Inferential Approach to Mining Surprising Patterns in Hypergraphs

Nil Geisweiller, Ben Goertzel AGI-19, Shenzhen





Reframing learning as reasoning





$$\mathcal{T} \vdash \mathcal{F}$$

Reframing mining surprising patterns as reasoning

- 1. Learning frequent patterns
- 2. Assessing their surprisingness

Learning how to reason efficiently

Unified Rule Engine

Evolves Inference Trees

Unified Rule Engine

- Evolves Inference Trees
- Control Rules to select premises and rules

$$\begin{array}{ccc}
A & A \rightarrow C & C \rightarrow B \\
\hline
A \rightarrow B & (MP)
\end{array}$$

Unified Rule Engine

- Evolves Inference Trees
- Control Rules to select premises and rules

$$\begin{array}{ccc}
A & A \rightarrow C & C \rightarrow B \\
\hline
A \rightarrow B & (MP)
\end{array}$$

Unified Rule Engine

- Evolves Inference Trees
- Control Rules to select premises and rules

$$\underbrace{ \begin{array}{ccc} A & \xrightarrow{A \to C} & \xrightarrow{C \to B} \\ B & & \\ \end{array} (\mathsf{MP})}_{\mathsf{B}} (\mathsf{DED}) \qquad \Rightarrow \qquad \underbrace{ \begin{array}{c} \mathsf{DED} \\ \mathsf{MP} \end{array} }_{\mathsf{DED}}$$

Mining Frequent Patterns

Brute force algorithm:

- D: database
- S: minimum support
- C: pattern pool
- P, Q: patterns
- 1. Select P from C
- 2. Select *specialization Q* of *P* such that $S \leq \text{support}(Q, \mathcal{D})$
- 3. Add Q to C
- 4. Repeat

$$\frac{\mathcal{S} \leq \text{support}(Q, \mathcal{D}) \quad \text{spec}(Q, P)}{\mathcal{S} \leq \text{support}(P, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \text{support}(Q, \mathcal{D}) \quad \text{spec}(Q, P)}{S \leq \text{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \quad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \quad \operatorname{spec}(P, Top)}{S \leq \operatorname{support}(Top, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \quad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, \textit{Top})}{S \leq \operatorname{support}(\textit{Top}, \mathcal{D})} \text{ (AP)}$$

$$\downarrow \downarrow$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, \textit{Top})}{S \leq \operatorname{support}(\textit{Top}, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \text{support}(Q, \mathcal{D}) \quad \text{spec}(Q, P)}{S \leq \text{support}(P, \mathcal{D})} \text{ (AP = A Priory Property)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, Top)}{S \leq \operatorname{support}(Top, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)} \qquad \operatorname{spec}(P, Top)} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(R, \mathcal{D}) \qquad \operatorname{spec}(R, Q)}{S \leq \operatorname{support}(Q, \mathcal{D})} \text{ (AP)} \qquad \operatorname{spec}(Q, P)} \text{ (AP)}$$

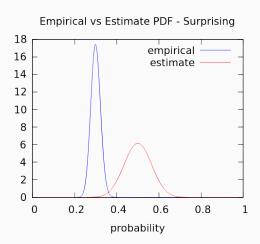
$$\frac{S \leq \operatorname{support}(Q, \mathcal{D}) \qquad \operatorname{spec}(Q, P)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

$$\frac{S \leq \operatorname{support}(P, \mathcal{D}) \qquad \operatorname{spec}(P, Top)}{S \leq \operatorname{support}(P, \mathcal{D})} \text{ (AP)}$$

Mining Surprising Patterns

Definition

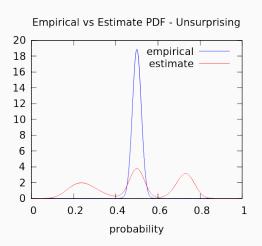
surprise: contrary to expectation



Mining Surprising Patterns

Definition

surprise: contrary to expectation



$$\frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (DE)} \quad \frac{?}{\exp(P,\mathcal{D})} \text{ (JSD)}$$

$$S \leq \operatorname{support}(P,\mathcal{D}) \quad \operatorname{jsd}(P,\mathcal{D})) \quad \text{(S)}$$

$$\operatorname{surprising}(P,\mathcal{D},\operatorname{jsd}(P,\mathcal{D}))$$

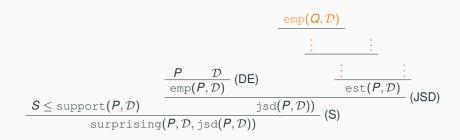
$$\frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (DE)} \quad \frac{P \quad \mathcal{D}}{\exp(P,\mathcal{D})} \text{ (IS)}$$

$$S \leq \operatorname{support}(P,\mathcal{D}) \quad \operatorname{jsd}(P,\mathcal{D}))$$

$$\operatorname{surprising}(P,\mathcal{D},\operatorname{jsd}(P,\mathcal{D})) \quad \text{(S)}$$

$$S \leq \operatorname{support}(P, \mathcal{D}) \qquad \frac{\vdots \qquad \vdots}{\operatorname{est}(P, \mathcal{D})} \text{ (JSD)}$$

$$\operatorname{Support}(P, \mathcal{D}) \qquad \operatorname{jsd}(P, \mathcal{D})) \qquad \operatorname{(S)}$$



$$\frac{P \quad \mathcal{D}}{\text{emp}(Q,\mathcal{D})}$$

$$\vdots \qquad \vdots$$

$$\frac{P \quad \mathcal{D}}{\text{emp}(P,\mathcal{D})} \text{ (DE)} \qquad \frac{\vdots \qquad \vdots}{\text{est}(P,\mathcal{D})} \text{ (JSD)}$$

$$S \leq \text{support}(P,\mathcal{D}) \qquad \text{jsd}(P,\mathcal{D})) \qquad \text{(S)}$$

Dynamic Surprisingness!

Examples