

Chamelean

Property-Based Testing for Lean via Metaprogramming

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In collaboration with



Property-Based Testing

1. Write *properties*

Spec for Binary Search Trees (BSTs):

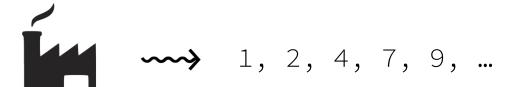
```
∀ x tree,
isBST tree

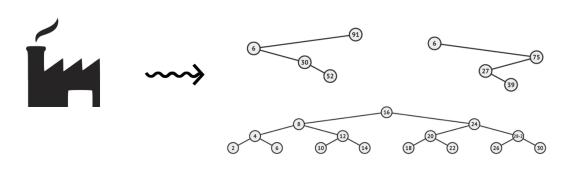
⇒ isBST (insert x tree)
```



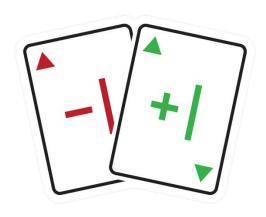
Property-Based Testing (PBT)

2. Generate *random inputs*





3. Test if random inputs satisfy property





Why should proof assistants support PBT?

Writing proofs is hard & time-consuming

⇒ Use PBT to *test* your specs before starting a proof!

the ability to use the same specifications both for runtime testing and for verification offers potential benefits for both, e.g. for quickly discovering some code and specification errors before embarking on proof,

Banerjee et al. (POPL '25)

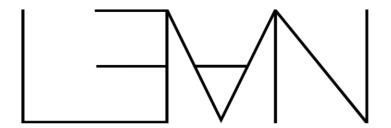


Every major proof assistant has a PBT framework











Problem: writing PBT generators is hard

Cedar team: writing good generators took 6 months (estimated)



Jane Street devs: writing generators is "tedious" & "high-effort"

Goldstein et al. (ICSE '24)



The Constrained Random Generation Problem

Given some proposition P, automatically generate random values satisfying P



The Constrained Random Generation Problem

Given some <u>inductive relation</u> P, automatically generate random values satisfying P



Inductive Relations

isBST lo hi tree

"is tree a BST containing values between lo & hi?"

```
inductive isBST : Nat → Nat → Tree → Prop where
```

•••



Inductive Relations

isBST lo hi tree

"is tree a BST containing values between lo & hi?"

```
inductive isBST : Nat → Nat → Tree → Prop where
| BSTLeaf : ∀ lo hi, isBST lo hi Leaf...
```



Inductive Relations

isBST lo hi tree

"is tree a BST containing values between lo & hi?"

```
inductive isBST : Nat → Nat → Tree → Prop where
| BSTLeaf : ∀ lo hi, isBST lo hi Leaf
| BSTNode : ∀ lo hi x l r,
    lo < x < hi →
    isBST lo x l →
    isBST x hi r →
    isBST lo hi (Node x l r)</pre>
```



isBST lo hi tree

"is tree a BST containing values between lo & hi?"

Function

Inductive Relation

```
def isBST :
  Nat → Nat → Tree → Bool :=
...
```

- ✓ Can be executed!
- X Can't encode all properties
- X Hard to reason inductively

```
inductive isBST :
  Nat → Nat → Tree → Prop where
```

- √ Facilitates inductive reasoning!
- ✓ Easy to model properties!
- X No computational content (Chamelean addresses this issue!)



Chamelean

1. User specifies a Lean inductive relation

```
1. Oser specifies a Leari inductive relation
```

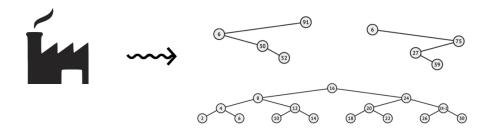
```
inductive isBST :
```

Nat → Nat → Tree → Prop where

BSTLeaf : ...

BSTNode: ...

2. Chamelean derives a generator of random data satisfying the relation



(a generator of Trees satisfying isBST)

#derive_generator (fun tree ⇒ isBST lo hi tree)



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
...
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⇒ ...
  | succ fuel' ⇒ ...
  pattern-match on fuel parameter
```



(needed to make generators

structurally drecreasing)

```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  | zero ⇒ return Leaf
  | succ fuel' ⇒ ...
  input t unified with Leaf
```

```
inductive isBST (lo : Nat) (hi : Nat) (t : Tree) : Prop where
| BSTLeaf : ∀ lo hi, isBST lo hi Leaf
```





```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
        match fuel with
        | zero ⇒ return Leaf
        | succ fuel' ⇒
         backtrack [
           (1, return Leaf), ← input t unified with Leaf
inductive isBST (lo: Nat) (hi: Nat) (t: Tree): Prop where
 | BSTLeaf : ∀ lo hi, isBST lo hi Leaf
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
  zero \implies ...
   succ fuel' ⇒
    backtrack [
      (1, return Leaf),
      (succ fuel', do (Recursive case)
                                                                  BSTNode : ∀ lo hi x l r,
                                                                    lo < x < hi \rightarrow
                                                                    isBST lo x l \rightarrow
                                                                    isBST x hi r \rightarrow
                                                                    isBST lo hi (Node x l r)
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
   zero \Rightarrow ...
   succ fuel' ⇒
    backtrack [
      (1, return Leaf),
      (succ fuel', do
                                                                     BSTNode : ∀ lo hi x l r,
          let x \leftarrow genSuchThat (fun x \Rightarrow lo < x < hi)
                                                                       lo < x < hi \rightarrow
       Type class method for the derived generator
             associated with lo < x < hi
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
   zero \Rightarrow ...
   succ fuel' ⇒
    backtrack [
      (1, return Leaf),
       (succ fuel', do
                                                                      BSTNode : ∀ lo hi x l r,
          let x \leftarrow genSuchThat (fun x \Rightarrow lo < x < hi)
                                                                         lo < x < hi \rightarrow
          let l ← genBST lo x fuel'
                                                                         isBST lo x l \rightarrow
            Recursively generate left subtree 1
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
   zero \Rightarrow ...
   succ fuel' ⇒
    backtrack [
      (1, return Leaf),
       (succ fuel', do
                                                                       BSTNode : ∀ lo hi x l r,
          let x \leftarrow genSuchThat (fun x \Rightarrow lo < x < hi)
                                                                         lo < x < hi \rightarrow
          let l ← genBST lo x fuel'
                                                                         isBST lo x l \rightarrow
          let r ← genBST x hi fuel'
                                                                         isBST x hi r \rightarrow
           Recursively generate right subtree r
```



```
def genBST (lo : Nat) (hi : Nat) (fuel : Nat) : Gen Tree :=
  match fuel with
   zero \implies ...
    succ fuel' ⇒
    backtrack [
      (1, return Leaf),
      (succ fuel', do
                                                                     BSTNode : ∀ lo hi x l r,
          let x \leftarrow genSuchThat (fun x \Rightarrow lo < x < hi)
                                                                       lo < x < hi \rightarrow
          let l ← genBST lo x fuel'
                                                                       isBST lo x l \rightarrow
          let r ← genBST x hi fuel'
                                                                       isBST x hi r \rightarrow
          return (Node x l r))
                                                                       isBST lo hi (Node x l r)
                  Return a Node
```



```
inductive isBST
                                                     (lo : Nat)
                                                     (hi : Nat)
                                                     (t: Tree) : Prop where
return (Node x l r)
                                                       isBST lo hi (Node x l r)
                          input t unified with (Node x l r)
```

Some Generators are Better Than Others

A *naïve* BST generator

let x ← arbitrary ← Generate some arbitrary (unconstrained) x



Some Generators are Better Than Others

A *naïve* BST generator



Generator Schedules

A *smarter* BST generator

- Prioritize constrained generation (genSuchThat) over checks
- Rewrite generator based on variable dependencies (i.e. generate x before 1 & r)

Testing Theorems, Fully Automatically

ANONYMOUS AUTHOR(S)

(Elazar-Mittelman et al., submitted to POPL '26)



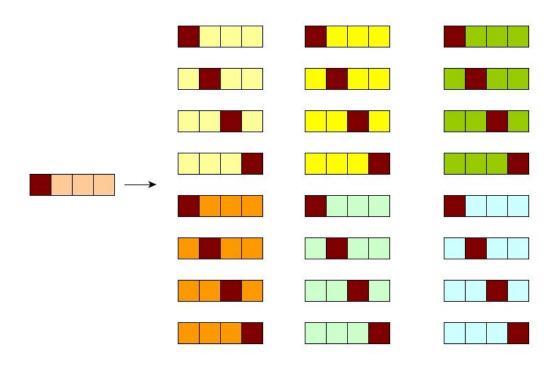
Chamelean also derives Checkers

inductive Permutation

(l': List Nat) : Prop

(l : List Nat)

Chamelean derives a function which *checks* if 1, 1' are permutations of each other





Chamelean also derives Enumerators

```
inductive Permutation : List Nat \rightarrow List Nat \rightarrow Prop where  | \text{ Transitivity : } \forall \ l_1 \ l_2 \ l_3,  Permutation l_1 \ l_2 \rightarrow Permutation l_2 \ l_3 \rightarrow Permutation l_1 \ l_3
```

l₂ doesn't appear in the conclusion of Transitivity

 \Rightarrow Chamelean *enumerates* l_2 such that l_2 is also a valid Permutation



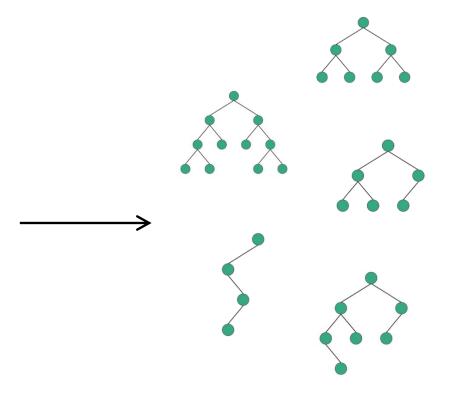
Deriving **Unconstrained Generators** for Inductive Types

inductive Tree

Leaf : Tree

Node : Nat → Tree → Tree → Tree

deriving Arbitrary, Enum





Chamelean implements ideas pioneered in Rocq's QuickChick PBT framework

Testing Theorems, Fully Automatically

ANONYMOUS AUTHOR(S)

Submitted to POPL '26



Computing Correctly with Inductive Relations

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PI DI '22

Generating Good Generators for Inductive Relations

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POPL '18





Demo



```
/-- Datatype for binary trees -/
inductive Tree where
  | Leaf : Tree
  | Node : Nat → Tree → Tree → Tree
/-- `Between lo x hi` means `lo < x < hi` -/
inductive Between : Nat \rightarrow Nat \rightarrow Prop where
 BetweenN : \forall n m,
  n \leq m \rightarrow
  Between n (.succ n) (.succ (.succ m))
  BetweenS : ∀ n m o,
  Between n m o \rightarrow Between n (.succ m) (.succ o)
#derive_generator (fun (x : Nat) \Rightarrow Between lo x hi)
/-- `BST lo hi t` describes whether a tree `t` is a BST that
    contains values strictly within `lo` and `hi` -/
inductive BST : Nat → Nat → Tree → Prop where
  | BSTLeaf: ∀ lo hi, BST lo hi .Leaf
    BSTNode: ∀ lo hi x l r,
    Between lo x hi →
    BST lo x l \rightarrow
    BST x hi r \rightarrow
    BST lo hi (.Node x l r)
#derive_generator (fun (t : Tree) ⇒ BST lo hi t)
```

Derives a generator for **x** satisfying **lo < x < hi**

Derives a generator for Trees satisfying BST

Code for derived generator automatically displayed in VS Code side panel

```
Plausible > Chamelean > ≡ FinalDemo.lean > ...
                                                                                    ▼ FinalDemo.lean:29:49
      /-- Datatype for binary trees -/
                                                                                    ▼ Suggestions
       inductive Tree where
                                                                                     Try this generator: instance : ArbitrarySizedSuchThat Tree (fun t 1 ⇒ BST lo_1 hi_1 t_1) where
         | Leaf : Tree
                                                                                       arbitrarySizedST :=
         | Node : Nat → Tree → Tree → Tree
                                                                                         let rec aux arb (initSize : Nat) (size : Nat) (lo_1 : Nat) (hi_1 : Nat) : OptionT Plausible.Gen Tree
  8
                                                                                           match size with
       /-- `Between lo x hi` means `lo < x < hi` -/
                                                                                           | Nat.zero ⇒ OptionTGen.backtrack [(1, return Tree.Leaf)]
       inductive Between : Nat \rightarrow Nat \rightarrow Prop where
                                                                                           | Nat.succ size' ⇒
       | BetweenN : ∀ n m,
                                                                                             OptionTGen.backtrack
        n \leq m \rightarrow
                                                                                               [(1, return Tree.Leaf),
         Between n (.succ n) (.succ (.succ m))
 13
                                                                                                 (Nat.succ size', do
 14
        BetweenS : ∀ n m o,
                                                                                                   let x \leftarrow ArbitrarySizedSuchThat.arbitrarySizedST (fun <math>x \Rightarrow Between lo_1 x hi_1) initSize;
         Between n m o → Between n (.succ m) (.succ o)
 15
 16
                                                                                                     let l ← aux_arb initSize size' lo_1 x;
      \#derive\_generator (fun (x : Nat) \Rightarrow Between lo x hi)
 17
 18
                                                                                                       let r ← aux_arb initSize size' x hi_1;
       /-- `BST lo hi t` describes whether a tree `t` is a BST that
 19
                                                                                                       return Tree.Node x l r)]
          contains values strictly within `lo` and `hi` -/
 20
                                                                                         fun size ⇒ aux_arb size size lo_1 hi_1
 21
       inductive BST : Nat → Nat → Tree → Prop where
         | BSTLeaf: ∀ lo hi, BST lo hi .Leaf
                                                                                    ► Messages (1)
 22
 23
         | BSTNode: ∀ lo hi x l r,
                                                                                   ► All Messages (2)
          Between lo x hi →
 24
 25
           BST lo x l \rightarrow
           BST x hi r \rightarrow
 26
           BST lo hi (.Node x l r)
 27
 28
      #derive_generator (fun (t : Tree) \Rightarrow BST lo hi t)
 29
 30
```

Clicking on suggested code automatically inserts the generator into your Lean file

```
/-- `BST lo hi t` describes whether a tree `t` is a BST that
    contains values strictly within `lo` and `hi` -/
inductive BST : Nat → Nat → Tree → Prop where
   BSTLeaf: ∀ lo hi, BST lo hi .Leaf
   BSTNode: ∀ lo hi x l r,
   Between lo x hi →
   BST lo x l \rightarrow
   BST x hi r \rightarrow
   BST lo hi (.Node x l r)
instance {lo_1 hi_1} : ArbitrarySizedSuchThat Tree (fun t_1 ⇒ BST lo_1 hi_1 t_1) where
 arbitrarySizedST :=
    let rec aux_arb (initSize : Nat) (size : Nat) (lo_1 : Nat) (hi_1 : Nat) : OptionT Plausible.Gen Tree :=
     match size with
      | Nat.zero ⇒ OptionTGen.backtrack [(1, return Tree.Leaf)]
      | Nat.succ size' ⇒
        OptionTGen.backtrack
          [(1, return Tree.Leaf),
            (Nat.succ size', do
              let x \leftarrow ArbitrarySizedSuchThat.arbitrarySizedST (fun <math>x \Rightarrow Between lo_1 x hi_1) initSize;
              do
                let l ← aux arb initSize size' lo 1 x;
                  let r ← aux arb initSize size' x hi 1;
                  return Tree.Node x l r)]
    fun size ⇒ aux_arb size size lo_1 hi_1
```

Inserted automatically

Testing a property using Chamelean

```
\forall x lo hi tree,
 Property
                        BST lo hi tree \Lambda lo \langle x \langle hi \rangle
                        ⇒ BST lo hi (insert x tree)
                     let x \leftarrow chooseNat lo hi
                     let t ← genSuchThat
                                                                             Derived
Test harness
                               (fun tree \Rightarrow BST lo hi tree)
                                                                            generator
(pseudocode)
                     let t' := insert x t
                                                                            Derived
                     check (BST lo hi t')
                                                                             checker
                                                                         (obtained the same
                                                                         way as generators)
```

Testing a property using Chamelean

```
▼ Messages (1)
/-- Inserts an element into a tree, respecting the BST invariants -/
                                                                              ▼ FinalDemo.lean:82:0
def insert (x : Nat) (t : Tree) : Tree :=
  match t with
                                                                              Chamelean: finished 10000 tests, 10000 passed
  | .Leaf ⇒ .Node x .Leaf .Leaf
                                                                            ▶ All Messages (5)
  | .Node y l r \Rightarrow
   if x < y then
      .Node y (insert x l) r
    else if x > y then
      .Node y l (insert x r)
    else t
/-- Test harness for testing the property
    \forall (x : Nat) (t : Tree), BST 0 10 t \Rightarrow BST 0 10 (insert x t)
    for `numTrials` iterations.
   (Details omitted) -/
def runTests (numTrials : Nat) : IO Unit := ...
-- Uncomment this to run the aforementioned test harness
#eval runTests (numTrials := 10000)
```

Falsifying a property using Chamelean

Buggy BST insertion function



```
/-- Buggy insertion function: ignores the input tree and
| returns a two-node tree where both values are `x` -/
def buggyInsert (x : Nat) (_ : Tree) : Tree :=
| .Node x (.Node x .Leaf .Leaf) .Leaf

/-- Test harness for testing the property
| `∀ (x : Nat) (t : Tree), BST 0 10 t → BST 0 10 (insert x t)`
for `numTrials` iterations.

(Details omitted) -/
def runTests (numTrials : Nat) : IO Unit := ...

-- Uncomment this to run the aforementioned test harness
#eval runTests (numTrials := 10000)
```

```
▼Messages (1)

▼FinalDemo.lean:84:0

Property falsified!
t = Tree.Node 9 (Tree.Node 8 (Tree.Node 7 (Tree.Node 2 (Tree.Leaf))
(Tree.Leaf)) (Tree.Leaf)) (Tree.Leaf)
x = 4
t' = Tree.Node 4 (Tree.Node 4 (Tree.Leaf)) (Tree.Leaf)

► All Messages (5)

II
```

Case Studies



Examples

Г⊢е: τ

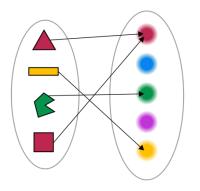
Well-typed STLC terms



Binary trees (BSTs, balanced, complete, ...)



Strings that match regular expressions



API calls to a Key-Value Store



Generating Simply-Typed λ-Calculus Terms

This is an area of active research:

Pałka et al. AST '11 Fetscher et al. ESOP '15 Claessen et al. JFP '15 Midtgaard et al. ICFP '17 Frank et al. POPL '24

. . .

Chamelean automatically derives a generator for well-typed terms!

```
\lambda \times : \text{Nat. 1}

\lambda \times : \text{Nat. } ((3 + x) + 4)

((\lambda \times : \text{Nat. } x) \cdot 0) + ((\lambda \times : \text{Nat. } x + 4) \cdot 1)
```



Aside: the Cedar language

Cutler et al. OOPSLA '24 Disselkoen et al. FSE '24

DSL developed at AWS for rule-based access control:

```
// Example Cedar policy:
// Interns can't create lists
forbid(
    principal in Team::interns,
    action == CreateList,
    resource
);
```



Ongoing Work: Generating Cedar Terms

$$\begin{array}{c} \alpha; \Gamma \vdash \text{true} : \textit{True}; \emptyset \\ \alpha; \Gamma \vdash \text{false} : \textit{False}; \varepsilon \\ \alpha; \Gamma \vdash \text{e} = = e : \textit{True}; \emptyset \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 = = e_2 : \textit{False}; \varepsilon \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 = e_2 : \textit{False}; \varepsilon \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : \tau_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : \tau_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_2 : \tau_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon \\ \alpha; \Gamma \vdash e_2 : \tau_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 = e_2 : \textit{Bool}; \emptyset \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : e_2 : E_2; \varepsilon_2 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_2 : E_2; \varepsilon_2 \\ \alpha; \Gamma \vdash e_1 : E_1; \varepsilon_1 \end{array} \qquad \begin{array}{c} \alpha; \Gamma \vdash e_1; \varepsilon_1 : \epsilon_1 : \epsilon_1; \varepsilon_1 : \epsilon_2 : \epsilon_2; \varepsilon_2 : \epsilon_2; \varepsilon_2 : \epsilon_2 : \epsilon_1; \varepsilon_2 : \epsilon_2; \varepsilon_2 : \epsilon_2 : \epsilon_2; \varepsilon_2 : \epsilon_2; \varepsilon_2 : \epsilon_1; \varepsilon_2 : \epsilon_1; \varepsilon_2$$

Lean formalization of Cedar's *static* semantics:

- 29 inductive relations
- Syntax defined via 17 types
- Chamelean can handle 23 / 41 typing rules
- Struggles with typing rules involving complex constraints
 - Algorithm times out! (Talk to me offline for details)

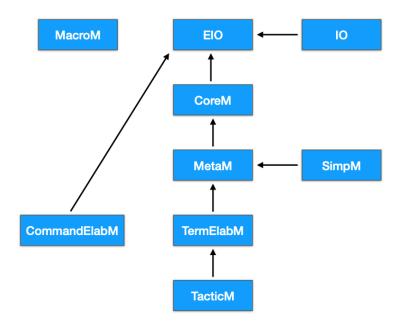
Cutler et al. OOPSLA '24



Building Chamelean via Metaprogamming

- Before internship: Chamelean prototype produced Lean code via pretty-printed strings
- My job: Implement QuickChick's algorithms using Lean metaprogramming idioms

Lean Monad Zoo



My prior research: developing PBT tools using OCaml metaprogramming

MICA: Automated Differential Testing for OCaml Modules

ERNEST NG*, University of Pennsylvania and Cornell University, USA HARRISON GOLDSTEIN*, University of Pennsylvania and University of Maryland, USA BENJAMIN C. PIERCE, University of Pennsylvania, USA

OCaml Workshop '24



Future / Related Work



The Golden Age of PBT Research

6 PBT papers to appear at ICFP / OOPSLA '25!

Bennet: Randomized Specification Testing for Heap-Manipulating Programs

ZAIN K AAMER, University of Pennsylvania, USA BENJAMIN C. PIERCE, University of Pennsylvania, USA

Tuning Random Generators

Property-Based Testing as Probabilistic Programming

RYAN TJOA, University of Washington, USA
POORVA GARG, University of California, Los Angeles, USA
HARRISON GOLDSTEIN, University of Maryland, USA
TODD MILLSTEIN, University of California, Los Angeles, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
GUY VAN DEN BROECK, University of California, Los Angeles, USA

We've Got You Covered: Type-Guided Repair of Incomplete Input Generators

PATRICK LAFONTAINE, Purdue University, USA ZHE ZHOU, Purdue University, USA ASHISH MISHRA, IIT Hyderabad, India SURESH JAGANNATHAN, Purdue University, USA BENIAMIN DELAWARE. Purdue University. USA

Lightweight Testing of Persistent Amortized Time Complexity in the Credit Monad

Technical Report, Aug 19, 2025 (v4).

Anton Lorenzen
University of Edinburgh
Edinburgh, UK
anton.lorenzen@ed.ac.uk

Teaching Software Specification (Experience Report)

CAMERON MOY, Northeastern University, USA DANIEL PATTERSON, Northeastern University, USA An Empirical Evaluation of Property-Based Testing Savitha Ravi, Michael Coblenz

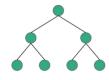
I maintain a PBT bibliography on GitHub:

ngernest/pbt-bibliography

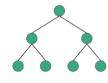




Automatically produce correctness proofs for derived generators (ask me offline about how we prove this!)



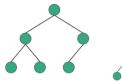
Soundness: If is generated, then is a valid BST



Completeness: All BSTs can be generated









Give users greater control over the distribution of generated values

Allow users to assign probabilities to constructors (à la OCaml QuickCheck)

```
type tree =
    | Leaf
    | Node1 of tree * int * tree [@weight 1/2]
    | Node2 of tree * int * tree [@weight 1/3]
[@@deriving quickcheck]
```

Tune generators using ideas from probabilistic programming

Tuning Random Generators

Property-Based Testing as Probabilistic Programming

RYAN TJOA, University of Washington, USA
POORVA GARG, University of California, Los Angeles, USA
HARRISON GOLDSTEIN, University of Maryland, USA
TODD MILLSTEIN, University of California, Los Angeles, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
GUY VAN DEN BROECK, University of California, Los Angeles, USA

To appear at OOPSLA '25



Integrate Chamelean with PBT projects by collaborators at UMD



Derive generators using Lean's Aesop proof search tactic

Heuristics for optimizing derived generators

The Search for Constrained Random Generators

ANONYMOUS AUTHOR(S)

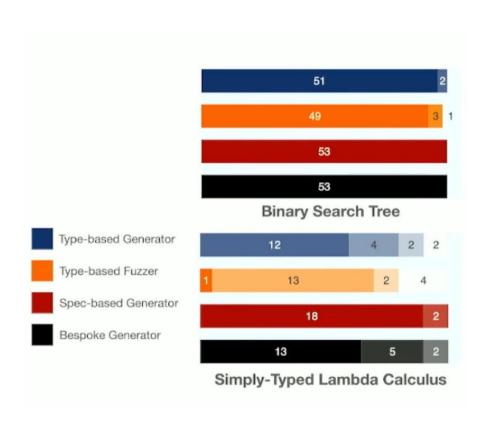
Testing Theorems, Fully Automatically

ANONYMOUS AUTHOR(S)

Both submitted to POPL '26



Benchmark Chamelean's derived generators against their QuickChick counterparts



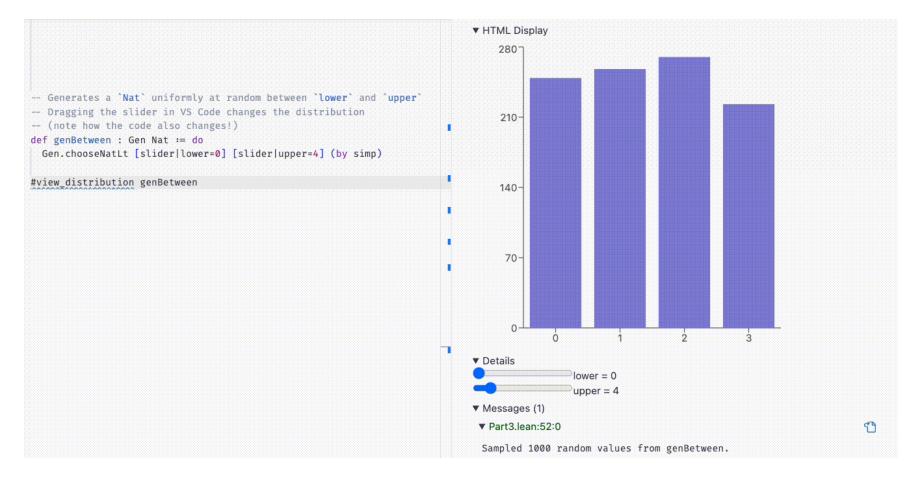
ETNA: An Evaluation Platform for Property-Based Testing (Experience Report)

JESSICA SHI, University of Pennsylvania, USA
ALPEREN KELES, University of Maryland, USA
HARRISON GOLDSTEIN, University of Pennsylvania, USA
BENJAMIN C. PIERCE, University of Pennsylvania, USA
LEONIDAS LAMPROPOULOS, University of Maryland, USA

ICFP '23 (extended version submitted to JFP)



Use Lean's support for live programming to give users greater insight into generated values



Example from Harry Goldstein



Extend Tyche with support for Chamelean (VS Code extension for visualizing PBT effectiveness)

TYCHE: Making Sense of Property-Based Testing Effectiveness

Harrison Goldstein

University of Pennsylvania Philadelphia, PA, USA hgo@seas.upenn.edu

Jeffrey Tao University of Pennsylvania

Philadelphia, PA, USA jefftao@seas.upenn.edu

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Andrew Head

University of Pennsylvania Philadelphia, PA, USA head@seas.upenn.edu

Goldstein et al. UIST '24





Summary

Chamelean derives the following using Lean metaprogramming idioms:

For inductive relations

Generators

Enumerators

Checkers

For algebraic data types

Generators

Enumerators



Chamelean is open-source!

ngernest/chamelean



Ongoing work: merging Chamelean into Lean's Plausible PBT library

Feat: Automatically Derive Generators for Algebraic Data Types #35



1) Open | ngernest wants to merge 60 commits into leanprover-community:main from ngernest:main []



Thank you!

Ernest Ng ernest@cs.cornell.edu



Appendix



Inductive Relations Can Encode Non-Termination

Example from Paraskevopoulou et al. (PLDI '22), §5

- The derived checker always returns **None** for any non-zero **Nat** (regardless of how much fuel is supplied)
- It will try to satisfy the isZero (succ n) hypothesis of the NonZero constructor (which is never satisfied!) until it runs out of fuel



Inductive Relations Can Encode Non-Determinism

Small-step semantics for the untyped λ -calculus, extended with non-deterministic choice e1 \square e2

$$\frac{}{e_1 \Box e_2 \longrightarrow e_1}$$
 (SCHOOSELEFT) $\frac{}{e_1 \Box e_2 \longrightarrow e_2}$ (SCHOOSERIGHT)

Example from CS 6110 Lecture 5



Functions vs Inductive Relations (Cont.)

Functions	(Inductive) Relations
f : A -> B	r : A -> B -> Prop
Total: for every x : A , there is one f x : B (termination checker)	Partial: for every x : A, there may be zero or more y : B such that r x y
In Coq: functions are computable terminates: TuringMachine -> Input -> bool equal: R -> R -> bool	May be non-computable terminates : TuringMachine -> Input -> Prop equal : \mathbb{R} -> \mathbb{R} -> Prop
Proving f x = y is automatic if x,y are constants (simpl, reflexivity)	Proving r x y is manual even if x,y are constants (apply constructors of r)
eval : env -> stmt -> env	big_step : env -> stmt -> env -> Prop

Taken from CS 6115 (Fall '24) Lecture 7 slides



Chamelean / QuickChick's Unification Algorithm

```
return ()
                                                                                                                                              if u_1 = u_2
unify u_1 u_2
                                                                        r_1 \leftarrow \kappa[u_1]; r_2 \leftarrow \kappa[u_2]; unifyR(u_1, r_1)(u_2, r_2) otherwise
                                                                 = unifyC(C_1 r_{11} \cdots r_{1n})(C_2 r_{21} \cdots r_{2m})
unify (C_1 r_{11} \cdots r_{1n}) (C_2 r_{21} \cdots r_{2m})
unify u_1 (C_2 r_{21} \cdots r_{2m})
                                                                 = r_1 \leftarrow \kappa[u_1]; unifyRC(u_1, r_1)(C_2 r_{21} \cdots r_{2m})
                                                                  = r_2 \leftarrow \kappa[u_2]; \ unifyRC (u_2, r_2) (C_1 r_{11} \cdots r_{1n})
unify (C_1 r_{11} \cdots r_{1n}) u_2
unifyR (u_1, undef_{\tau}) (u_2, r)
                                                                 = update u_1 u_2
unifyR (u_1, r) (u_2, undef_{\tau})
                                                                 = update u_2 u_1
unifyR (u_1, u_1') (u_2, r)
                                                                 = unify u'_1 u_2
unifyR (u_1, r) (u_2, u_2')
                                                                 = unify u_1 u_2'
unifyR(_{-},C_{1} r_{11} \cdots r_{1n})(_{-},C_{2} r_{21} \cdots r_{2m}) = unifyC(C_{1} r_{11} \cdots r_{1n})(C_{2} r_{21} \cdots r_{2m})
unifyR(u_1, fixed)(u_2, fixed)
                                                                 = equality u_1 u_2; update u_1 u_2
unifyR (u_1, fixed) (-, C_2 r_{21} \cdots r_{2m})
                                                                = match u_1 (C_2 r_{21} \cdots r_{2m})
unifyR (_-, C_1 r_{11} \cdots r_{1n}) (u_2, fixed)
                                                                 = match u_2 (C_1 r_{11} \cdots r_{1n})
                                                                = \begin{cases} fold \ unify \ \overline{(r_{1i}, r_{2i})} & \text{if } C_1 = C_2 \text{ and } n = m \end{cases}
unifyC (C_1 r_{11} \cdots r_{1n}) (C_2 r_{21} \cdots r_{2m})
unifyRC(u, undef_{\tau})(C_2 r_{21} \cdots r_{2m})
                                                                 = update u_1 (C_2 r_{21} \cdots r_{2m})
unifyRC (u, u') (C_2 r_{21} \cdots r_{2m})
                                                                 = r \leftarrow \kappa[u']; unifyRC (u',r) (C_2 r_{21} \cdots r_{2m})
unifyRC (u, fixed) (C_2 r_{21} \cdots r_{2m})
                                                                 = match\ u\ (C_2\ r_{21}\ \cdots\ r_{2m})
unifyRC(u, C_1 r_{11} \cdots r_{1n}) (C_2 r_{21} \cdots r_{2m}) = unifyC(C_1 r_{11} \cdots r_{1n}) (C_2 r_{21} \cdots r_{2m})
match\ u\ (C\ r_1\ \cdots\ r_n) = \bar{p} \leftarrow mapM\ matchAux\ \bar{r};\ pattern\ u\ (C\ \bar{p})
matchAux (C \overline{r})
                                  = \bar{p} \leftarrow mapM \ matchAux \ \bar{r}; \ return \ (C \ \bar{p})
matchAux u
                                  = r \leftarrow \kappa[u]; case r of undef \Rightarrow update u fixed
                                                                    | fixed \Rightarrow u' \leftarrow fresh; equality u' u; update u' u; return u'
                                                                                \Rightarrow matchAux u'
                                                                               \Rightarrow \bar{p} \leftarrow mapM \ matchAux \ \bar{r}; \ return \ (C \ \bar{p})
                                                            Fig. 3. Unification algorithm
```

- Works on *unknowns* (set of values that variables can take on during generation)
 - Difference: unknowns can be provided as inputs to generators (i.e. they have one single fixed value, but that value is unknown at compile time)
- Implemented using the State & Option monads!

FAQ

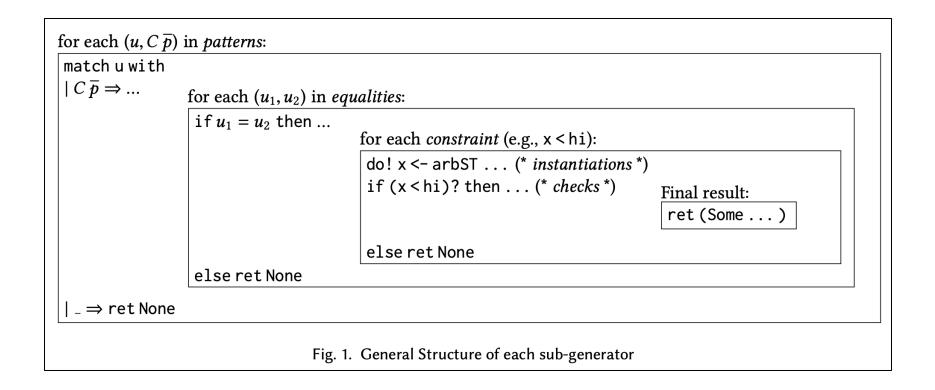
Q: Why can't we just use Rocq/Lean's internal unifier?

A: Rocq's unifier works on Rocq terms, whereas we need to unify our representation of knowledge of the state of each unknown at any particular point

Lampropoulos et al. POPL '18



General Structure of a Generator



Lampropoulos et al. POPL '18



Checker Correctness Proof (Sketch)

Soundness

\forall fuel, check (P e₁ ... e_m) fuel = Some true \Rightarrow P e₁ ... e_m

By induction on the **fuel** argument

Completeness

```
P e_1 \dots e_m

\Rightarrow \exists \text{ fuel,}

\text{check } (P e_1 \dots e_m) \text{ fuel = Some true}
```

By induction on the derivation of $P e_1 \dots e_m$

Proof for generators is more complex (requires reasoning about generators' *support*)

See §5 of Paraskevopoulou et al. (PLDI '22) for more details!



Checkers Invoking Enumerators: An Example

$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau_2 \qquad \Gamma \vdash e_2 : \tau_1}{\Gamma \vdash e_1 e_2 : \tau_2}$$

t1 doesn't appear in the conclusion of TApp, but is used in hypotheses \Rightarrow the derived checker for typing needs to enumerate **t1**



•••

Checkers Invoking Enumerators: An Example

```
TApp: ∀ Γ e1 e2 τ1 τ2,
     typing Γ e2 τ1 →
     typing Γ e1 (Fun τ1 τ2) →
     typing Γ (App e1 e2) τ2
```

t1 doesn't appear in the conclusion of TApp, but is used in hypotheses \Rightarrow the derived checker for typing needs to enumerate **t1**



Given some inductive relation P, Chamelean derives:

Generators

Gen (Option α)

(random)

Produce α 's satisfying P

Enumerators

(deterministic)

List (Option α)

(produced lazily)

Checkers

(semi-decision procedures)

Option Bool

(None = out of fuel)

Checks if $P(\alpha)$ holds



Smarter constraint ordering

Behavior of derived generator:

- Generate x such that lo < x < hi
- 2. Generate left & right subtrees



Smarter constraint ordering

- 1. Generate some unconstrained x
- 2. Generate left & right subtrees
- 3. Check that lo < x < hi This check will often fail!

(For arbitrarily generated x, Pr[lo < x < hi] is low)

