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Task 2:

(a) Write truth tables for $(\sim pVq)\Lambda q$ and $(\sim p\Lambda q)Vq$. What do you notice? Based on this result, we hypothesise that we can interchange V and Λ in a statement without affecting the truth table.

p	q	~ p	~ p V q	(~ p ∨ q) ∧ q
T	T	F	T	T
T	F	F	F	F
F	F	T	T	F
F	T	T	T	T

p	q	~ p	~ p ∧ q	(~ p ∧ q) ∨ q
T	T	F	F	T
T	F	F	F	F
F	F	T	F	F
F	T	T	T	T

- → Both statements have the same truth values in every row of their respective truth tables.
- (b) Write truth tables for $(\sim p \lor q) \land p$ and $(\sim p \land q) \lor p$. What do you think of the hypothesis now?

p	q	~ p	~ p V q	(~ p ∨ q) ∧ p
T	T	F	T	T
T	F	F	F	F
F	F	T	T	F
F	T	T	T	F

p	q	~ p	~ p ∧ q	(~ p ∧ q) ∨ p
T	T	F	F	T
T	F	F	F	T
F	F	T	F	F
F	T	T	T	T

- → The truth tables for the two statements are different.
- → The hypothesis that we can interchange V and ∧ in a statement without affecting the truth table does not hold true for these specific statements.