# R. Notebook

```
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 3.4.2
## -- Attaching packages -------
## v ggplot2 3.1.0
                     v purrr
                              0.2.5
## v tibble 2.0.1
                     v dplyr
                              0.7.8
## v tidyr
            0.8.0
                     v stringr 1.3.1
## v readr
            1.1.1
                     v forcats 0.3.0
## Warning: package 'ggplot2' was built under R version 3.4.4
## Warning: package 'tibble' was built under R version 3.4.4
## Warning: package 'tidyr' was built under R version 3.4.3
## Warning: package 'purrr' was built under R version 3.4.4
## Warning: package 'dplyr' was built under R version 3.4.4
## Warning: package 'forcats' was built under R version 3.4.3
## -- Conflicts ------
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
library(knitr)
## Warning: package 'knitr' was built under R version 3.4.3
library(caret)
## Warning: package 'caret' was built under R version 3.4.4
## Loading required package: lattice
## Warning in as.POSIXlt.POSIXct(Sys.time()): unknown timezone 'zone/tz/2018i.
## 1.0/zoneinfo/America/Chicago'
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
```

Market segmentation is a strategy that divides a broad target market of customers into smaller, more similar groups, and then designs a marketing strategy specifically for each group. Clustering is a common technique for market segmentation since it automatically finds similar groups given a data set.

In this problem, we'll see how clustering can be used to find similar groups of customers who belong to an airline's frequent flyer program. The airline is trying to learn more about its customers so that it can target different customer segments with different types of mileage offers.

The file Airlines Cluster.csv contains information on 3,999 members of the frequent flyer program. This data comes from the textbook "Data Mining for Business Intelligence," by Galit Shmueli, Nitin R. Patel, and Peter C. Bruce. For more information, see the website for the book.

There are seven different variables in the dataset, described below:

**Balance** = number of miles eligible for award travel

QualMiles = number of miles qualifying for TopFlight status

BonusMiles = number of miles earned from non-flight bonus transactions in the past 12 months

BonusTrans = number of non-flight bonus transactions in the past 12 months

FlightMiles = number of flight miles in the past 12 months

FlightTrans = number of flight transactions in the past 12 months

**DaysSinceEnroll** = number of days since enrolled in the frequent flyer program

#### 1.1) Normalizing the Data

Read the dataset AirlinesCluster.csv into R and call it "airlines".

Looking at the summary of airlines, which TWO variables have (on average) the smallest values?

Which TWO variables have (on average) the largest values?

```
airlines = read.csv('AirlinesCluster.csv')
summary(airlines)
```

##	Balance	QualMiles	BonusMiles	BonusTrans
##	Min. : 0	Min. : 0.0	$\mathtt{Min.}$ : 0	Min. : 0.0
##	1st Qu.: 18528	1st Qu.: 0.0	1st Qu.: 1250	1st Qu.: 3.0
##	Median : 43097	Median: 0.0	Median: 7171	Median :12.0
##	Mean : 73601	Mean : 144.1	Mean : 17145	Mean :11.6
##	3rd Qu.: 92404	3rd Qu.: 0.0	3rd Qu.: 23800	3rd Qu.:17.0
##	Max. :1704838	Max. :11148.0	Max. :263685	Max. :86.0
##	FlightMiles	FlightTrans	DaysSinceEnroll	
##	Min. : 0.0	Min. : 0.000	Min. : 2	
##	1st Qu.: 0.0	1st Qu.: 0.000	1st Qu.:2330	
##	Median: 0.0	Median : 0.000	Median:4096	
##	Mean : 460.1	Mean : 1.374	Mean :4119	
##	3rd Qu.: 311.0	3rd Qu.: 1.000	3rd Qu.:5790	
##	Max. :30817.0	Max. :53.000	Max. :8296	

#### Explanation

You can read in the data and look at the summary with the following commands:

```
airlines = read.csv("AirlinesCluster.csv")
```

summary(airlines)

For the smallest values, BonusTrans and FlightTrans are on the scale of tens, whereas all other variables have values in the thousands.

For the largest values, Balance and BonusMiles have average values in the tens of thousands.

### 1.2) Normalizing the Data

In this problem, we will normalize our data before we run the clustering algorithms. Why is it important to normalize the data before clustering?

```
include_graphics('1.2.png')
```

- If we don't normalize the data, the clustering algorith
- O If we don't normalize the data, it will be hard to inter
- If we don't normalize the data, the clustering will be
- If we don't normalize the data, the clustering will be

## 1.3) Normalizing the Data

Let's go ahead and normalize our data. You can normalize the variables in a data frame by using the preProcess function in the "caret" package. You should already have this package installed from Week 4, but if not, go ahead and install it with install.packages("caret"). Then load the package with library(caret).

Now, create a normalized data frame called "airlinesNorm" by running the following commands:

```
pre_proc = preProcess(airlines)
airlines_norm = predict(pre_proc, airlines)
summary(airlines_norm)
```

```
##
       Balance
                         QualMiles
                                            BonusMiles
                                                               BonusTrans
##
    Min.
           :-0.7303
                              :-0.1863
                                                 :-0.7099
                                                                    :-1.20805
                       Min.
                                         Min.
                                                             Min.
    1st Qu.:-0.5465
                       1st Qu.:-0.1863
                                          1st Qu.:-0.6581
##
                                                             1st Qu.:-0.89568
##
   Median :-0.3027
                       Median :-0.1863
                                          Median :-0.4130
                                                             Median : 0.04145
   Mean
           : 0.0000
                       Mean
                              : 0.0000
                                         Mean
                                                 : 0.0000
                                                             Mean
                                                                    : 0.00000
    3rd Qu.: 0.1866
                       3rd Qu.:-0.1863
                                          3rd Qu.: 0.2756
                                                             3rd Qu.: 0.56208
##
##
    Max.
           :16.1868
                       Max.
                              :14.2231
                                          Max.
                                                 :10.2083
                                                             Max.
                                                                    : 7.74673
##
    FlightMiles
                       FlightTrans
                                           DaysSinceEnroll
##
           :-0.3286
                              :-0.36212
   Min.
                       Min.
                                           Min.
                                                  :-1.99336
                       1st Qu.:-0.36212
##
    1st Qu.:-0.3286
                                           1st Qu.:-0.86607
##
    Median :-0.3286
                       Median :-0.36212
                                           Median :-0.01092
##
    Mean
           : 0.0000
                       Mean
                              : 0.00000
                                           Mean
                                                  : 0.00000
                       3rd Qu.:-0.09849
    3rd Qu.:-0.1065
                                           3rd Qu.: 0.80960
           :21.6803
                              :13.61035
                                           Max.
                                                   : 2.02284
```

The first command pre-processes the data, and the second command performs the normalization. If you look at the summary of airlinesNorm, you should see that all of the variables now have mean zero. You can also see that each of the variables has standard deviation 1 by using the sd() function.

In the normalized data, which variable has the largest maximum value?

In the normalized data, which variable has the smallest minimum value?

# Explanation

After running the two lines of code to normalize the data, you can look at the summary of airlinesNorm with the command:

summary(airlinesNorm)

You can see from the output that FlightMiles now has the largest maximum value, and DaysSinceEnroll now has the smallest minimum value. Note that these were not the variables with the largest and smallest values in the original dataset airlines.

# 2.1) Hierarchical Clustering

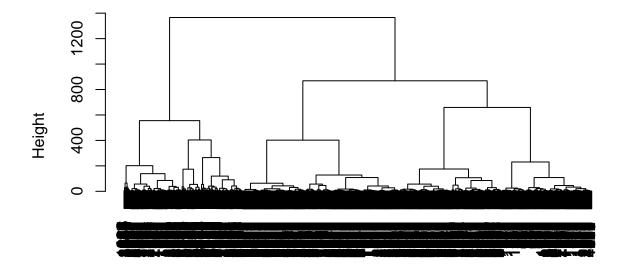
Compute the distances between data points (using euclidean distance) and then run the Hierarchical clustering algorithm (using method="ward.D") on the normalized data. It may take a few minutes for the commands to finish since the dataset has a large number of observations for hierarchical clustering.

```
dist_mat = dist(airlines_norm, method = 'euclidean')
clusters_hc = hclust(dist_mat, method = 'ward.D')
```

Then, plot the dendrogram of the hierarchical clustering process. Suppose the airline is looking for somewhere between 2 and 10 clusters. According to the dendrogram, which of the following is NOT a good choice for the number of clusters?

plot(clusters\_hc)

# **Cluster Dendrogram**



dist\_mat hclust (\*, "ward.D")



# **Explanation**

You can plot the dendrogram with the command: plot(hierClust)

If you run a horizontal line down the dendrogram, you call clusters, 3 clusters, or 7 clusters. However, it it hard to se clusters is probably not a good choice.

### 2.2) Hierarchical Clustering

Suppose that after looking at the dendrogram and discussing with the marketing department, the airline decides to proceed with 5 clusters. Divide the data points into 5 clusters by using the cutree function. How many data points are in Cluster 1?

```
clusters = cutree(clusters_hc, 5)
table(clusters)
```

## clusters

```
##
           2
                3
   776
        519
              494
                  868 1342
```

## Explanation

You can divide the data points into 5 clusters with the following command:

```
clusterGroups = cutree(hierClust, k = 5)
```

If you type table(clusterGroups), you can see that there are 776 data points in the first cluster.

#### 2.3) Hierarchical Clustering

Now, use tapply to compare the average values in each of the variables for the 5 clusters (the centroids of the clusters). You may want to compute the average values of the unnormalized data so that it is easier to interpret. You can do this for the variable "Balance" with the following command:

```
tapply(airlines$Balance, clusters, mean)
##
                                                    5
   57866.90 110669.27 198191.57 52335.91
##
                                             36255.91
tapply(airlines$QualMiles, clusters, mean)
##
                                                                   5
      0.6443299 1065.9826590
                                30.3461538
                                              4.8479263
                                                           2.5111773
tapply(airlines$BonusMiles, clusters, mean)
##
                                                    5
## 10360.124 22881.763 55795.860 20788.766
                                             2264.788
tapply(airlines$BonusTrans, clusters, mean)
##
                     2
                                          4
                                                    5
## 10.823454 18.229287 19.663968 17.087558
                                            2.973174
tapply(airlines$FlightMiles, clusters, mean)
##
     83.18428 2613.41811 327.67611 111.57373 119.32191
tapply(airlines$FlightTrans, clusters, mean)
                     2
                               3
##
           1
                                          4
                                                    5
## 0.3028351 7.4026975 1.0688259 0.3444700 0.4388972
tapply(airlines$DaysSinceEnroll, clusters, mean)
## 6235.365 4402.414 5615.709 2840.823 3060.081
Compared to the other clusters, Cluster 1 has the largest average values in which variables (if
```

any)?

```
include_graphics('2.3.a.png')
```

□ Balance		
□ QualMiles		
□ BonusMiles		
□ BonusTrans		
□ FlightMiles		
□ FlightTrans		
☑ DaysSinceEnroll ✔		
□ None		
How would you describe the customers in Cluster 1?		

include\_graphics('2.3.b.png')

○ Relatively new customers who don't use the airline v
 ○ Infrequent but loyal customers. ✓
 ○ Customers who have accumulated a large amount of transactions.

Relatively new customers who seem to be accumula

2.4) Hierarchical Clustering

Compared to the other clusters, Cluster 2 has the largest average values in which variables (if any)? Select all that apply.

```
83.18428 2613.41811 327.67611 111.57373 119.32191
tapply(airlines$FlightTrans, clusters, mean)
       1 2 3
## 0.3028351 7.4026975 1.0688259 0.3444700 0.4388972
tapply(airlines$DaysSinceEnroll, clusters, mean)
## 6235.365 4402.414 5615.709 2840.823 3060.081
include_graphics('2.4.a.png')
    □ Balance
    QualMiles
       Bonus Miles
     ☐ BonusTrans
    FlightMiles
    ✓ FlightTrans
       DaysSinceEnroll
      None
```

include\_graphics('2.4.b.png')

- Relatively new customers who don't use the airline
   Infrequent but loyal customers.
   Customers who have accumulated a large amount of transactions.
  - O Relatively new customers who seem to be accumula

#### 2.5) Hierarchical Clustering

Compared to the other clusters, Cluster 3 has the largest average values in which variables (if any)? Select all that apply.

```
## 1 2 3 4 5
## 10.823454 18.229287 19.663968 17.087558 2.973174

tapply(airlines$FlightMiles, clusters, mean)

## 1 2 3 4 5
## 83.18428 2613.41811 327.67611 111.57373 119.32191

tapply(airlines$FlightTrans, clusters, mean)

## 1 2 3 4 5
## 0.3028351 7.4026975 1.0688259 0.3444700 0.4388972

tapply(airlines$DaysSinceEnroll, clusters, mean)

## 1 2 3 4 5
## 6235.365 4402.414 5615.709 2840.823 3060.081
include_graphics('2.5.a.png')
```

✓ Balance		
□ QualMiles		
✓ BonusMiles		
✓ BonusTrans		
□ FlightMiles		
□ FlightTrans		
□ DaysSinceEnroll		
□ None		
How would you describe the customers in Cluster 3?		

include\_graphics('2.5.b.png')

- Relatively new customers who don't use the airline version of the control of the control of the customers.
  - Customers who have accumulated a large amount of
  - Customers who have accumulated a large amount of transactions.
  - Relatively new customers who seem to be accumulat

# 2.6) Hierarchical Clustering

Compared to the other clusters, Cluster 4 has the largest average values in which variables (if any)? Select all that apply.

```
tapply(airlines$Balance, clusters, mean)

## 1 2 3 4 5
## 57866.90 110669.27 198191.57 52335.91 36255.91

tapply(airlines$QualMiles, clusters, mean)

## 1 2 3 4 5
## 0.6443299 1065.9826590 30.3461538 4.8479263 2.5111773

tapply(airlines$BonusMiles, clusters, mean)

## 1 2 3 4 5
## 10360.124 22881.763 55795.860 20788.766 2264.788

tapply(airlines$BonusTrans, clusters, mean)

## 1 2 3 4 5
## 10.823454 18.229287 19.663968 17.087558 2.973174

tapply(airlines$FlightMiles, clusters, mean)

## 1 2 3 4 5
## 10.823454 18.229287 19.663968 17.087558 2.973174
```

```
## 83.18428 2613.41811 327.67611 111.57373 119.32191
tapply(airlines$FlightTrans, clusters, mean)
## 0.3028351 7.4026975 1.0688259 0.3444700 0.4388972
tapply(airlines$DaysSinceEnroll, clusters, mean)
## 6235.365 4402.414 5615.709 2840.823 3060.081
include_graphics('2.6.a.png')
    □ Balance
    □ QualMiles
       Bonus Miles
    □ BonusTrans
    ☐ FlightMiles
    ☐ FlightTrans
    □ DaysSinceEnroll
    None
```

```
include_graphics('2.6.b.png')
```

- Relatively new customers who don't use the airline v
   Infrequent but loyal customers.
   Customers who have accumulated a large amount of transactions.
  - Relatively new customers who seem to be accumulated

#### 2.7) Hierarchical Clustering

Compared to the other clusters, Cluster 5 has the largest average values in which variables (if any)? Select all that apply.

```
tapply(airlines$Balance, clusters, mean)

## 1 2 3 4 5
## 57866.90 110669.27 198191.57 52335.91 36255.91

tapply(airlines$QualMiles, clusters, mean)

## 1 2 3 4 5
## 0.6443299 1065.9826590 30.3461538 4.8479263 2.5111773

tapply(airlines$BonusMiles, clusters, mean)

## 1 2 3 4 5
## 10360.124 22881.763 55795.860 20788.766 2264.788

tapply(airlines$BonusTrans, clusters, mean)

## 1 2 3 4 5
## 10.823454 18.229287 19.663968 17.087558 2.973174
```

```
tapply(airlines$FlightMiles, clusters, mean)

## 1 2 3 4 5

## 83.18428 2613.41811 327.67611 111.57373 119.32191

tapply(airlines$FlightTrans, clusters, mean)

## 1 2 3 4 5

## 0.3028351 7.4026975 1.0688259 0.3444700 0.4388972

tapply(airlines$DaysSinceEnroll, clusters, mean)

## 1 2 3 4 5

## 6235.365 4402.414 5615.709 2840.823 3060.081

include_graphics('2.7.a.png')
```

□ Balance		
□ QualMiles		
□ BonusMiles		
□ BonusTrans		
□ FlightMiles		
□ FlightTrans		
□ DaysSinceEnroll		
✓ None		
How would you describe the customers in Cluster 5?		

include\_graphics('2.7.b.png')

Relatively new customers who don't use the airline
O Infrequent but loyal customers.
Customers who have accumulated a large amount of
<ul> <li>Customers who have accumulated a large amount of transactions.</li> </ul>
Relatively new customers who seem to be accumulated.

#### 3.1) K-Means Clustering

Now run the k-means clustering algorithm on the normalized data, again creating 5 clusters. Set the seed to 88 right before running the clustering algorithm, and set the argument iter.max to 1000.

```
set.seed(88)

clusters_k = kmeans(airlines_norm, centers = 5, iter.max = 1000)
```

How many clusters have more than 1,000 observations?

table(clusters\_k\$cluster)

# Explanation

You can run the k-means clustering algorithm with the following commands:

set.seed(88)

kmeansClust = kmeans(airlinesNorm, centers=5, iter.max=1000)

And you can look at the number of observations in each cluster with the following command:

table(kmeansClust\$cluster)

There are two clusters with more than 1000 observations.

#### 3.2) K-Means Clustering

Now, compare the cluster centroids to each other either by dividing the data points into groups and then using tapply, or by looking at the output of kmeansClustcenters, where "kmeansClust" is then ame of the output of the kmeans function will be for the normalized data. If you want to look at the average values for the unnormalized data, you need to use tapply like we did for hierarchical clustering.)

```
clusters_no = cutree(clusters_hc, 5)
table(clusters_no, clusters_k$cluster)
##
## clusters_no
                  1
                        2
                             3
                                       5
                        0
                                673
##
                  4
                            98
                                        1
##
             2
                 92
                      137
                           105
                                 92
                                       93
##
             3
                300
                        4
                           132
                                 58
                                        0
##
             4
                           653
                                 30
                                     173
                  12
                        0
##
             5
                  0
                        0
                             5
                                329 1008
clusters k$centers
##
         Balance
                    QualMiles BonusMiles BonusTrans FlightMiles FlightTrans
## 1
      1.44439706
                  0.51115730
                               1.8769284
                                           1.0331951
                                                       0.1169945
                                                                    0.1444636
     1.00054098
                  0.68382234
                               0.6144780
                                                                    4.1196141
                                           1.7214887
                                                       3.8559798
## 3 -0.05580605 -0.14104391
                               0.3041358
                                          0.7108744
                                                      -0.1218278
                                                                   -0.1287569
## 4 -0.13331742 -0.11491607 -0.3492669 -0.3373455
                                                      -0.1833989
                                                                   -0.1961819
## 5 -0.40579897 -0.02281076 -0.5816482 -0.7619054
                                                      -0.1989602
                                                                   -0.2196582
     DaysSinceEnroll
##
## 1
           0.7198040
## 2
           0.2742394
## 3
          -0.3398209
           0.9640923
## 4
## 5
          -0.8897747
```

Do you expect Cluster 1 of the K-Means clustering output to necessarily be similar to Cluster 1 of the Hierarchical clustering output?

```
include_graphics('3.2.png')
```

O Yes, because the clusters are displayed in order of size
<ul> <li>Yes, because the clusters are displayed according to similar.</li> </ul>
O No, because cluster ordering is not meaningful in eith
<ul> <li>No, because the clusters produced by the k-means al the Hierarchical algorithm.</li> </ul>

# **Explanation**

The clusters are not displayed in a meaningful order, so valgorithm that is similar to Cluster 1 produced by the Hier