# Inferential Approach to Mining Surprising Patterns in Hypergraphs

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# Reframing learning as reasoning





$$\mathcal{T} \vdash \mathcal{F}$$

# Reframing mining surprising patterns as reasoning

- 1. Learning frequent patterns
- 2. Assessing their surprisingness

Learning how to reason efficiently

## Unified Rule Engine

Evolves Inference Trees

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- Evolves Inference Trees
- Control Rules to select premises and rules

$$\begin{array}{ccc}
A & A \rightarrow C & C \rightarrow B \\
\hline
A \rightarrow B & (MP)
\end{array}$$

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## Unified Rule Engine

- Evolves Inference Trees
- Control Rules to select premises and rules

$$\underbrace{ \begin{array}{ccc} A & \xrightarrow{A \to C} & \xrightarrow{C \to B} \\ B & & \\ \end{array} (\mathsf{MP})}_{\mathsf{B}} (\mathsf{DED}) \qquad \Rightarrow \qquad \underbrace{ \begin{array}{c} \mathsf{DED} \\ \mathsf{MP} \end{array} }_{\mathsf{DED}}$$

## **Mining Frequent Patterns**

### Brute force algorithm:

- D: database
- S: minimum support
- C: pattern pool
- P, Q: patterns
- 1. Select P from C
- 2. Select *specialization Q* of *P* such that  $S \leq \text{support}(Q, \mathcal{D})$
- 3. Add Q to C
- 4. Repeat

$$\frac{\mathcal{S} \leq \text{support}(Q, \mathcal{D}) \quad \text{spec}(Q, P)}{\mathcal{S} \leq \text{support}(P, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \text{support}(Q, \mathcal{D}) \quad \text{spec}(Q, P)}{S \leq \text{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

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$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \quad \operatorname{spec}(P, Top)}{S \leq \operatorname{support}(Top, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \quad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, \textit{Top})}{S \leq \operatorname{support}(\textit{Top}, \mathcal{D})} \text{ (AP)}$$

$$\downarrow \downarrow$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

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$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)} \qquad \operatorname{spec}(P, Top)} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(R, \mathcal{D}) \qquad \operatorname{spec}(R, Q)}{S \leq \operatorname{support}(Q, \mathcal{D})} \text{ (AP)} \qquad \operatorname{spec}(Q, P)} \text{ (AP)}$$

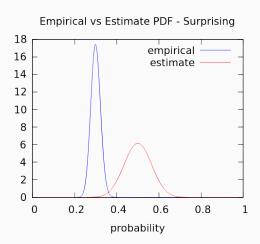
$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, Top)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

# **Mining Surprising Patterns**

#### Definition

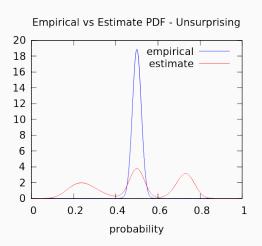
#### surprise: contrary to expectation



# **Mining Surprising Patterns**

#### Definition

#### surprise: contrary to expectation



$$\frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (DE)} \quad \frac{?}{\exp(P,\mathcal{D})} \text{ (JSD)}$$

$$S \leq \operatorname{support}(P,\mathcal{D}) \quad \operatorname{jsd}(P,\mathcal{D})) \quad \text{(S)}$$

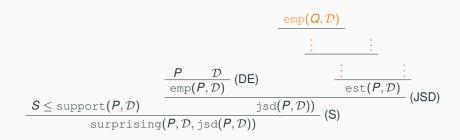
$$\operatorname{surprising}(P,\mathcal{D},\operatorname{jsd}(P,\mathcal{D}))$$

$$\frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (DE)} \quad \frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (IS)}$$

$$S \leq \operatorname{support}(P,\mathcal{D}) \quad \operatorname{jsd}(P,\mathcal{D}))$$

$$\operatorname{surprising}(P,\mathcal{D},\operatorname{jsd}(P,\mathcal{D})) \quad \text{(S)}$$

$$S \leq \operatorname{support}(P, \mathcal{D}) \qquad \frac{\vdots \qquad \vdots}{\operatorname{est}(P, \mathcal{D})} \text{ (JSD)}$$
 
$$\operatorname{Support}(P, \mathcal{D}) \qquad \operatorname{jsd}(P, \mathcal{D})) \qquad \operatorname{(S)}$$



Dynamic Surprisingness!

## **Examples**

## SUMO: Suggested Upper Merged Ontology

- 25K terms
- 80K axioms
- Covers many domains
  - Economy
  - Finance
  - Food
  - Sports
  - Music
  - . . .
- Open Source

## **Domain: Geography**

```
(EvaluationLink (stv 0.98404255 1)
   (PredicateNode "isurp")
   (ListLink
      (LambdaLink
         (VariableNode "$X")
         (PresentLink
            (InheritanceLink
               (VariableNode "$X")
               (ConceptNode "SaltWaterArea")
            (InheritanceLink
               (VariableNode "$X")
               (ConceptNode "MaritimeClaimArea")
      (ConceptNode "sumo")
```

# **Domain: Countries And Regions**

```
(EvaluationLink (stv 0.99387284 1)
   (PredicateNode "nisurp")
   (ListLink
      (LambdaLink
         (VariableList
            (VariableNode "$X")
            (VariableNode "$Y")
         (PresentLink
            (EvaluationLink
               (PredicateNode "geographicSubregion")
               (ListLink
                   (VariableNode "$X")
                  (ConceptNode "WesternEurope")
            (EvaluationLink
               (PredicateNode "dependentGeopoliticalArea")
               (ListLink
                  (VariableNode "$Y")
                  (VariableNode "$X")
      (ConceptNode "sumo")
```

## **Domain: Countries And Regions**

```
(EvaluationLink (stv 0.98713296 1)
  (PredicateNode "nisurp")
  (ListLink
     (LambdaLink
        (VariableList
           (VariableNode "$X")
           (VariableNode "$Y")
        (PresentLink
           (EvaluationLink
              (PredicateNode "dependentGeopoliticalArea")
              (ListLink
                 (VariableNode "$Y")
                 (VariableNode "$X")
           (MemberLink
              (VariableNode "$X")
              (ConceptNode "EuropeanNation")
     (ConceptNode "sumo")
```

## **Domain: Countries And Regions**

```
(EvaluationLink (stv 0.98350379 1)
  (PredicateNode "nisurp")
  (ListLink
     (LambdaLink
        (VariableNode "$X")
        (PresentLink
           (EvaluationLink
              (PredicateNode "meetsSpatially")
              (ListLink
                 (VariableNode "$X")
                 (ConceptNode "NorthAtlanticOcean")
           (MemberLink
              (VariableNode "$X")
              (ConceptNode "AmericanState")
     (ConceptNode "sumo")
```

## **Domain: Economy**

```
(EvaluationLink (stv 0.97436702 1)
  (PredicateNode "nisurp")
  (ListLink
     (LambdaLink
        (VariableNode "$X")
        (PresentLink
           (EvaluationLink
              (PredicateNode "economyType")
              (ListLink
                 (VariableNode "$X")
                 (ConceptNode "AdvancedEconomy")
           (EvaluationLink
              (PredicateNode "economyType")
              (ListLink
                 (VariableNode "$X")
                 (ConceptNode "DevelopedCountry")
     (ConceptNode "sumo")
```

# **Examples**