	Hodgkin&Huxley (1952) Nobel Prize 1963		

Exercise 4 – Hodgkin-Huxley model – gating dynamics		
A) Often the gating dynamics is formulated as		
$\frac{dm}{dt} = \alpha_m(u)(1-m) - \beta_m(u)m \qquad \qquad \frac{dm}{dt} = -\frac{m - m_0(u)}{\tau_m(u)}$		
Calculate $m_0(u)$ and $\tau_m(u)$		
B) Assume a form $\alpha_m(u) = \beta_m(u) = \frac{1}{1 - \exp[-(u+a)/b]}$		
How are a and b related to γ and θ in the equations		
$\frac{dm}{dt} = -\frac{m - m_0(u)}{c}$		
$dt \tau_m(u)$ $m_0(u) = 0.5\{1 + \tanh[\gamma(u - \theta)]$		
C) What is the time constant $\tau_m(u)$?		

Week 2 – References and Suggested Reading	
Reading: W. Gerstner, W.M. Kistler, R. Naud and L. Paninski, Neuronal Dynamics: from single neurons to networks and models of cognition. Chapter 2: The Hodgkin-Huxley Model, Cambridge Univ. Press, 2014	
- Hodgkin, A. L. and Huxley, A. F. (1952). A quantitative description of membrane current and its application to conduction and excitation in nerve. J Physiol, 117(4):500-544.	
-Ranjan, R., et al. (2011). Channelpedia: an integrative and interactive database for ion channels. Front Neuroinform, 5:36. -Toledo-Rodriguez, M., Blumenfeld, B., Wu, C., Luo, J., Attali, B., Goodman, P., and Markram, H. (2004). Correlation maps allow neuronal electrical properties to be predicted	
from single-cell gene expression profiles in rat neocortex. Cerebral Cortex, 14:1310-1327. - Yamada, W. M., Koch, C., and Adams, P. R. (1989). Multiple channels and calcium dynamics. In Koch, C. and Segev, I., editors, Methods in neuronal modeling, MIT Press.	
 - Aracri, P., et al. (2006). Layer-specic properties of the persistent sodium current in sensorimotor cortex. Journal of Neurophysiol., 95(6):3460-3468. 	
New Computer Foundation	
Now Computer Exercises:	
Play with Hodgkin-Huxley model	
The End	
THE EHU	