## ĐẠI HỌC QUỐC GIA TP. HÒ CHÍ MINH TRƯỜNG ĐẠI HỌC CÔNG NGHỆ THÔNG TIN ++++++



BÁO CÁO THỰC

HÀNH

MÔN CS106 – TRÍ TUỆ NHÂN TẠO

**BT3 - Solving Knapsack Problems Using Google OR Tools** 

Giảng viên hướng dẫn: Thầy Lương Ngọc Hoàng

Sinh viên thực hiện: Trần Ngọc Thiện

MSSV: 21521465

TP. HÒ CHÍ MINH, Tháng 3 Năm 2024

| NHẬN XÉT CỦA GIÁNG VIÊN |
|-------------------------|
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
|                         |
| TPHCM, Ngày Tháng Năm . |
| Người nhận xét          |
|                         |

CS106.021 2

(Ký tên)

# Mục lục

| Quá ti | rình thực hiện                | 4  |
|--------|-------------------------------|----|
| Kết qu | ıả                            | 4  |
| 00.    | Uncorrelated                  |    |
| 01.    | WeaklyCorrelated              | 4  |
| 02.    | StronglyCorrelated            | 5  |
| 03.    | InverseStronglyCorrelated     | 5  |
| 04.    | AlmostStronglyCorrelated      | 6  |
| 05.    | SubsetSum                     | 7  |
| 06.    | UncorrelatedWithSimilarWeight | 7  |
| 07.    | SpannerUncorrelated           | 8  |
| 08.    | SpannerWeaklyCorrelated       | 8  |
| 09.    | SpannerStronglyCorrelated     | 9  |
| 10.    | MultipleStronglyCorrelated    | 10 |
| 11.    | ProfitCeiling                 | 10 |
| 12.    | Circle                        | 11 |

## Quá trình thực hiện

- Đặt mốc chi phí là tối đa 120 giây cho mỗi lần chạy.
- Trong mỗi nhóm testcase, chọn ngẫu nhiên 1 testcase ứng với mỗi kích thước.

## Kết quả

#### 00.Uncorrelated

| File path                                   | Problem | Max     | Total   | Total   | Runtime  |
|---|---------|---------|---------|---------|----------|
|   | size    | weight  | value   | weight  |          |
| testcase\kplib-                             | 50      | 13335   | 19473   | 13322   | 0        |
| master\00Uncorrelated\n00050\R01000\s081.kp |         |         |         |         |          |
| testcase\kplib-                             | 100     | 26464   | 37248   | 26450   | 0        |
| master\00Uncorrelated\n00100\R01000\s014.kp |         |         |         |         |          |
| testcase\kplib-                             | 200     | 49551   | 81680   | 49545   | 0        |
| master\00Uncorrelated\n00200\R01000\s003.kp |         |         |         |         |          |
| testcase\kplib-                             | 500     | 123596  | 209767  | 123594  | 0        |
| master\00Uncorrelated\n00500\R01000\s094.kp |         |         |         |         |          |
| testcase\kplib-                             | 1000    | 246819  | 398394  | 246812  | 0.01718  |
| master\00Uncorrelated\n01000\R01000\s035.kp |         |         |         |         |          |
| testcase\kplib-                             | 2000    | 496783  | 822269  | 496780  | 0.015942 |
| master\00Uncorrelated\n02000\R01000\s031.kp |         |         |         |         |          |
| testcase\kplib-                             | 5000    | 1233887 | 2034212 | 1233885 | 0.067444 |
| master\00Uncorrelated\n05000\R01000\s028.kp |         |         |         |         |          |
| testcase\kplib-                             | 10000   | 2469230 | 4032422 | 2469230 | 0.31084  |
| master\00Uncorrelated\n10000\R01000\s017.kp |         |         |         |         |          |

• Tìm ra lời giải chắc chắn tối ưu cho tất cả testcase

#### 01. WeaklyCorrelated

| File path                                       | Problem | Max    | Total | Total  | Runtime |
|---|---------|--------|-------|--------|---------|
|   | size    | weight | value | weight |         |
| testcase\kplib-                                 | 50      | 11888  | 13175 | 11885  | 0       |
| master\01WeaklyCorrelated\n00050\R01000\s094.kp |         |        |       |        |         |
| testcase\kplib-                                 | 100     | 24322  | 26297 | 24319  | 0       |
| master\01WeaklyCorrelated\n00100\R01000\s013.kp |         |        |       |        |         |
| testcase\kplib-                                 | 200     | 48881  | 54298 | 48881  | 0       |

| master\01WeaklyCorrelated\n00200\R01000\s086.kp      |       |         |         |         |          |
|--|-------|---------|---------|---------|----------|
| testcase\kplib-                                      | 500   | 129518  | 142384  | 129516  | 0.015621 |
| master\01WeaklyCorrelated\n00500\R01000\s094.kp      |       |         |         |         |          |
| testcase\kplib-                                      | 1000  | 245164  | 271373  | 245163  | 0.004618 |
| master\01WeaklyCorrelated\n01000\R01000\s069.kp      |       |         |         |         |          |
| testcase\kplib-                                      | 2000  | 493039  | 545286  | 493039  | 0.009233 |
| master\01WeaklyCorrelated\n02000\R01000\s011.kp      |       |         |         |         |          |
| testcase\kplib-                                      | 5000  | 1225116 | 1354119 | 1225116 | 0.092209 |
| master\01WeaklyCorrelated\n05000\R01000\s075.kp      |       |         |         |         |          |
| testcase\kplib-                                      | 10000 | 2485622 | 2747406 | 2485622 | 0.299428 |
| $master \\ lem:lem:lem:lem:lem:lem:lem:lem:lem:lem:$ |       |         |         |         |          |

Tìm ra lời giải chắc chắn tối ưu cho tất cả testcase

#### 02. StronglyCorrelated

| File path   | Problem | Max     | Total   | Total   | Runtime  |
|---|---------|---------|---------|---------|----------|
|   | size    | weight  | value   | weight  |          |
| testcase\kplib-   | 50      | 12263   | 15763   | 12263   | 0        |
| master\02StronglyCorrelated\n00050\R01000\s004.kp                         |         |         |         |         |          |
| testcase\kplib-   | 100     | 26811   | 33711   | 26811   | 0.149914 |
| master\02StronglyCorrelated\n00100\R01000\s003.kp                         |         |         |         |         |          |
| testcase\kplib-   | 200     | 49817   | 63917   | 49817   | 120.0431 |
| master\02StronglyCorrelated\n00200\R01000\s011.kp                         |         |         |         |         |          |
| testcase\kplib-   | 500     | 128606  | 163206  | 128606  | 120.0339 |
| master\02StronglyCorrelated\n00500\R01000\s027.kp                         |         |         |         |         |          |
| testcase\kplib-   | 1000    | 242756  | 313119  | 242519  | 120.0459 |
| master\02StronglyCorrelated\n01000\R01000\s029.kp                         |         |         |         |         |          |
| testcase\kplib-   | 2000    | 494251  | 635151  | 494251  | 120.0243 |
| master\02StronglyCorrelated\n02000\R01000\s064.kp                         |         |         |         |         |          |
| testcase\kplib-   | 5000    | 1220893 | 1572869 | 1220469 | 120.0731 |
| master\02StronglyCorrelated\n05000\R01000\s077.kp                         |         |         |         |         |          |
| testcase\kplib-   | 10000   | 2480159 | 3184177 | 2479877 | 120.3268 |
| $master \ \ O2S trongly Correlated \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |

<sup>•</sup> Chỉ tìm được lời giải chắc chắn tối ưu cho 2 testcase có kích thước 50 và 100

## ${\bf 03.}\ Inverse Strongly Correlated$

| File path | Problem | Max    | Total | Total  | Runtime |
|-----------|---------|--------|-------|--------|---------|
|           | size    | weight | value | weight |         |

| testcase\kplib-  | 50    | 12930   | 11430   | 12930   | 0.018454 |
|--|-------|---------|---------|---------|----------|
| master\03InverseStronglyCorrelated\n00050\R01000\s071.kp |       |         |         |         |          |
| testcase\kplib-  | 100   | 28170   | 24970   | 28170   | 12.21254 |
| master\03InverseStronglyCorrelated\n00100\R01000\s025.kp |       |         |         |         |          |
| testcase\kplib-  | 200   | 63271   | 56671   | 63271   | 120.0443 |
| master\03InverseStronglyCorrelated\n00200\R01000\s091.kp |       |         |         |         |          |
| testcase\kplib-  | 500   | 155169  | 138642  | 155042  | 121.9788 |
| master\03InverseStronglyCorrelated\n00500\R01000\s083.kp |       |         |         |         |          |
| testcase\kplib-  | 1000  | 297453  | 265691  | 296991  | 120.5593 |
| master\03InverseStronglyCorrelated\n01000\R01000\s089.kp |       |         |         |         |          |
| testcase\kplib-  | 2000  | 593015  | 529919  | 592719  | 120.0464 |
| master\03InverseStronglyCorrelated\n02000\R01000\s069.kp |       |         |         |         |          |
| testcase\kplib-  | 5000  | 1492281 | 1333928 | 1492128 | 120.0723 |
| master\03InverseStronglyCorrelated\n05000\R01000\s053.kp |       |         |         |         |          |
| testcase\kplib-  | 10000 | 2966188 | 2652217 | 2966117 | 120.1523 |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$           |       |         |         |         |          |

• Chỉ tìm được lời giải chắc chắn tối ưu cho 2 testcase có kích thước 50 và 100

## 04. AlmostStronglyCorrelated

| File path   | Problem | Max     | Total   | Total   | Runtime  |
|---|---------|---------|---------|---------|----------|
|   | size    | weight  | value   | weight  |          |
| testcase\kplib-   | 50      | 12889   | 16292   | 12889   | 0        |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$          |         |         |         |         |          |
| testcase\kplib-   | 100     | 25741   | 32654   | 25741   | 0.244647 |
| master\04AlmostStronglyCorrelated\n00100\R01000\s075.kp |         |         |         |         |          |
| testcase\kplib-   | 200     | 47486   | 61694   | 47484   | 0        |
| master\04AlmostStronglyCorrelated\n00200\R01000\s035.kp |         |         |         |         |          |
| testcase\kplib-   | 500     | 127278  | 162154  | 127278  | 120.0145 |
| master\04AlmostStronglyCorrelated\n00500\R01000\s000.kp |         |         |         |         |          |
| testcase\kplib-   | 1000    | 248678  | 319110  | 248678  | 120.028  |
| master\04AlmostStronglyCorrelated\n01000\R01000\s097.kp |         |         |         |         |          |
| testcase\kplib-   | 2000    | 490184  | 631421  | 489843  | 120.0349 |
| master\04AlmostStronglyCorrelated\n02000\R01000\s020.kp |         |         |         |         |          |
| testcase\kplib-   | 5000    | 1237047 | 1589318 | 1237047 | 6.847284 |
| master\04AlmostStronglyCorrelated\n05000\R01000\s089.kp |         |         |         |         |          |
| testcase\kplib-   | 10000   | 2485622 | 3188670 | 2485622 | 120.3157 |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$          |         |         |         |         |          |

• Tìm được lời giải chắc chắn tối ưu cho 4 testcase có kích thước 50; 100; 200; 5000

CS106.021

#### 05. SubsetSum

| File path  | Problem | Max     | Total   | Total   | Runtime  |
|--|---------|---------|---------|---------|----------|
|  | size    | weight  | value   | weight  |          |
| testcase\kplib-                                      | 50      | 12828   | 12828   | 12828   | 0.00368  |
| $master \ 05 Subset Sum \ n00050 \ R01000 \ s043.kp$ |         |         |         |         |          |
| testcase\kplib-                                      | 100     | 24868   | 24868   | 24868   | 0        |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$       |         |         |         |         |          |
| testcase\kplib-                                      | 200     | 45641   | 45641   | 45641   | 0.000999 |
| master\05SubsetSum\n00200\R01000\s019.kp             |         |         |         |         |          |
| testcase\kplib-                                      | 500     | 128606  | 128606  | 128606  | 0.001684 |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$       |         |         |         |         |          |
| testcase\kplib-                                      | 1000    | 248678  | 248678  | 248678  | 0.002572 |
| master\05SubsetSum\n01000\R01000\s097.kp             |         |         |         |         |          |
| testcase\kplib-                                      | 2000    | 491101  | 491101  | 491101  | 0.012677 |
| master\05SubsetSum\n02000\R01000\s043.kp             |         |         |         |         |          |
| testcase\kplib-                                      | 5000    | 1231397 | 1231397 | 1231397 | 0.045912 |
| master\05SubsetSum\n05000\R01000\s013.kp             |         |         |         |         |          |
| testcase\kplib-                                      | 10000   | 2462668 | 2462668 | 2462668 | 0.145541 |
| $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$       |         |         |         |         |          |

Tìm ra lời giải chắc chắn tối ưu cho tất cả testcase

## ${\bf 06.\ Uncorrelated With Similar Weight}$

| File path   | Proble | Max    | Total | Total  | Runti  |
|---|--------|--------|-------|--------|--------|
|   | m size | weight | value | weight | me     |
| testcase\kplib-                                     | 50     | 247654 | 15837 | 240128 | 0.0045 |
| master\06UncorrelatedWithSimilarWeights\n00050\R010 |        | 2      |       | 9      | 87     |
| 00\s048.kp  |        |        |       |        |        |
| testcase\kplib-                                     | 100    | 495307 | 35206 | 490252 | 0.0478 |
| master\06UncorrelatedWithSimilarWeights\n00100\R010 |        | 6      |       | 5      | 31     |
| 00\s012.kp  |        |        |       |        |        |
| testcase\kplib-                                     | 200    | 990632 | 75694 | 990514 | 0      |
| master\06UncorrelatedWithSimilarWeights\n00200\R010 |        | 2      |       | 8      |        |
| 00\s045.kp  |        |        |       |        |        |
| testcase\kplib-                                     | 500    | 247649 | 18175 | 247127 | 120.03 |
| master\06UncorrelatedWithSimilarWeights\n00500\R010 |        | 70     | 8     | 33     | 44     |
| 00\s044.kp  |        |        |       |        |        |
| testcase\kplib-                                     | 1000   | 495290 | 37222 | 495235 | 0.3414 |
| master\06UncorrelatedWithSimilarWeights\n01000\R010 |        | 80     | 2     | 72     | 79     |

| 00\s077.kp  |       |         |       |         |        |
|---|-------|---------|-------|---------|--------|
| testcase\kplib-                                     | 2000  | 990595  | 74726 | 990493  | 120.02 |
| master\06UncorrelatedWithSimilarWeights\n02000\R010 |       | 96      | 1     | 94      | 98     |
| 00\s033.kp  |       |         |       |         |        |
| testcase\kplib-                                     | 5000  | 2.48E+0 | 18619 | 2.48E+0 | 120.09 |
| master\06UncorrelatedWithSimilarWeights\n05000\R010 |       | 8       | 06    | 8       | 14     |
| 00\s005.kp  |       |         |       |         |        |
| testcase\kplib-                                     | 10000 | 4.95E+0 | 37335 | 4.95E+0 | 120.23 |
| master\06UncorrelatedWithSimilarWeights\n10000\R010 |       | 8       | 39    | 8       | 99     |
| 00\s093.kp  |       |         |       |         |        |

<sup>•</sup> Tìm được lời giải chắc chắn tối ưu cho 4 testcase có kích thước 50; 100; 200; 1000

## 07. SpannerUncorrelated

| testcase\kplib-<br>master\07SpannerUncorrelated\n00050\R01000\s081.kp         50         6076         6777         6075         0.009973           testcase\kplib-<br>master\07SpannerUncorrelated\n00100\R01000\s014.kp         100         19750         14616         19720         120.0302           testcase\kplib-<br>master\07SpannerUncorrelated\n00200\R01000\s003.kp         200         24625         22344         24624         120.0288           testcase\kplib-<br>master\07SpannerUncorrelated\n00500\R01000\s094.kp         500         43763         72200         43748         126.8287           testcase\kplib-<br>master\07SpannerUncorrelated\n01000\R01000\s035.kp         1000         199191         173615         199182         120.0665           master\07SpannerUncorrelated\n01000\R01000\s031.kp         2000         265680         42850         265670         122.0943           testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s028.kp         5000         482811         198036         482800         120.1127           testcase\kplib-<br>master\07SpannerUncorrelated\n05000\R01000\s028.kp         10000         1545201         2414869         1545128         120.2763 | File path                                      | Problem | Max     | Total   | Total   | Runtime  |
|---|--|---------|---------|---------|---------|----------|
| master\07SpannerUncorrelated\n00050\R01000\s081.kp         100         19750         14616         19720         120.0302           master\07SpannerUncorrelated\n00100\R01000\s014.kp         200         24625         22344         24624         120.0288           master\07SpannerUncorrelated\n00200\R01000\s003.kp         500         43763         72200         43748         126.8287           master\07SpannerUncorrelated\n00500\R01000\s094.kp         1000         199191         173615         199182         120.0665           master\07SpannerUncorrelated\n01000\R01000\s035.kp         2000         265680         42850         265670         122.0943           testcase\kplib- master\07SpannerUncorrelated\n02000\R01000\s031.kp         5000         482811         198036         482800         120.1127           master\07SpannerUncorrelated\n05000\R01000\s028.kp         10000         1545201         2414869         1545128         120.2763  |  | size    | weight  | value   | weight  |          |
| testcase\kplib- master\07SpannerUncorrelated\n00100\k01000\s014.kp  testcase\kplib- master\07SpannerUncorrelated\n00200\k01000\s003.kp  testcase\kplib- master\07SpannerUncorrelated\n00200\k01000\s003.kp  testcase\kplib- master\07SpannerUncorrelated\n00500\k01000\s094.kp  testcase\kplib- master\07SpannerUncorrelated\n01000\k01000\s094.kp  testcase\kplib- master\07SpannerUncorrelated\n01000\k01000\s035.kp  testcase\kplib- master\07SpannerUncorrelated\n01000\k01000\s031.kp  testcase\kplib- master\07SpannerUncorrelated\n02000\k01000\s031.kp  testcase\kplib- master\07SpannerUncorrelated\n02000\k01000\s031.kp  testcase\kplib- master\07SpannerUncorrelated\n02000\k01000\s031.kp  testcase\kplib- master\07SpannerUncorrelated\n05000\k01000\s038.kp  testcase\kplib- master\07SpannerUncorrelated\n05000\k01000\s028.kp  testcase\kplib- 10000 1545201 2414869 1545128 120.2763  | testcase\kplib-                                | 50      | 6076    | 6777    | 6075    | 0.009973 |
| master\07SpannerUncorrelated\n00100\R01000\s014.kp         200         24625         22344         24624         120.0288           master\07SpannerUncorrelated\n00200\R01000\s003.kp         500         43763         72200         43748         126.8287           testcase\kplib- master\07SpannerUncorrelated\n00500\R01000\s094.kp         1000         199191         173615         199182         120.0665           testcase\kplib- master\07SpannerUncorrelated\n01000\R01000\s035.kp         2000         265680         42850         265670         122.0943           testcase\kplib- master\07SpannerUncorrelated\n02000\R01000\s031.kp         5000         482811         198036         482800         120.1127           master\07SpannerUncorrelated\n05000\R01000\s028.kp         10000         1545201         2414869         1545128         120.2763  | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib-<br>master\07SpannerUncorrelated\n00200\R01000\s003.kp       200       24625       22344       24624       120.0288         testcase\kplib-<br>master\07SpannerUncorrelated\n00500\R01000\s094.kp       500       43763       72200       43748       126.8287         testcase\kplib-<br>master\07SpannerUncorrelated\n01000\R01000\s035.kp       1000       199191       173615       199182       120.0665         testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s031.kp       2000       265680       42850       265670       122.0943         testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s028.kp       5000       482811       198036       482800       120.1127         testcase\kplib-<br>testcase\kplib-       10000       1545201       2414869       1545128       120.2763   | testcase\kplib-                                | 100     | 19750   | 14616   | 19720   | 120.0302 |
| master\07SpannerUncorrelated\n00200\R01000\s003.kp         500         43763         72200         43748         126.8287           master\07SpannerUncorrelated\n00500\R01000\s094.kp         1000         199191         173615         199182         120.0665           master\07SpannerUncorrelated\n01000\R01000\s035.kp         2000         265680         42850         265670         122.0943           master\07SpannerUncorrelated\n02000\R01000\s031.kp         5000         482811         198036         482800         120.1127           master\07SpannerUncorrelated\n05000\R01000\s028.kp         10000         1545201         2414869         1545128         120.2763  | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib-<br>master\07SpannerUncorrelated\n00500\R01000\s094.kp         500         43763         72200         43748         126.8287           testcase\kplib-<br>master\07SpannerUncorrelated\n01000\R01000\s035.kp         1000         199191         173615         199182         120.0665           testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s031.kp         2000         265680         42850         265670         122.0943           testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s028.kp         5000         482811         198036         482800         120.1127           testcase\kplib-<br>testcase\kplib-         10000         1545201         2414869         1545128         120.2763  | testcase\kplib-                                | 200     | 24625   | 22344   | 24624   | 120.0288 |
| master\07SpannerUncorrelated\n00500\R01000\s094.kp       1000       199191       173615       199182       120.0665         testcase\kplib-<br>master\07SpannerUncorrelated\n01000\R01000\s035.kp       2000       265680       42850       265670       122.0943         testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s031.kp       5000       482811       198036       482800       120.1127         testcase\kplib-<br>master\07SpannerUncorrelated\n05000\R01000\s028.kp       10000       1545201       2414869       1545128       120.2763   | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib-<br>master\07SpannerUncorrelated\n01000\R01000\s035.kp       1000       199191       173615       199182       120.0665         testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s031.kp       2000       265680       42850       265670       122.0943         testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s028.kp       5000       482811       198036       482800       120.1127         testcase\kplib-<br>testcase\kplib-       10000       1545201       2414869       1545128       120.2763   | testcase\kplib-                                | 500     | 43763   | 72200   | 43748   | 126.8287 |
| master\07SpannerUncorrelated\n01000\R01000\s035.kp       2000       265680       42850       265670       122.0943         testcase\kplib- master\07SpannerUncorrelated\n02000\R01000\s031.kp       5000       482811       198036       482800       120.1127         testcase\kplib- master\07SpannerUncorrelated\n05000\R01000\s028.kp       10000       1545201       2414869       1545128       120.2763  | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib-<br>master\07SpannerUncorrelated\n02000\R01000\s031.kp       2000       265680       42850       265670       122.0943         testcase\kplib-<br>master\07SpannerUncorrelated\n05000\R01000\s028.kp       5000       482811       198036       482800       120.1127         testcase\kplib-<br>testcase\kplib-       10000       1545201       2414869       1545128       120.2763  | testcase\kplib-                                | 1000    | 199191  | 173615  | 199182  | 120.0665 |
| master\07SpannerUncorrelated\n02000\R01000\s031.kp       5000       482811       198036       482800       120.1127         testcase\kplib-       10000       1545201       2414869       1545128       120.2763  | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib- 5000 482811 198036 482800 120.1127 master\07SpannerUncorrelated\n05000\R01000\s028.kp testcase\kplib- 10000 1545201 2414869 1545128 120.2763  | testcase\kplib-                                | 2000    | 265680  | 42850   | 265670  | 122.0943 |
| master\07SpannerUncorrelated\n05000\R01000\s028.kp       10000       1545201       2414869       1545128       120.2763   | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |
| testcase\kplib- 10000 1545201 2414869 1545128 120.2763  | testcase\kplib-                                | 5000    | 482811  | 198036  | 482800  | 120.1127 |
| ' 1   | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         | _       |         |          |
| master\07SpannerUncorrelated\n10000\R01000\s017.kp  | testcase\kplib-                                | 10000   | 1545201 | 2414869 | 1545128 | 120.2763 |
| master to repaired entertained in to  | $master \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |

<sup>•</sup> Chỉ tìm được lời giải chắc chắn tối ưu cho testcase có kích thước 50

### 08. SpannerWeaklyCorrelated

| File path       | Problem size | Max<br>weight | Total<br>value | Total<br>weight | Runtime  |
|-----------------|--------------|---------------|----------------|-----------------|----------|
| testcase\kplib- | 50           | 6178          | 10988          | 6164            | 0.011968 |

| master\08SpannerWeaklyCorrelated\n00050\R01000\s081.kp |       |         |         |         |          |
|--|-------|---------|---------|---------|----------|
| testcase\kplib-  | 100   | 9824    | 37952   | 9819    | 120.0503 |
| master\08SpannerWeaklyCorrelated\n00100\R01000\s014.kp |       |         |         |         |          |
| testcase\kplib-  | 200   | 19807   | 40005   | 19775   | 119.7033 |
| master\08SpannerWeaklyCorrelated\n00200\R01000\s003.kp |       |         |         |         |          |
| testcase\kplib-  | 500   | 41977   | 88122   | 41969   | 120.021  |
| master\08SpannerWeaklyCorrelated\n00500\R01000\s094.kp |       |         |         |         |          |
| testcase\kplib-  | 1000  | 158826  | 360726  | 158820  | 120.023  |
| master\08SpannerWeaklyCorrelated\n01000\R01000\s035.kp |       |         |         |         |          |
| testcase\kplib-  | 2000  | 30321   | 406972  | 30319   | 120.0367 |
| master\08SpannerWeaklyCorrelated\n02000\R01000\s031.kp |       |         |         |         |          |
| testcase\kplib-  | 5000  | 143186  | 932456  | 143178  | 120.0619 |
| master\08SpannerWeaklyCorrelated\n05000\R01000\s028.kp |       |         |         |         |          |
| testcase\kplib-  | 10000 | 1617013 | 4171773 | 1617006 | 120.2716 |
| master\08SpannerWeaklyCorrelated\n10000\R01000\s017.kp |       |         |         |         |          |

<sup>•</sup> Tìm được lời giải chắc chắn tối ưu cho 2 testcase có kích thước 50 và 200

## 09. SpannerStronglyCorrelated

| File path   | Problem | Max     | Total   | Total   | Runtime  |
|---|---------|---------|---------|---------|----------|
|   | size    | weight  | value   | weight  |          |
| testcase\kplib-   | 50      | 4230    | 22222   | 4222    | 93.53636 |
| master\09SpannerStronglyCorrelated\n00050\R01000\s094.kp                            |         |         |         |         |          |
| testcase\kplib-   | 100     | 10370   | 40746   | 10346   | 116.3455 |
| master\09SpannerStronglyCorrelated\n00100\R01000\s013.kp                            |         |         |         |         |          |
| testcase\kplib-   | 200     | 18971   | 98654   | 18954   | 120.0616 |
| master\09SpannerStronglyCorrelated\n00200\R01000\s086.kp                            |         |         |         |         |          |
| testcase\kplib-   | 500     | 41953   | 232320  | 41920   | 120.0254 |
| master\09SpannerStronglyCorrelated\n00500\R01000\s094.kp                            |         |         |         |         |          |
| testcase\kplib-   | 1000    | 94391   | 483084  | 94384   | 120.0346 |
| master\09SpannerStronglyCorrelated\n01000\R01000\s069.kp                            |         |         |         |         |          |
| testcase\kplib-   | 2000    | 245896  | 833361  | 245861  | 120.0296 |
| master\09SpannerStronglyCorrelated\n02000\R01000\s011.kp                            |         |         |         |         |          |
| testcase\kplib-   | 5000    | 541956  | 1929455 | 541955  | 120.0514 |
| master\09SpannerStronglyCorrelated\n05000\R01000\s075.kp                            |         |         |         |         |          |
| testcase\kplib-   | 10000   | 1273941 | 5212314 | 1273914 | 120.2806 |
| $master \ \ O9 Spanner Strongly Correlated \ \ \ 10000 \ \ \ \ \ \ \ \ \ \ \ \ \ \$ |         |         |         |         |          |

<sup>•</sup> Tìm được lời giải chắc chắn tối ưu cho 2 testcase có kích thước 50; 100

## 10. MultipleStronglyCorrelated

| File path   | Problem | Max     | Total   | Total   | Runtime  |
|---|---------|---------|---------|---------|----------|
|   | size    | weight  | value   | weight  |          |
| testcase\kplib-   | 50      | 12258   | 20450   | 12250   | 0        |
| master\10MultipleStronglyCorrelated\n00050\R01000\s004.kp |         |         |         |         |          |
| testcase\kplib-   | 100     | 26808   | 41805   | 26805   | 0        |
| master\10MultipleStronglyCorrelated\n00100\R01000\s003.kp |         |         |         |         |          |
| testcase\kplib-   | 200     | 49812   | 80908   | 49808   | 0.001248 |
| master\10MultipleStronglyCorrelated\n00200\R01000\s011.kp |         |         |         |         |          |
| testcase\kplib-   | 500     | 128604  | 205104  | 128604  | 120.3484 |
| master\10MultipleStronglyCorrelated\n00500\R01000\s027.kp |         |         |         |         |          |
| testcase\kplib-   | 1000    | 242754  | 398754  | 242754  | 120.0261 |
| master\10MultipleStronglyCorrelated\n01000\R01000\s029.kp |         |         |         |         |          |
| testcase\kplib-   | 2000    | 494250  | 802850  | 494250  | 120.0435 |
| master\10MultipleStronglyCorrelated\n02000\R01000\s064.kp |         |         |         |         |          |
| testcase\kplib-   | 5000    | 1220892 | 1994892 | 1220892 | 120.1189 |
| master\10MultipleStronglyCorrelated\n05000\R01000\s077.kp |         |         |         |         |          |
| testcase\kplib-   | 10000   | 2480154 | 4030439 | 2480139 | 120.4751 |
| master\10MultipleStronglyCorrelated\n10000\R01000\s003.kp |         |         |         |         |          |

<sup>•</sup> Tìm được lời giải chắc chắn tối ưu cho 3 testcase có kích thước 50; 100; 200

## 11. ProfitCeiling

| File path                                    | Problem | Max     | Total   | Total   | Runtime  |
|--|---------|---------|---------|---------|----------|
|  | size    | weight  | value   | weight  |          |
| testcase\kplib-                              | 50      | 10454   | 10446   | 10453   | 0.004988 |
| master\11ProfitCeiling\n00050\R01000\s071.kp |         |         |         |         |          |
| testcase\kplib-                              | 100     | 23220   | 23205   | 23220   | 0.018113 |
| master\11ProfitCeiling\n00100\R01000\s025.kp |         |         |         |         |          |
| testcase\kplib-                              | 200     | 53370   | 53340   | 53370   | 3.943108 |
| master\11ProfitCeiling\n00200\R01000\s091.kp |         |         |         |         |          |
| testcase\kplib-                              | 500     | 130417  | 130371  | 130415  | 120.1193 |
| master\11ProfitCeiling\n00500\R01000\s083.kp |         |         |         |         |          |
| testcase\kplib-                              | 1000    | 247948  | 247854  | 247946  | 120.041  |
| master\11ProfitCeiling\n01000\R01000\s089.kp |         |         |         |         |          |
| testcase\kplib-                              | 2000    | 494005  | 493821  | 494004  | 120.0301 |
| master\11ProfitCeiling\n02000\R01000\s069.kp |         |         |         |         |          |
| testcase\kplib-                              | 5000    | 1244756 | 1244301 | 1244755 | 120.0555 |
| master\11ProfitCeiling\n05000\R01000\s053.kp |         |         |         |         |          |

| testcase\kplib-                              | 10000 | 2471138 | 2470188 | 2471137 | 120.2981 |
|--|-------|---------|---------|---------|----------|
| master\11ProfitCeiling\n10000\R01000\s028.kp |       |         |         |         |          |

• Tìm được lời giải chắc chắn tối ưu cho 3 testcase có kích thước 50; 100; 200

#### 12. Circle

| File path                             | Problem | Max     | Total    | Total   | Runtime  |
|---------------------------------------|---------|---------|----------|---------|----------|
|                                       | size    | weight  | value    | weight  |          |
| testcase\kplib-                       | 50      | 12889   | 271584   | 12889   | 0.001996 |
| master\12Circle\n00050\R01000\s057.kp |         |         |          |         |          |
| testcase\kplib-                       | 100     | 25741   | 542386   | 25741   | 120.242  |
| master\12Circle\n00100\R01000\s075.kp |         |         |          |         |          |
| testcase\kplib-                       | 200     | 47486   | 1000572  | 47486   | 0.008444 |
| master\12Circle\n00200\R01000\s035.kp |         |         |          |         |          |
| testcase\kplib-                       | 500     | 127278  | 2681868  | 127278  | 120.2467 |
| master\12Circle\n00500\R01000\s000.kp |         |         |          |         |          |
| testcase\kplib-                       | 1000    | 248678  | 5239876  | 248678  | 120.0385 |
| master\12Circle\n01000\R01000\s097.kp |         |         |          |         |          |
| testcase\kplib-                       | 2000    | 490184  | 10328628 | 490184  | 120.0165 |
| master\12Circle\n02000\R01000\s020.kp |         |         |          |         |          |
| testcase\kplib-                       | 5000    | 1237047 | 26065737 | 1237047 | 120.0419 |
| master\12Circle\n05000\R01000\s089.kp |         |         |          |         |          |
| testcase\kplib-                       | 10000   | 2485622 | 52374379 | 2485622 | 120.173  |
| master\12Circle\n10000\R01000\s054.kp |         |         |          |         |          |

• Tìm được lời giải chắc chắn tối ưu cho 2 testcase có kích thước 50; 200

## Kết luận

- Các nhóm testcase 00Uncorrelated, 01WeaklyCorrelated, 05SubsetSum là dễ nhất (tìm được lời giải chắc chắn chắc chắn tối ưu cho tất cả testcase).
- Nhóm 07SpannerUncorrelated là khó nhất (chỉ tìm được lời giải tối ưu cho 1 testcase).