**HOMEWORK #3**

**Part 1: Translating English into Formal Logic**   
For the first part, you will translate the sentences below into first order logic. These came from the famous mathematician (and more famous writer) Lewis Carroll. You might want to check out the puzzles at the [Lewis Carrol Puzzles website](http://www.math.hawaii.edu/~hile/math100/logice.htm) to see how some of them are approached. Remember that you can use any of the logical equivalence rules (slide 31 in the Logical Agents lecture). In particular, you might find contraposition useful.

No kitten, that loves fish, is unteachable. (a)

No kitten without a tail will play with a gorilla. (b)

Kittens with whiskers always love fish. (c)

No teachable kitten has green eyes. (d)

No kittens have tails unless they have whiskers. (e)

**Solution**:

1. ­­¬∃x [Is(x, Kitten) ^ Loves(x, Fish) ^ ¬Teachable(x)]

“There is not a kitten that loves fish and is not teachable"

1. ­­¬∃x [Is(x, Kitten) ^ ¬Has(x, Tail) ^ PlayWith(x, Gorilla)]

“There is not a kitten that does not have a tail and will play with a gorilla”

1. ∀x [Is(x, Kitten) ^ HasWhiskers(x) => Loves(x, Fish)]

“All kittens that have whiskers love fish”

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**Part 2: Inference in First Order Logic**   
Let's say we also know:

My kitten who has green eyes does not love fish.

Using three approaches, try to prove the following:

My kitten is unteachable.

**A. Forward Chaining.**Use forward chaining to try to prove the previous assertion. Remember, that in order to use forward (or backward) chaining, the knowledge base must be in Horn form. So start by translating your KB into Horn clauses. Show your work in doing the translation, and then as you do the inference, show the logical progression so I can see how you did your reasoning.

**Solution**:

**B. Backward Chaining.**Now use backward chaining to try to prove the previous assertion. You can use your KB from the previous part, but I do want to see all your steps in doing the backward chaining.  
  
**Solution**:

**C. Resolution.**Finally, use resolution to try to prove the assertion. Remember, that in order to use resolution, your KB must be in conjunctive normal form. So start by translating your KB into CNF. Show me all your work in this step. Then use resolution and show me all of your steps there, also.

**Solution**: