

Combinatorial Explosion with 12–15 Primitives

1) Ordered sequences, one primitive per step

- Without repetition (each primitive used at most once): Count of sequences of length $k = P(n,k) = n! / (n-k)!$ - With repetition (can reuse a primitive): Count of sequences of length $k = n^k$
Concrete numbers: - For $n=12$, $K=3$: No repeat = [12, 132, 1,320] (total 1,464). With repeat = [12, 144, 1,728] (total 1,884). - For $n=12$, $K=5$: Totals $\approx 108k$ (no repeat) vs $\approx 271k$ (with repeat). - For $n=15$, $K=3$: No repeat = [15, 210, 2,730] (total 2,955). With repeat = [15, 225, 3,375] (total 3,615). - For $n=15$, $K=5$: Totals $\approx 396k$ (no repeat) vs $\approx 814k$ (with repeat).

2) Multiple primitives in the same step (concurrent sets)

If you allow a “step” to be any non-empty subset of primitives, the options per step are $(2^n - 1)$. - For $n=12$: 4,095 options per step. Two steps $\rightarrow \sim 16.8$ million. Three steps $\rightarrow \sim 68.7$ billion. - For $n=15$: 32,767 options per step. Two steps $\rightarrow \sim 1.07$ billion. Three steps $\rightarrow \sim 35.2$ trillion.

3) Parameters multiply the space

If each primitive has r discrete parameter choices (e.g., amounts, slippage bands), sequences of length k get multiplied by r^k . Example: $n=12$, $k=4$, with repetition and $r=10 \rightarrow 12^4 \times 10^4 \approx 2.07 \times 10^8$. With continuous parameters, the raw space is effectively unbounded.

4) Why WDD + constraints are essential

- A static hash map of allowed combos can help for a few hard “never” rules, but won’t scale with these numbers. - WDD (Warp \rightarrow Detect \rightarrow Denoise) slashes the search by only keeping primitives with real trace evidence and suppressing phantoms. - A small declarative constraint layer (compatibility + ordering + stateful guards) prunes the rest. - Verifiers (AMM invariant, $HF \geq 1$, oracle freshness, etc.) are the final gate \rightarrow abstain if anything fails.

TL;DR

With 12–15 primitives, even short sequences (4–5 steps) already reach 10^4 – 10^6 possibilities; allowing combos per step jumps to 10^9 – 10^{13} +. Parameter choices multiply these counts dramatically. This is why we don’t enumerate: we detect from signals (WDD), apply tight constraints, and verify.