Chamelean

Property-Based Testing for Lean via Metaprogramming

In collaboration with

Ernest Ng
(advised by Cody Roux & Mike Hicks)

Property-Based Testing

1. Write *properties*

Spec for Binary Search Trees (BSTs):

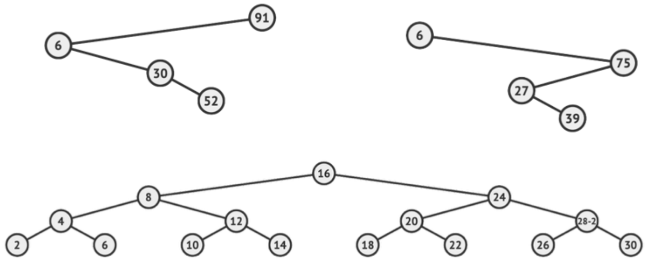
```
∀ x tree,
  isBST tree
  ⟹ isBST (insert x tree)
```

Property-Based Testing (PBT)

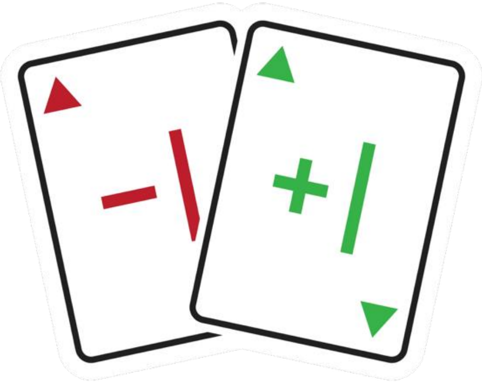
2. Generate *random inputs*

⇝ `1, 2, 4, 7, 9, …`

⇝



3. Test if random inputs satisfy property



Why should proof assistants support PBT?

Writing proofs is hard & time-consuming

$\Longrightarrow$ Perform PBT before embarking on proofs!

Every major proof assistant has a PBT framework

ROCQ

Agda

Isabelle

LEAN

Problem: writing PBT generators is hard

Cedar team: writing good generators took 6 months (estimated)

CEDAR

Jane Street devs: writing generators is “tedious” & “high-effort”

Goldstein et al. (ICSE ‘24)

The Constrained Random Generation Problem

Given some proposition P,
automatically generate random values satisfying P

The Constrained Random Generation Problem

Given some ***inductive relation*** P,

automatically generate random values satisfying P

Inductive Relations

`isBST lo hi tree`

"is `tree` a `BST` containing values between `lo` & `hi`?"

```
inductive isBST : Nat → Nat → Tree → Prop where
  …
```

Inductive Relations

`isBST lo hi tree`

"is `tree` a `BST` containing values between `lo` & `hi`?"

```
inductive isBST : Nat → Nat → Tree → Prop where
 | BSTLeaf : ∀ lo hi, isBST lo hi Leaf
 …
```

Inductive Relations

`isBST lo hi tree`

"is `tree` a `BST` containing values between `lo` & `hi`?"

```
inductive isBST : Nat → Nat → Tree → Prop where
 | BSTLeaf : ∀ lo hi, isBST lo hi Leaf
 | BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    isBST x hi r →
    isBST lo hi (Node x l r)
```

`isBST lo hi tree`

"is `tree` a `BST` containing values between `lo` & `hi`?"

Function

```
def isBST :
  Nat → Nat → Tree → Bool :=
  …
```

✓ Can be executed!
✗ Can't encode all properties
✗ Hard to reason inductively

Inductive Relation

```
inductive isBST :
  Nat → Nat → Tree → Prop where
  …
```

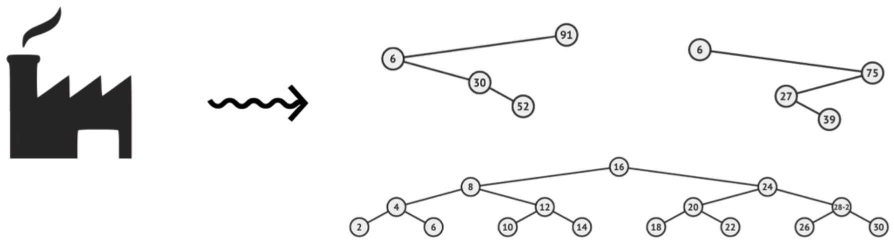
✓ Facilitates inductive reasoning!
✓ Easy to model properties!
✗ No computational content
(Chamelean addresses this issue!)

Chamelean

1. User specifies a Lean inductive relation

```
inductive isBST :
  Nat → Nat → Tree → Prop where
| BSTLeaf : …
| BSTNode : …
```

2. Chamelean derives a generator of random data satisfying the relation



(a generator of `Tree`s satisfying `isBST`)

```
#derive_generator (fun tree ⇒ isBST lo hi tree)
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  ...
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⇒ …
  | succ fuel’ ⇒ …
```

pattern-match on `fuel` parameter

(needed to make generators structurally drecreasing)

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ return Leaf
  | succ fuel’ ⟹ …
```

input t unified with Leaf

```
inductive isBST (lo : Nat) (hi : Nat) (t : Tree) : Prop where
 | BSTLeaf : ∀ lo hi, isBST lo hi Leaf
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ return Leaf
  | succ fuel’ ⟹
    backtrack [
      …
    ]
```

`backtrack` keeps picking from a (weighted) list of sub-generators until one succeeds

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⇒ return Leaf
  | succ fuel’ ⇒
    backtrack [
      (1, return Leaf),
       …
    ]
```

input t unified with Leaf

```
inductive isBST (lo : Nat) (hi : Nat) (t : Tree) : Prop where
 | BSTLeaf : ∀ lo hi, isBST lo hi Leaf
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ …
  | succ fuel’ ⟹
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
        …
```

(Recursive case)

```
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    isBST x hi r →
    isBST lo hi (Node x l r)
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⇒ …
  | succ fuel’ ⇒
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
        let x ← genSuchThat (fun x ⇒ lo < x < hi)
        …
```

```
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    …
```

Type class method for the derived generator associated with `lo < x < hi`

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ …
  | succ fuel’ ⟹
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
         let x ← genSuchThat (fun x ⟹ lo < x < hi)
         let l ← genBST lo x fuel’
         …
```

Recursively generate left subtree `l`

```
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    …
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ …
  | succ fuel’ ⟹
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
         let x ← genSuchThat (fun x ⟹ lo < x < hi)
         let l ← genBST lo x fuel’
         let r ← genBST x hi fuel’
         …
```

Recursively generate right subtree r

```
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    isBST x hi r →
    …
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ …
  | succ fuel’ ⟹
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
        let x ← genSuchThat (fun x ⟹ lo < x < hi)
        let l ← genBST lo x fuel’
        let r ← genBST x hi fuel’
        return (Node x l r))
    ]
```

Return a Node

```
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    isBST x hi r →
    isBST lo hi (Node x l r)
```

Anatomy of a Generator

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⟹ …
  | succ fuel’ ⟹
    backtrack [
      (1, return Leaf),
      (succ fuel’, do
         let x ← genSuchThat (fun x ⟹ lo < x < hi)
         let l ← genBST lo x fuel’
         let r ← genBST x hi fuel’
         return (Node x l r)
    ]
```

```
inductive isBST
  (lo : Nat)
  (hi : Nat)
  (t : Tree) : Prop where
| BSTNode : ∀ lo hi x l r,
    lo < x < hi  →
    isBST lo x l →
    isBST x hi r →
    isBST lo hi (Node x l r)
```

input `t` unified with `(Node x l r)`

Some Generators are Better Than Others

A ***naïve*** BST generator

```
let x ← arbitrary
```

Generate some `arbitrary` (unconstrained) x

Some Generators are Better Than Others

A *naïve* BST generator

```
let x ← arbitrary
if (lo < x < hi) then
    …
    return some (Node x l r)
else
    return none
```

← Generate some `arbitrary` (unconstrained) x

← Check if `lo < x < hi`

Bad!
For arbitrary x, $\mathbb{P}$(`lo < x < hi`) is low

Generator Schedules

A ***smarter*** BST generator

```
do
  let x ← genSuchThat
              (fun x ⇒ lo < x < hi)
  let l ← genBST lo x fuel'
  let r ← genBST x hi fuel'
  return (Node x l r))
```

- Prioritize constrained generation (`genSuchThat`) over checks
- Rewrite generator based on variable dependencies (i.e. generate x before `l` & `r`)

Testing Theorems, Fully Automatically

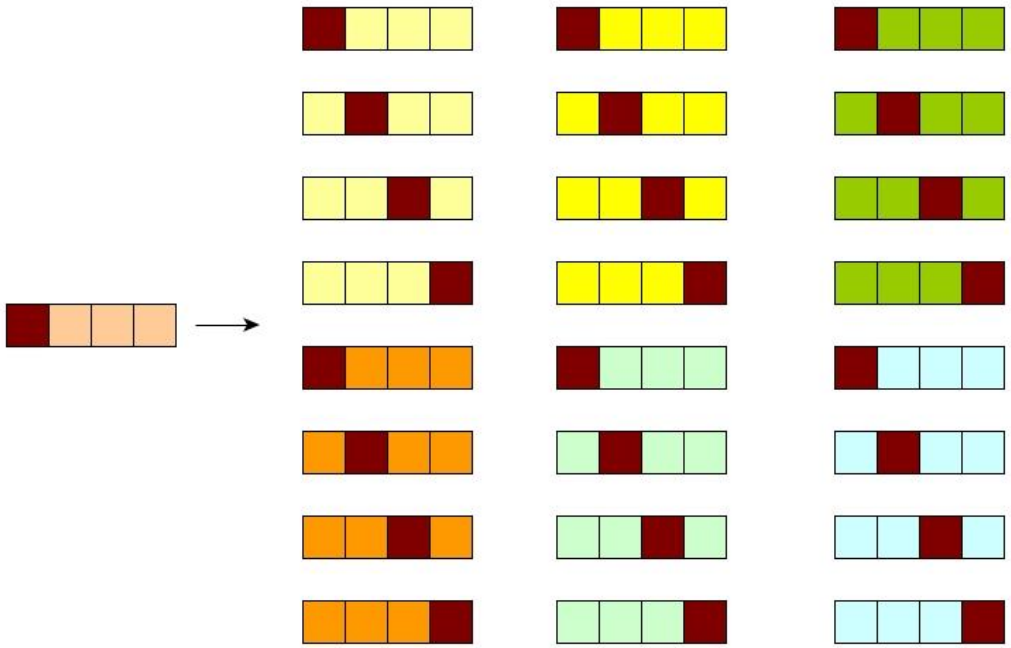
ANONYMOUS AUTHOR(S)

(Elazar-Mittelman et al., submitted to POPL '26)

Chamelean also derives **Checkers**

```
inductive Permutation
  (l  : List Nat)
  (l’ : List Nat) : Prop
```

Chamelean derives a function which ***checks*** if `l`, `l’` are permutations of each other



Chamelean also derives **Enumerators**

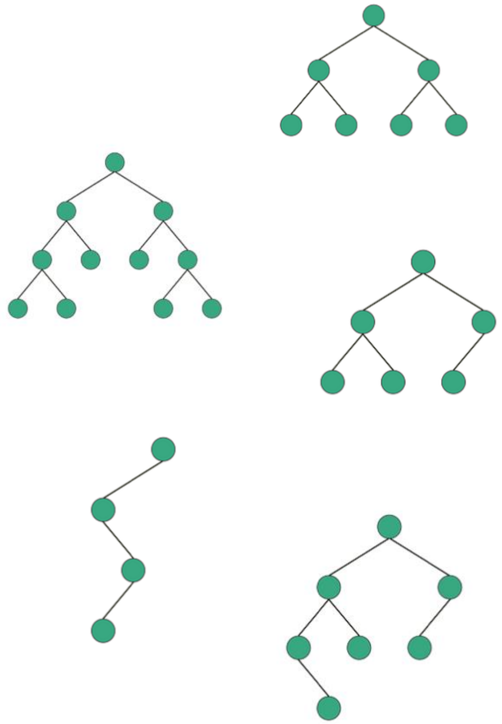
```
inductive Permutation : List Nat → List Nat → Prop where
  | Transitivity : ∀ l₁ l₂ l₃,
              Permutation l₁ l₂ →
              Permutation l₂ l₃ →
              Permutation l₁ l₃
...
```

l_2 doesn't appear in the conclusion of `Transitivity`

⟹ Chamelean ***enumerates*** l_2 such that l_2 is also a valid `Permutation`

Deriving **Unconstrained Generators** for Inductive Types

```
inductive Tree
  | Leaf : Tree
  | Node : Nat → Tree → Tree → Tree
  deriving Arbitrary, Enum
```



Chamelean implements ideas pioneered in Rocq's QuickChick PBT framework

Testing Theorems, Fully Automatically

ANONYMOUS AUTHOR(S)

Submitted to POPL '26

Computing Correctly with Inductive Relations

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PLDI '22

ROCQ

Generating Good Generators for Inductive Relations

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ZOE PARASKEVOPOULOU, Princeton University, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA

POPL '18

QuickChick

Demo

```
/-- Datatype for binary trees -/
inductive Tree where
  | Leaf : Tree
  | Node : Nat → Tree → Tree → Tree

/-- `Between lo x hi` means `lo < x < hi` -/
inductive Between : Nat → Nat → Nat → Prop where
| BetweenN : ∀ n m,
  n ≤ m →
  Between n (.succ n) (.succ (.succ m))
| BetweenS : ∀ n m o,
  Between n m o → Between n (.succ m) (.succ o)

#derive_generator (fun (x : Nat) ⇒ Between lo x hi)

/-- `BST lo hi t` describes whether a tree `t` is a BST that
    contains values strictly within `lo` and `hi` -/
inductive BST : Nat → Nat → Tree → Prop where
  | BSTLeaf: ∀ lo hi, BST lo hi .Leaf
  | BSTNode: ∀ lo hi x l r,
    Between lo x hi →
    BST lo x l →
    BST x hi r →
    BST lo hi (.Node x l r)

#derive_generator (fun (t : Tree) ⇒ BST lo hi t)
```

Derives a generator for
`x` satisfying `lo < x < hi`

Derives a generator for
`Tree`s satisfying `BST`

Code for derived generator automatically displayed in VS Code side panel

FinalDemo.lean U

Plausible > Chamelean > FinalDemo.lean > ...

```lean
/-- Datatype for binary trees -/
inductive Tree where
  | Leaf : Tree
  | Node : Nat → Tree → Tree → Tree

/-- `Between lo x hi` means `lo < x < hi` -/
inductive Between : Nat → Nat → Nat → Prop where
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#derive_generator (fun (x : Nat) ⇒ Between lo x hi)

/-- `BST lo hi t` describes whether a tree `t` is a BST that
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inductive BST : Nat → Nat → Tree → Prop where
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  | BSTNode: ∀ lo hi x l r,
    Between lo x hi →
    BST lo x l →
    BST x hi r →
    BST lo hi (.Node x l r)

#derive_generator (fun (t : Tree) ⇒ BST lo hi t)
```

Lean InfoView

▼ FinalDemo.lean:29:49

▼ Suggestions

```lean
Try this generator: instance : ArbitrarySizedSuchThat Tree (fun t_1 ⇒ BST lo_1 hi_1 t_1) where
  arbitrarySizedST :=
    let rec aux_arb (initSize : Nat) (size : Nat) (lo_1 : Nat) (hi_1 : Nat) : OptionT Plausible.Gen Tree :=
      match size with
      | Nat.zero ⇒ OptionTGen.backtrack [(1, return Tree.Leaf)]
      | Nat.succ size' ⇒
        OptionTGen.backtrack
          [(1, return Tree.Leaf),
            (Nat.succ size', do
              let x ← ArbitrarySizedSuchThat.arbitrarySizedST (fun x ⇒ Between lo_1 x hi_1) initSize;
              do
                let l ← aux_arb initSize size' lo_1 x;
                do
                  let r ← aux_arb initSize size' x hi_1;
                  return Tree.Node x l r)]
    fun size ⇒ aux_arb size size lo_1 hi_1
```

▶ Messages (1)

▶ All Messages (2)

Clicking on suggested code automatically inserts the generator into your Lean file

```
/-- `BST lo hi t` describes whether a tree `t` is a BST that
    contains values strictly within `lo` and `hi` -/
inductive BST : Nat → Nat → Tree → Prop where
  | BSTLeaf: ∀ lo hi, BST lo hi .Leaf
  | BSTNode: ∀ lo hi x l r,
    Between lo x hi →
    BST lo x l →
    BST x hi r →
    BST lo hi (.Node x l r)

instance {lo_1 hi_1} : ArbitrarySizedSuchThat Tree (fun t_1 ⇒ BST lo_1 hi_1 t_1) where
  arbitrarySizedST :=
    let rec aux_arb (initSize : Nat) (size : Nat) (lo_1 : Nat) (hi_1 : Nat) : OptionT Plausible.Gen Tree :=
      match size with
      | Nat.zero ⇒ OptionTGen.backtrack [(1, return Tree.Leaf)]
      | Nat.succ size' ⇒
        OptionTGen.backtrack
          [(1, return Tree.Leaf),
            (Nat.succ size', do
              let x ← ArbitrarySizedSuchThat.arbitrarySizedST (fun x ⇒ Between lo_1 x hi_1) initSize;
              do
                let l ← aux_arb initSize size' lo_1 x;
                do
                  let r ← aux_arb initSize size' x hi_1;
                  return Tree.Node x l r)]
    fun size ⇒ aux_arb size size lo_1 hi_1
```

Inserted automatically

Testing a property using Chamelean

Property

```
∀ x lo hi tree,
  BST lo hi tree ∧ lo < x < hi
  ⟹ BST lo hi (insert x tree)
```

Test harness
(pseudocode)

```
let x ← chooseNat lo hi
let t ← genSuchThat
        (fun tree ⟹ BST lo hi tree)
let t' := insert x t
check (BST lo hi t')
```

Derived generator

Derived checker

(obtained the same way as generators)

Testing a property using Chamelean

```lean
/-- Inserts an element into a tree, respecting the BST invariants -/
def insert (x : Nat) (t : Tree) : Tree :=
  match t with
  | .Leaf ⇒ .Node x .Leaf .Leaf
  | .Node y l r ⇒
    if x < y then
      .Node y (insert x l) r
    else if x > y then
      .Node y l (insert x r)
    else t

/-- Test harness for testing the property
    `∀ (x : Nat) (t : Tree), BST 0 10 t → BST 0 10 (insert x t)`
    for `numTrials` iterations.

    (Details omitted) -/
def runTests (numTrials : Nat) : IO Unit :=⋯

-- Uncomment this to run the aforementioned test harness
#eval runTests (numTrials := 10000)
```

▼ Messages (1)

▼ FinalDemo.lean:82:0

```
Chamelean: finished 10000 tests, 10000 passed
```

▶ All Messages (5)

Falsifying a property using Chamelean

Buggy BST
insertion function

```
/-- Buggy insertion function: ignores the input tree and
    returns a two-node tree where both values are `x` -/
def buggyInsert (x : Nat) (_ : Tree) : Tree :=
  .Node x (.Node x .Leaf .Leaf) .Leaf

/-- Test harness for testing the property
    `∀ (x : Nat) (t : Tree), BST 0 10 t → BST 0 10 (insert x t)`
    for `numTrials` iterations.

    (Details omitted) -/
def runTests (numTrials : Nat) : IO Unit :=⋯

-- Uncomment this to run the aforementioned test harness
#eval runTests (numTrials := 10000)
```

▼Messages (1)

▼FinalDemo.lean:84:0

```
Property falsified!
t = Tree.Node 9 (Tree.Node 8 (Tree.Node 7 (Tree.Node 2 (Tree.Leaf)
(Tree.Leaf)) (Tree.Leaf)) (Tree.Leaf)) (Tree.Leaf)
x = 4
t' = Tree.Node 4 (Tree.Node 4 (Tree.Leaf) (Tree.Leaf)) (Tree.Leaf)
```

▶ All Messages (5)

Case Studies

Examples

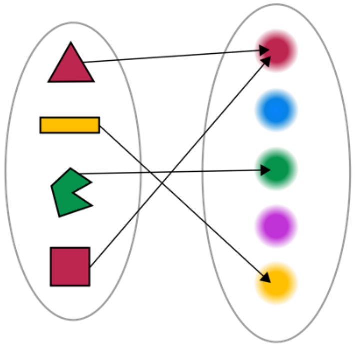
$$\Gamma \vdash e : \tau$$

Well-typed
STLC terms

`[^ ]*?@[^ ]*?\.[^ ]*`

Strings that match
regular expressions

Binary trees
(BSTs, balanced, complete, ...)



API calls to a
Key-Value Store

Generating Simply-Typed λ-Calculus Terms

This is an area of active research:

Pałka et al. AST '11
Fetscher et al. ESOP '15
Claessen et al. JFP '15
Midtgaard et al. ICFP '17
Frank et al. POPL '24
...

Chamelean automatically derives a generator for well-typed terms!

```
λ x : Nat. 1
λ x : Nat. ((3 + x) + 4)
((λ x : Nat. x) 0) + ((λ x : Nat. x + 4) 1)
```

Aside: the Cedar language

Cutler et al. OOPSLA ’24
Disselkoen et al. FSE ‘24

DSL developed at AWS
for rule-based access control:

```
forbid(                                        // Effect
  principal,                                   // Scope
  action,
  resource)
when {                                         // Condition
 resource.tags.contains(“private”) &&
 !(resource in principal.account)
};
```

Ongoing Work: Generating Cedar Terms

$$\alpha;\Gamma \vdash \texttt{true} : \mathit{True}; \emptyset \qquad \alpha;\Gamma \vdash \texttt{false} : \mathit{False}; \varepsilon \qquad \alpha;\Gamma \vdash e \texttt{ == } e : \mathit{True}; \emptyset$$

$$\frac{\alpha;\Gamma \vdash e_1 : E_1; \varepsilon_1 \qquad \alpha;\Gamma \vdash e_2 : E_2; \varepsilon_2 \qquad E_1 \neq E_2}{\alpha;\Gamma \vdash e_1 \texttt{ == } e_2 : \mathit{False}; \varepsilon}$$

$$\frac{s_1 \neq s_2}{\alpha;\Gamma \vdash E{::}s_1 \texttt{ == } E{::}s_2 : \mathit{False}; \varepsilon}$$

$$\frac{\alpha;\Gamma \vdash e_1 : \tau_1; \varepsilon_1 \qquad \alpha;\Gamma \vdash e_2 : \tau_2; \varepsilon_2 \qquad \tau_1 <: \tau \quad \tau_2 <: \tau \text{ for some } \tau}{\alpha;\Gamma \vdash e_1 \texttt{ == } e_2 : \mathit{Bool}; \emptyset}$$

$$\frac{\alpha;\Gamma \vdash e : E_1; \varepsilon \qquad (E_1 = E) \Rightarrow \tau = \mathit{True} \qquad (E_1 \neq E) \Rightarrow \tau = \mathit{False}}{\alpha;\Gamma \vdash e \texttt{ is } E : \tau; \emptyset}$$

$$\frac{\alpha;\Gamma \vdash e_1 : E_1; \varepsilon_1 \qquad \alpha;\Gamma \vdash e_2 : E_2; \varepsilon_2 \qquad E_1 \neq E_2 \qquad M(E_1) = (\_, H) \qquad E_2 \notin H}{\alpha;\Gamma \vdash e_1 \texttt{ in } e_2 : \mathit{False}; \varepsilon}$$

$$\frac{\alpha;\Gamma \vdash e_1 : E_1; \varepsilon_1 \qquad \alpha;\Gamma \vdash e_2 : E_2; \varepsilon_2}{\alpha;\Gamma \vdash e_1 \texttt{ in } e_2 : \mathit{Bool}; \emptyset}$$

$$\frac{\alpha;\Gamma \vdash e_1 : \mathit{True}; \varepsilon_1 \qquad \alpha \cup \varepsilon_1;\Gamma \vdash e_2 : \tau; \varepsilon_2}{\alpha;\Gamma \vdash \texttt{if } e_1 \texttt{ then } e_2 \texttt{ else } e_3 : \tau; \varepsilon_1 \cup \varepsilon_2}$$

$$\frac{\alpha;\Gamma \vdash e_1 : \mathit{False}; \varepsilon_1 \qquad \alpha;\Gamma \vdash e_3 : \tau; \varepsilon_3}{\alpha;\Gamma \vdash \texttt{if } e_1 \texttt{ then } e_2 \texttt{ else } e_3 : \tau; \varepsilon_3}$$

$$\frac{\alpha;\Gamma \vdash e_1 : \mathit{Bool}; \varepsilon_1 \qquad \alpha \cup \varepsilon_1;\Gamma \vdash e_2 : \tau; \varepsilon_2 \qquad \alpha;\Gamma \vdash e_3 : \tau; \varepsilon_3}{\alpha;\Gamma \vdash \texttt{if } e_1 \texttt{ then } e_2 \texttt{ else } e_3 : \tau, (\varepsilon_1 \cup \varepsilon_2) \cap \varepsilon_3}$$

$$\frac{\alpha;\Gamma \vdash e : \tau; \varepsilon \qquad \tau <: \tau'}{\alpha;\Gamma \vdash e : \tau'; \varepsilon}$$

$$\frac{\alpha;\Gamma \vdash e : \tau; \varepsilon \qquad \mathit{attribute}(f, \tau) = (?\, f : \tau_f)}{\alpha;\Gamma \vdash e \mathit{ has } f : \mathit{Bool}, \{e.f\}}$$

$$\frac{\alpha;\Gamma \vdash e : \tau; \varepsilon \qquad \mathit{attribute}(f, \tau) = (\omega f : \tau_f) \qquad \omega = ? \Rightarrow e.f \in \alpha}{\alpha;\Gamma \vdash e.f : \tau_f; \emptyset}$$

$\mathit{attribute}(f, \tau) = \omega f : \tau_f$ when
$\tau = \{\ldots, \omega f : \tau_f, \ldots\}$, or
$\tau = E$ and
$M(E) = (\{\ldots, \omega f : \tau_f, \ldots\}, \_)$

Cutler et al. OOPSLA '24

Lean formalization of Cedar's *static* semantics:

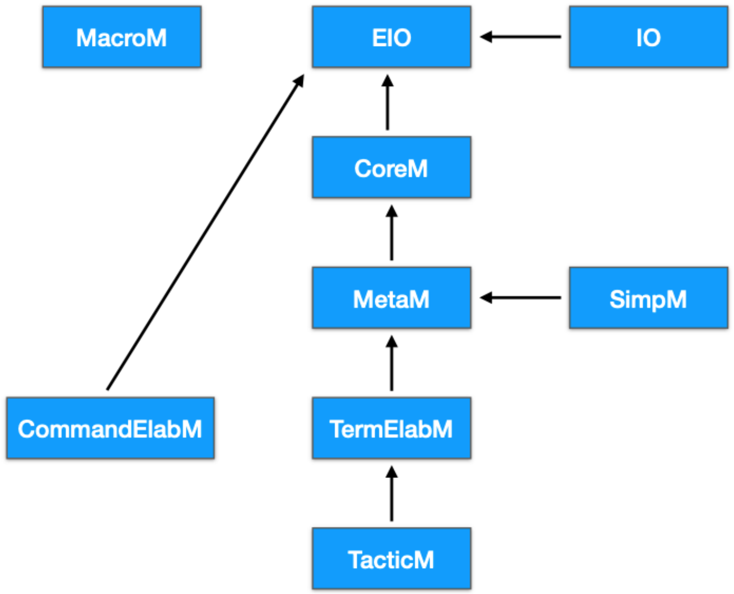
- 29 inductive relations
- Syntax defined via 17 types

- Chamelean can handle 23 / 41 typing rules
- Struggles with typing rules involving complex constraints
  - (Algorithm times out)

Building Chamelean via Metaprogamming

- Before internship: Chamelean prototype produced Lean code via pretty-printed strings
- My job: Implement QuickChick's algorithms using Lean metaprogramming idioms

Lean Monad Zoo



My prior research: developing PBT tools using OCaml metaprogramming

MICA: Automated Differential Testing for OCaml Modules

ERNEST NG*, University of Pennsylvania and Cornell University, USA
HARRISON GOLDSTEIN*, University of Pennsylvania and University of Maryland, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA

OCaml Workshop '24

Future / Related Work

The Golden Age of PBT Research

6 PBT papers to appear at ICFP / OOPSLA '25!

Bennet: Randomized Specification Testing for Heap-Manipulating Programs

ZAIN K AAMER, University of Pennsylvania, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA

We've Got You Covered: Type-Guided Repair of Incomplete Input Generators

PATRICK LAFONTAINE, Purdue University, USA
ZHE ZHOU, Purdue University, USA
ASHISH MISHRA, IIT Hyderabad, India
SURESH JAGANNATHAN, Purdue University, USA
BENJAMIN DELAWARE, Purdue University, USA

Lightweight Testing of Persistent Amortized Time Complexity in the Credit Monad

Technical Report, Aug 19, 2025 (v4).

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Tuning Random Generators

Property-Based Testing as Probabilistic Programming

RYAN TJOA, University of Washington, USA
POORVA GARG, University of California, Los Angeles, USA
HARRISON GOLDSTEIN, University of Maryland, USA
TODD MILLSTEIN, University of California, Los Angeles, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
GUY VAN DEN BROECK, University of California, Los Angeles, USA

Teaching Software Specification (Experience Report)

CAMERON MOY, Northeastern University, USA
DANIEL PATTERSON, Northeastern University, USA

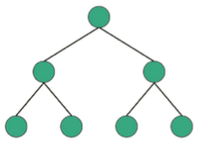
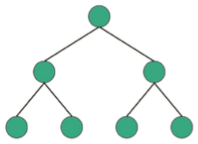
☆ An Empirical Evaluation of Property-Based Testing
Savitha Ravi, Michael Coblenz

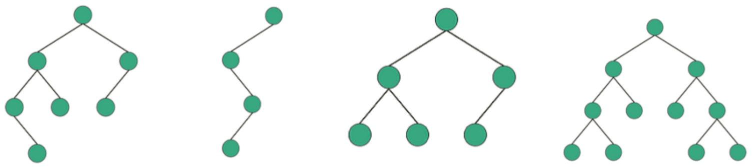
I maintain a PBT bibliography on GitHub:

`ngernest/pbt-bibliography`

Future Work

Automatically produce correctness proofs for derived generators

Soundness: If  is generated, then  is a valid BST

Completeness: All BSTs can be generated 

Future Work

Give users greater control over the distribution of generated values

Allow users to assign probabilities to constructors (à la OCaml QuickCheck)

```
type tree =
  | Leaf
  | Node1 of tree * int * tree [@weight 1/2]
  | Node2 of tree * int * tree [@weight 1/3]
[@@deriving quickcheck]
```

Tune generators using ideas from probabilistic programming

Tuning Random Generators

Property-Based Testing as Probabilistic Programming

RYAN TJOA, University of Washington, USA
POORVA GARG, University of California, Los Angeles, USA
HARRISON GOLDSTEIN, University of Maryland, USA
TODD MILLSTEIN, University of California, Los Angeles, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
GUY VAN DEN BROECK, University of California, Los Angeles, USA

To appear at OOPSLA '25

Future Work

Integrate Chamelean with PBT projects by collaborators at UMD

UNIVERSITY OF MARYLAND 1856

Derive generators using Lean's Aesop proof search tactic

The Search for Constrained Random Generators

ANONYMOUS AUTHOR(S)

Heuristics for optimizing derived generators

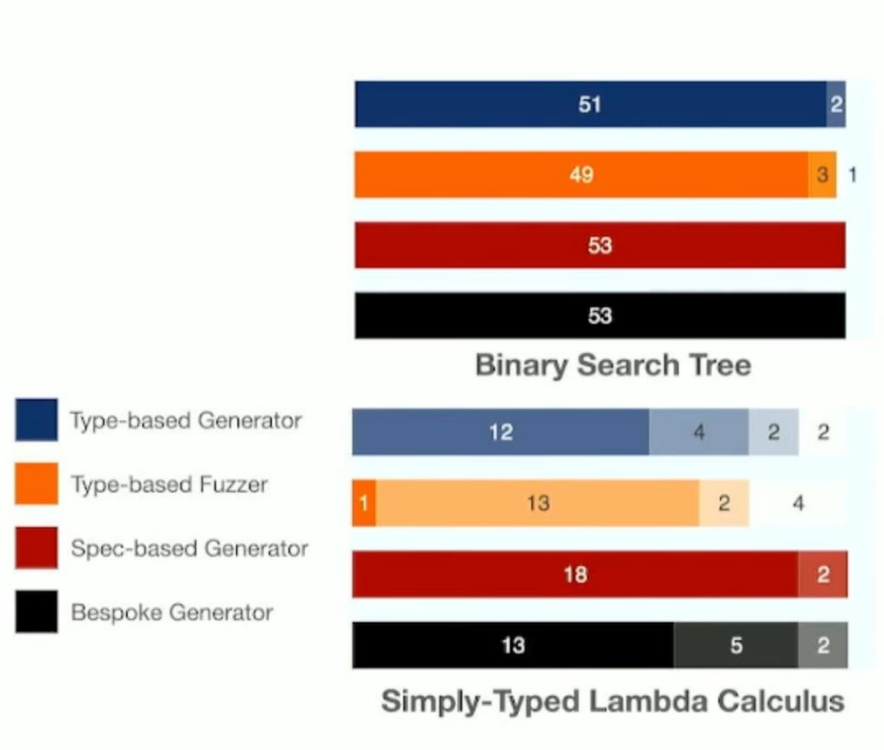
Testing Theorems, Fully Automatically

ANONYMOUS AUTHOR(S)

Both submitted to POPL '26

Future Work

Benchmark Chamelean's derived generators against their QuickChick counterparts



ETNA: An Evaluation Platform for Property-Based Testing (Experience Report)

JESSICA SHI, University of Pennsylvania, USA
ALPEREN KELES, University of Maryland, USA
HARRISON GOLDSTEIN, University of Pennsylvania, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
LEONIDAS LAMPROPOULOS, University of Maryland, USA

ICFP '23
(extended version submitted to JFP)

Use Lean's support for live programming to give users greater insight into generated values

Example from Harry Goldstein

Future Work

Extend Tyche with support for Chamelean
(VS Code extension for visualizing PBT effectiveness)

TYCHE: Making Sense of Property-Based Testing Effectiveness

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Goldstein et al. UIST '24

Summary

Chamelean derives the following
using Lean metaprogramming idioms:

For inductive relations

Generators

Enumerators

Checkers

For algebraic data types

Generators

Enumerators

Chamelean is open-source!

`ngernest/chamelean`

Ongoing work:
merging Chamelean into Lean's Plausible PBT library

Feat: Automatically Derive Generators for Algebraic Data Types #35

Open **ngernest** wants to merge 60 commits into `leanprover-community:main` from `ngernest:main`

Thank you!

Ernest Ng

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Appendix

Checkers Invoking Enumerators: An Example

$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau_2 \qquad \Gamma \vdash e_2 : \tau_1}{\Gamma \vdash e_1\ e_2 : \tau_2}$$

```
-- `typing Γ e τ` is the typing judgment `Γ ⊢ e : τ`
inductive typing: context → term → type → Prop where
  | TApp : ∀ Γ e1 e2 τ1 τ2,
      typing Γ e2 τ1 →
      typing Γ e1 (Fun τ1 τ2) →
      typing Γ (App e1 e2) τ2
…
```

τ1 doesn't appear in the conclusion of `TApp`, but is used in hypotheses
⟹ the derived checker for `typing` needs to enumerate **τ1**

Checkers Invoking Enumerators: An Example

```
| TApp : ∀ Γ e1 e2 τ1 τ2,
    typing Γ e2 τ1 →
    typing Γ e1 (Fun τ1 τ2) →
    typing Γ (App e1 e2) τ2
```

```
match e, τ with
| App e1 e2, τ2 ⇒ do
  let τ1 ← enumerateSuchThat
             (fun τ ⇒ typing Γ e2 τ)
  check (typing Γ e1 (Fun τ1 τ2))
| …
```

τ1 doesn't appear in the conclusion of `TApp`, but is used in hypotheses
⟹ the derived checker for `typing` needs to enumerate **τ1**

Given some inductive relation P, Chamelean derives:

Generators (random) — `Gen (Option α)`

Enumerators (deterministic) — `List (Option α)` (produced lazily)

Produce α's satisfying P

Checkers (semi-decision procedures) — `Option Bool` (`None` = out of fuel)

Checks if `P(α)` holds

Smarter constraint ordering

```
inductive BST : Nat → Nat → Tree → Prop where
  | BSTNode: ∀ lo hi x l r,
             lo < x < hi →
             BST lo x l →
             BST x hi r →
             BST lo hi (Node x l r)
```

Behavior of derived generator :

1. Generate x such that `lo < x < hi`
2. Generate left & right subtrees

Smarter constraint ordering

```
inductive BST : Nat → Nat → Tree → Prop where
  | BSTNode: ∀ lo hi x l r,
             BST lo x l →
             BST x hi r →
             lo < x < hi →             -- Order of hypotheses swapped
             BST lo hi (Node x l r)
```

1. Generate some unconstrained `x`
2. Generate left & right subtrees
3. **Check that `lo < x < hi`**

This check will often fail!

(For arbitrarily generated `x`, `Pr[lo < x < hi]` is low)