

1 Assignment 1

1. **[Points 10]** We learned two linear model - linear regression and logistic regression. Compare both methods. Can we use linear regression model to detect person face in an image? Describe your rationale behind it.

Answer: Linear regression is a linear model that is used to model a linear relationship - as an input variable is related to an output variable. Logistic regression is a linear model that is used to model a binary output - for example, given an input variable, the output variable is either true or false.

For detecting a face in an image, it might not make sense to use a linear model, unless we are trying to count the number of faces in the image. Instead, we can use a logistic regression model to output 'contains a face' or 'does not contain a face' based on the input image.

2. **[Points 15]** In logistic regression classifier, we are fitting a s-shape curve to fit the data. We are given 10 sample points with corresponding probabilities as follows, 0.34, 0.21, 0.54, 0.45, 0.60, 0.70, 0.80, 0.95, 0.99.

- (a) **[Points 7]** What is log odds? Compute log odds values for those given data points.

Answer: Odds is a ratio of the probability of success to the probability of failure. Log odds is the logarithm of the odds.

Probability	Odds	Log Odds
0.34	0.52	-0.65
0.21	0.27	-1.31
0.54	1.17	0.16
0.45	0.82	-0.2
0.6	1.5	0.41
0.7	2.33	0.85
0.8	4.0	1.39
0.95	19.0	2.94
0.99	99.0	4.6

- (b) **[Points 8]** Compute log likelihood for this given data points.
3. **[Points 15]** We know logistic regression is a binary classifier. Can we use it for multiclass classification? Provide detail rationale behind your answer and include any drawback of your proposed approaches.

Answer: Since logistic regression is a binary classifier, we can use it for multiclass classification with some considerations. First, we might consider a series of models

which classifies the input as 'A' or 'Not A'. If the input is classified as 'Not A', then we can move to the next model, which classifies the input as 'B' or 'Not B'. A problem with this kind of approach is that the accuracy can be low.

Another approach is to compare each class to each other class. We might have models such as 'A' or 'B', and 'A' or 'C'. A problem with this kind of approach is that it can be slow.

4. **[Points 10]** SoftMax is a multiclass classifier, and it converts logits to probabilities. We are given logit values 3.5, 6.1, -2.9, -1.2 for 4 classes “bus”, “truck”, “car”, “van”, respectively. Compute the probability of those given logits and classify it.
5. **[Points 25]** We are designing a 2-layer feedforward neural network. Our input features are 3-dimensional. The first hidden layer has 5 neurons with sigmoid activation function. Final layer contains two neurons with Relu activation function. Assume that given inputs are x_1, x_2, x_3 and hidden layer weights are w_{ij}^l , where $l \in 1, 2$ is the layer number and $i \in 1, 2, 3$ is the number of inputs. $j \in 1, 2, 3, 4, 5$ indicates the number of neurons. b_j^l indicates bias for corresponding layers and neurons. For any inconsistency with the notation given, you can modify it and mentioned the notation scheme in your answer.
 - (a) **[Points 10]** Draw a complete diagram of this feed forward neural network showing all individual weights, biases.
 - (b) **[Points 10]** Show forward computation for this given input x_1, x_2, x_3 . Show detailed equations for each computing unit (neuron) for each layer.