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UNIVERSITY OF TECHNOLOGY  
FACULTY OF COMPUTER SCIENCE AND ENGINEERING



## INTRODUCTION TO ARTIFICIAL INTELLIGENCE (CO3061)

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### Assignment 1

# Developing search algorithms, with a reference framework from UCB

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## 1 Introduction

**Pac-Man**, originally called Puck Man in Japan, is a 1980 maze video game developed and released by Namco for arcades. In North America, the game was released by Midway Manufacturing as part of its licensing agreement with Namco America. The player controls Pac-Man, who must eat all the dots inside an enclosed maze while avoiding four colored ghosts. Eating large flashing dots called "Power Pellets" causes the ghosts to temporarily turn blue, allowing Pac-Man to eat them for bonus points.

In this project, we try to teach pacman how to find the food in some particular algorithm (e.g, one or many foods in the maze) and may try to teach it to take as few steps as possible.



Figure 1: Game Pacman from the project UCB

The project UCB about Pacman can be divided into 2 parts: Implementing the `search.py` file (The first 4 questions about searching algorithm) and implementing the `searchAgent.py` file (The next 4 questions about Agent and implementing some heuristic function).

**Files to Edit and Submit:** We will have to fill in portions of `search.py` and `searchAgents.py` during the assignment. And we will not be allowed to modify any files.

## 2 General search algorithm

The next 4 questions from the project which are Depth-First-Search, Breadth-First-Search, Uniform-Cost-Search and Astar-Search actually have something in common. They just differ in how we choose the data-structure of the frontier or the fringe appropriately.



```
function GRAPH-SEARCH(problem, fringe) return a solution or failure
  closed ← an empty set
  fringe ← INSERT(MAKE-NODE(INITIAL-STATE[problem]), fringe)
  loop do
    if EMPTY?(fringe) then return failure
    node ← REMOVE-FIRST(fringe)
    if GOAL-TEST[problem] applied to STATE[node] succeeds
      then return SOLUTION(node)
    if STATE[node] is not in closed then
      add STATE[node] to closed
      fringe ← INSERT-ALL(EXPAND(node, problem), fringe)
```

Figure 2: A general searching algorithm

```
function EXPAND(node, problem) return a set of nodes
  successors ← the empty set
  for each <action, result> in SUCCESSOR-FN[problem](STATE[node]) do
    s ← a new NODE
    STATE[s] ← result
    PARENT-NODE[s] ← node
    ACTION[s] ← action
    PATH-COST[s] ← PATH-COST[node] + STEP-COST(node, action, s)
    DEPTH[s] ← DEPTH[node] + 1
    add s to successors
  return successors
```

Figure 3: A general expanding function for the searching algorithm

### 3 File search.py

#### 3.1 Question 1 (3 points): Finding a Fixed Food Dot using Depth First Search

```
1 fringe = Stack()
2 start = problem.getStartState()
3 fringe.push(start)
4 parent_find = {start:None} # hashmap
5 visited = {}
6
7 while not fringe.isEmpty():
8
9     currentState = fringe.pop()
10
11     visited[currentState] = 1
12     if problem.isGoalState(currentState):
13         return_path = []
14         while True:
15             if parent_find[currentState] != None:
16                 return_path.append(parent_find[currentState][1])
17                 currentState = parent_find[currentState][0]
18             else:
```

```
19         break
20
21     return list(reversed(return_path))
22
23     temp_list = problem.getSuccessors(currentState)
24     for next_state,direction,cost in temp_list:
25         if next_state in visited:
26             continue
27         else:
28             fringe.push(next_state)
29             parent_find[next_state]=(currentState,direction)
```

In question 1 about the Depth-First-Search algorithm, we will use the Stack() data-structure for the fringe. Since we want to find as deep as we can. Whenever we cannot go further or find a solution. Backtrack to the closest node that we haven't searched for the other successor.

we am also using 1 more data structure than the set visited. Because we can see that the grandchild of the child node has a path to another child, it will modify the path (also the parent of that node). So the visited-set can be used to keep nodes that have already expanded and we will not handle those nodes again.

Table 1: Result for Depth-First-Search

Layout	Total Cost	Nodes Expanded	Score
tinyMaze	10	15	500
mediumMaze	130	146	380
bigMaze	210	390	300

### 3.2 Question 2 (3 points): Finding a Fixed Food Dot using Breadth First Search

```
1 fringe = Queue()
2 start = problem.getStartState()
3 fringe.push(start)
4 parent_find = {start:None} # hashmap
5
6 while not fringe.isEmpty():
7
8     currentState = fringe.pop()
9
10    if problem.isGoalState(currentState):
11        return_path = []
12        while True:
13            if parent_find[currentState] != None:
14                return_path.append(parent_find[currentState][1])
```

```
15         currentState = parent_find[currentState][0]
16     else:
17         break
18
19     return list(reversed(return_path))
20
21     temp_list = problem.getSuccessors(currentState)
22     for next_state,direction,cost in temp_list:
23         if next_state in parent_find:
24             continue
25         else:
26             fringe.push(next_state)
27             parent_find[next_state]=(currentState,direction)
```

In question 2, with the Breadth-First-Search algorithm, we will use the Queue() data-structure for the fringe. Because we can clearly understand that. The BFS searches all the child nodes before continuing with the grand-child nodes, so using Queue() would be an excellent choice for us.

In this problem, differ from question 1, we don't use the visited-set algorithm any more. Because thinking that if the child-node expanded a grand-child node which was already in the queue() or handled. So we have to pass it because the old path will have lower cost. (Remember each step in the DFS and BFS is default 1)

Table 2: Result for Breadth-First-Search

Layout	Total Cost	Nodes Expanded	Score
tinyMaze	8	15	502
mediumMaze	68	269	442
bigMaze	210	620	300

The comparison with the DFS algorithm shows that the cost is reduced, but in return, BFS requires expanding more nodes, resulting in a lower score.

### 3.3 Question 3 (3 points): Varying the Cost Function

```
1 fringe = PriorityQueue()
2 start = problem.getStartState()
3 fringe.push((start,0),0)
4 parent_find = {start:None} # hashmap
5 while not fringe.isEmpty():
6
7     (currentState,cost_current) = fringe.pop()
8     if problem.isGoalState(currentState):
9         return_path = []
10        while True:
11            if parent_find[currentState] != None:
```

```

12         return_path.append(parent_find[currentState][1])
13         currentState = parent_find[currentState][0]
14     else:
15         break
16
17     return list(reversed(return_path))
18
19     temp_list = problem.getSuccessors(currentState)
20     for next_state,direction,cost in temp_list:
21         if next_state not in parent_find:
22             fringe.update((next_state,cost+cost_current),cost+
cost_current)
23             parent_find[next_state]=(currentState,direction,cost+
cost_current)
24         elif parent_find[next_state] == None:
25             continue
26         elif parent_find[next_state][2] > cost+cost_current:
27             fringe.update((next_state,cost+cost_current),cost+
cost_current)
28             parent_find[next_state]=(currentState,direction,cost+
cost_current)

```

In question 3, with the Uniform-Cost-Search algorithm, we will use the PriorityQueue() data-structure for the fringe. Because we need to search from the lowest cost path to the highest cost path. If we use the vector or a simple array, when a new path is inserted. We have to sort the vector or array and lead to the time complexity nearly  $n^2$  or  $n \cdot \log(n)$ . The PriorityQueue() will cost the time  $\log(n)$  whenever we need to insert a new path into the queue.

Table 3: Result for Uniform-Cost-Search

Layout	Total Cost	Nodes Expanded	Score
mediumMaze	68	269	442
mediumDottedMaze	1	186	646
mediumScaryMaze	68719479864	108	418

Seeing that the cost from the mediumDottedMaze and the mediumScaryMaze is very low and very high. Since we call the problem on the class StayEastSearchAgent, class StayWestSearchAgent. Since the first class using the function cost:  $0.5^x$  and the second class using the function cost:  $2^x$ .

```

1 class StayEastSearchAgent(SearchAgent):
2     """
3     An agent for position search with a cost function that penalizes being
    in
4     positions on the West side of the board.
5
6     The cost function for stepping into a position (x,y) is  $1/2^x$ .

```



```
7     """
8     def __init__(self):
9         self.searchFunction = search.uniformCostSearch
10        costFn = lambda pos: .5 ** pos[0]
11        self.searchType = lambda state: PositionSearchProblem(state, costFn
12        , (1, 1), None, False)
13
14    class StayWestSearchAgent(SearchAgent):
15        """
16        An agent for position search with a cost function that penalizes being
17        in
18        positions on the East side of the board.
19
20        The cost function for stepping into a position (x,y) is 2^x.
21        """
22        def __init__(self):
23            self.searchFunction = search.uniformCostSearch
24            costFn = lambda pos: 2 ** pos[0]
25            self.searchType = lambda state: PositionSearchProblem(state, costFn
26            )
```

### 3.4 Question 4 (3 points): A\* search

```
1 fringe = PriorityQueue()
2 start = problem.getStartState()
3 fringe.push((start,0),0)
4 parent_find = {start:None} # hashmap
5
6 while not fringe.isEmpty():
7
8     (currentState, cost_current) = fringe.pop()
9
10
11
12     if problem.isGoalState(currentState):
13         return_path = []
14         while True:
15             if parent_find[currentState] != None:
16                 return_path.append(parent_find[currentState][1])
17                 currentState = parent_find[currentState][0]
18             else:
19                 break
20
21         return list(reversed(return_path))
22
23     temp_list = problem.getSuccessors(currentState)
24     for next_state, direction, cost in temp_list:
25
26
```



```

27         heuristic_value = heuristic(next_state, problem)
28
29         if next_state not in parent_find:
30             fringe.update((next_state, cost+cost_current), cost+
cost_current+heuristic_value)
31             parent_find[next_state]=(currentState, direction, cost+
cost_current)
32         elif parent_find[next_state] == None:
33             continue
34         elif parent_find[next_state][2] > cost+cost_current:
35             fringe.update((next_state, cost+cost_current), cost+
cost_current+heuristic_value)
36             parent_find[next_state]=(currentState, direction, cost+
cost_current)

```

In question 4, upgrade the algorithm search UCS above, we estimate the whole length of the path using the already computed cost path plus the estimate from that point to the goal. Using the heuristic function as an argument of the function.

It evaluates nodes by combining  $g(n)$ , the cost to reach the node, and  $h(n)$ , the cost to get from the node to the goal:  $f(n) = g(n) + h(n)$ . Since  $g(n)$  gives the path cost from the start node to node  $n$ , and  $h(n)$  is the estimated cost of the cheapest path from  $n$  to the goal, we have  $f(n)$  = estimated cost of the cheapest solution through  $n$ .

Table 4: Show the different between UCS and Astar(Astar using manhattan heuristic function)

Algorithm	Layout	Total Cost	Nodes Expanded	Score
UCS	mediumMaze	68	269	442
Astar	mediumMaze	68	222	442
UCS	bigMaze	210	620	300
Astar	bigMaze	210	549	300

We can clearly see that the performance using the heuristic function will improve the algorithm in expanding fewer nodes and also lead to a better run time.

Table 5: Show the general 4 searching algorithm

Algorithm	Layout	Total Cost	Nodes Expanded	Score
DFS	bigMaze	210	390	300
BFS	bigMaze	210	620	300
UCS	bigMaze	210	620	300
Astar	bigMaze	210	549	300



## 4 File searchAgents.py

### 4.1 Question 5 (3 points): Finding All the Corners

```
1 class CornersProblem(search.SearchProblem):
2     """
3     This search problem finds paths through all four corners of a layout.
4
5     You must select a suitable state space and successor function
6     """
7
8     def __init__(self, startingGameState: pacman.GameState):
9         """
10        Stores the walls, pacman's starting position and corners.
11        """
12        self.walls = startingGameState.getWalls()
13        #self.startingPosition = startingGameState.getPacmanPosition()
14        top, right = self.walls.height-2, self.walls.width-2
15        self.corners = ((1,1), (1,top), (right, 1), (right, top))
16
17
18        # EDIT
19        self.startingPosition = (startingGameState.getPacmanPosition(), self
20        .corners)
21        # EDIT
22
23        for corner in self.corners:
24            if not startingGameState.hasFood(*corner):
25                print('Warning: no food in corner ' + str(corner))
26        self._expanded = 0 # DO NOT CHANGE; Number of search nodes expanded
27
28
29     def getStartState(self):
30         """
31        Returns the start state (in your state space, not the full Pacman
32        state
33        space)
34        """
35        """*** YOUR CODE HERE ***"""
36
37        return self.startingPosition
38        #util.raiseNotDefined()
39
40     def isGoalState(self, state: Any):
41         """
42        Returns whether this search state is a goal state of the problem.
43        """
44        """*** YOUR CODE HERE ***"""
45        size = len(list(state[1]))
```



```
45         return size == 0
46
47     #util.raiseNotDefined()
48
49     def getSuccessors(self, state: Any):
50         """
51         Returns successor states, the actions they require, and a cost of
52         1.
53
54         As noted in search.py:
55         For a given state, this should return a list of triples, (
56         successor,
57         action, stepCost), where 'successor' is a successor to the
58         current
59         state, 'action' is the action required to get there, and '
60         stepCost'
61         is the incremental cost of expanding to that successor
62         """
63
64         currentPosition,tuple_corner = state
65
66         successors = []
67         for action in [Directions.NORTH, Directions.SOUTH, Directions.EAST,
68             Directions.WEST]:
69             # Add a successor state to the successor list if the action is
70             legal
71             # Here's a code snippet for figuring out whether a new position
72             hits a wall:
73             #   x,y = currentPosition
74             #   dx, dy = Actions.directionToVector(action)
75             #   nextx, nexty = int(x + dx), int(y + dy)
76             #   hitsWall = self.walls[nextx][nexty]
77             """ YOUR CODE HERE """
78             x,y = currentPosition
79             dx,dy = Actions.directionToVector(action)
80             nextx,nexty = int(x+dx),int(y+dy)
81             hitsWall = self.walls[nextx][nexty]
82
83             if not hitsWall:
84                 new_tuple = tuple(i for i in tuple_corner if i != (nextx,
85                     nexty))
86
87                 new_state = ((nextx,nexty),new_tuple)
88                 cost = 1
89                 successors.append((new_state,action,cost))
90
91         self._expanded += 1 # DO NOT CHANGE
92         return successors
```

Now this problem is the food is not only one but 4 (each in the corner of the maze). Since the 4 search algorithm is completed above, now we have to determine the state of the search problem, the rules, the actions and the getSuccessors also. To do that keeping in mind that the initial code of the project already has the tuple of 4 corners so we will use that information to do this question. Using the position plus the tuple of 4 corners, whenever we expand a node that has that corner, remove it from the tuple. And when there is nothing left in the tuple, that is the goal of the problem.

Table 6: Result for Question 5

Layout	Total Cost	Nodes Expanded	Score
tinyCorners	28	252	512
mediumCorners	106	1966	434
bigCorners	162	7949	378

## 4.2 Question 6 (3 points): Corners Problem: Heuristic

```
1 def helper(pos, tuple_corner):
2     result = 0
3     tuple_corner = set(tuple_corner)
4
5
6     while(len(list(tuple_corner)) != 0):
7         min_distance_manhattan = float('inf')
8         corner_remove = None
9
10        for i in tuple_corner:
11            check_temp = abs(pos[0]-i[0]) + abs(pos[1]-i[1])
12
13            if check_temp < min_distance_manhattan:
14                min_distance_manhattan = check_temp
15                corner_remove = i
16
17        result += min_distance_manhattan
18        tuple_corner.remove(corner_remove)
19        pos = corner_remove
20
21    return result
22
23
24 def cornersHeuristic(state: Any, problem: CornersProblem):
25     """
26     A heuristic for the CornersProblem that you defined.
27
28     state:      The current search state
29                 (a data structure you chose in your search problem)
```



```
30
31     problem: The CornersProblem instance for this layout.
32
33     This function should always return a number that is a lower bound on
34     the
35     shortest path from the state to a goal of the problem; i.e. it should
36     be
37     admissible.
38     """
39     corners = problem.corners # These are the corner coordinates
40     walls = problem.walls # These are the walls of the maze, as a Grid (
41     game.py)
42
43     """ YOUR CODE HERE """
44     result = 0
45     pos,tuple_corner = state
46
47     return helper(pos,tuple_corner)
48
49     #return 0 # Default to trivial solution
```

To solve this question, we have to design a function that will estimate the cost from the position to the goal in the most appropriate way. In this question, because the goal isn't simply a single food like the first 4 questions anymore. It now contains 4 foods in the 4 corners. So we decided to use the distance from pos to the closest corner, and then from that corner to the other corner, and so on until there is no corner left.

### 4.3 Question 7 (3 points): Corners Problem: Eating All The Dots

Now we'll solve a hard search problem: eating all the Pacman food in as few steps as possible. The problem now will not only be 4 food in each corner, it now contains a random number of food located randomly in the maze. And we will use the command `autograder.py -q q7` to evaluate.

```
1 def compute_mst(points):
2     """
3     Using Prim Algorithm
4     """
5     if len(points) <= 1:
6         return 0
7
8     # Priority queue for Prim's algorithm
9     pq = PriorityQueue()
10    visited = set()
11    mst_cost = 0
12
13    # Start with the first point
14    start = points[0]
15    visited.add(start)
```

```
16
17     # Push initial edges to the priority queue
18     for point in points[1:]:
19         pq.push((start, point), manhattanDistance(start, point))
20
21     # Process the MST
22     while not pq.isEmpty():
23         start, end = pq.pop() # Pop the lowest-cost edge
24         #print(cost)
25         cost = manhattanDistance(start, end)
26         if end not in visited:
27             visited.add(end)
28             mst_cost += cost
29
30         # Add new edges from the newly visited point
31         for other in points:
32             if other not in visited:
33                 pq.push((end, other), manhattanDistance(end, other))
34
35     return mst_cost
36
37     pacmanPosition, foodGrid = state
38     foodList = foodGrid.asList()
39
40     if not foodList:
41         return 0 # No food left, heuristic is 0 at the goal state.
42
43     # Compute the MST cost for the food points only
44     mst_cost = compute_mst(foodList)
45
46     # Add the distance from Pacman to the closest food point
47     min_dist_to_food = min(manhattanDistance(pacmanPosition, food) for food
48                             in foodList)
49
49     return mst_cost + min_dist_to_food
```

Result:

- Expanded node = 7209 nodes
- Time = 1.86 s

#### 4.4 Question 8 (3 points): Suboptimal Search

Now the question will fill the maze with food. And our job is to make it play like a human(which is to make it come to the nearest food).

```
1 class ClosestDotSearchAgent(SearchAgent):
2     "Search for all food using a sequence of searches"
3     def registerInitialState(self, state):
```



```
4     self.actions = []
5     currentState = state
6     while(currentState.getFood().count() > 0):
7         nextPathSegment = self.findPathToClosestDot(currentState) # The
missing piece
8         self.actions += nextPathSegment
9         for action in nextPathSegment:
10             legal = currentState.getLegalActions()
11             if action not in legal:
12                 t = (str(action), str(currentState))
13                 raise Exception('findPathToClosestDot returned an
illegal move: %s!\n%s' % t)
14             currentState = currentState.generateSuccessor(0, action)
15     self.actionIndex = 0
16     print('Path found with cost %d.' % len(self.actions))
17
18     def findPathToClosestDot(self, gameState: pacman.GameState):
19         """
20         Returns a path (a list of actions) to the closest dot, starting
from
21         gameState.
22         """
23         # Here are some useful elements of the startState
24         startPosition = gameState.getPacmanPosition()
25         food = gameState.getFood()
26         walls = gameState.getWalls()
27         problem = AnyFoodSearchProblem(gameState)
28
29         """ YOUR CODE HERE """
30         from search import depthFirstSearch
31         from search import breadthFirstSearch
32         from search import uniformCostSearch
33         from search import aStarSearch
34
35         #return depthFirstSearch(problem)
36         #return breadthFirstSearch(problem)
37         #return uniformCostSearch(problem)
38         return aStarSearch(problem)
39         util.raiseNotDefined()
40
41     class AnyFoodSearchProblem(PositionSearchProblem):
42         """
43         A search problem for finding a path to any food.
44
45         This search problem is just like the PositionSearchProblem, but has a
different goal test, which you need to fill in below. The state space
and
46         successor function do not need to be changed.
47
48         """
```

```
49     The class definition above, AnyFoodSearchProblem(PositionSearchProblem)
50     ,
51     inherits the methods of the PositionSearchProblem.
52
53     You can use this search problem to help you fill in the
54     findPathToClosestDot
55     method.
56     """
57
58     def __init__(self, gameState):
59         "Stores information from the gameState.  You don't need to change
60         this."
61         # Store the food for later reference
62         self.food = gameState.getFood()
63
64         # Store info for the PositionSearchProblem (no need to change this)
65         self.walls = gameState.getWalls()
66         self.startState = gameState.getPacmanPosition()
67         self.costFn = lambda x: 1
68         self._visited, self._visitedlist, self._expanded = {}, [], 0 # DO
69         NOT CHANGE
70
71     def isGoalState(self, state: Tuple[int, int]):
72         """
73         The state is Pacman's position. Fill this in with a goal test that
74         will
75         complete the problem definition.
76         """
77         x,y = state
78
79         "*** YOUR CODE HERE ***"
80
81         #print(self.food)
82
83         return self.food[x][y]
84         util.raiseNotDefined()
```

It just simply uses which function that has been implemented from the first 4 questions. First, look at the result for each search algorithm

Table 7: Result for Question 8

Algorithm	Layout	Total Cost	Score
DFS	bigSearch	5324	-2614
BFS	bigSearch	350	2360
UCS	bigSearch	350	2360
Astar	bigSearch	350	2360

We can see that 3 algorithms BFS,UCS, Astar will all have results much better than DFS.





DFS cannot pass this question since it uses too much cost and has a negative score.

Because of the DFS algorithm, whenever Pacman eats food, it will randomly generate the child node. Example: there is a food in the next left side of the Pacman, but it looks for the right hand side first. So it will not be correct in this question (which wants us to find the closest food).

The BFS algorithm will handle this question correctly since it begins to search all the nodes closest to it before going further.

UCS and Astar are actually the same because we call the Astar function without passing the heuristic function, so Astar is also the UCS. It had the result like the BFS but the way Pacman goes to find food is not similar to BFS. We can understand this because UCS looks for the shortest path first.



## References

- [1] *Project 1: Search*, 2024