Probabilistic Logic Networks for Temporal and Procedural Reasoning

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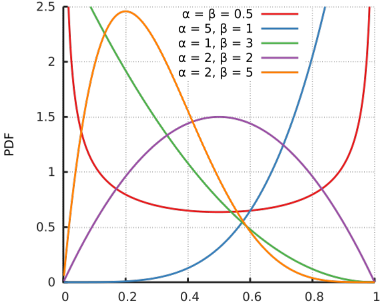

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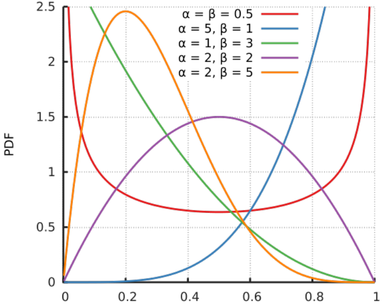

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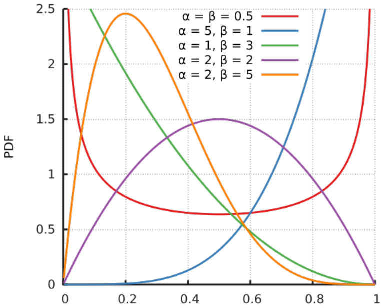

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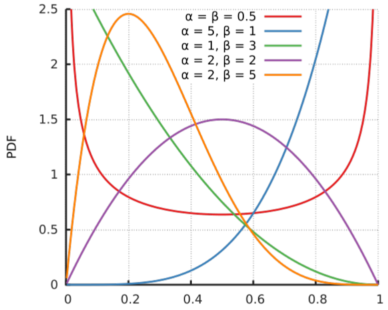

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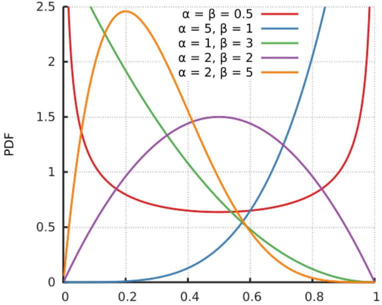

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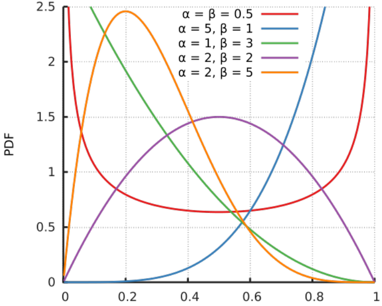

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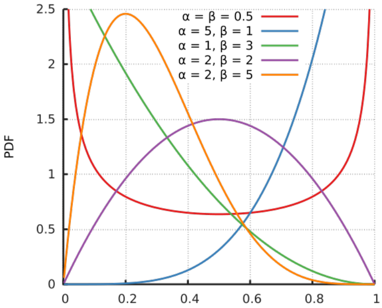

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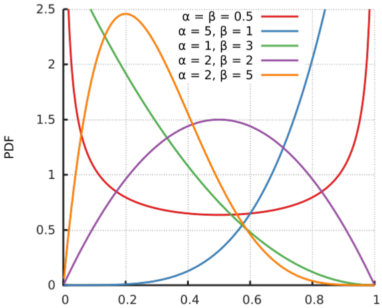

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- Implication Direct Introduction (IDI)

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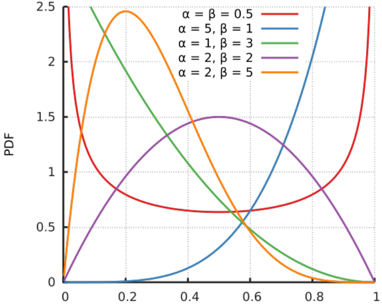

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- Deduction (D)

$$\frac{P \rightarrow Q \stackrel{m}{=} TV^{PQ} \qquad Q \rightarrow R \stackrel{m}{=} TV^{QR} \qquad P \stackrel{m}{=} TV^P \qquad Q \stackrel{m}{=} TV^Q \qquad R \stackrel{m}{=} TV^R}{P \rightarrow R \stackrel{m}{=} \phi_D\left(TV^{PQ}, \ldots, TV^R\right)} \text{(D)}$$