

# Phoebe-framework-and-experimental-results-for-estimating-fetal-age-and-weight.doc

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## Phoebe Framework and Experimental Results for Estimating Fetal Age and Weight

Loc Nguyen

Sunflower Soft Company, Ho Chi Minh, Vietnam

Email: ng\_phloc@yahoo.com

Thu-Hang T. Ho

Vinh Long General Hospital, Vinh Long, Vietnam

Email: bshangvl2000@yahoo.com

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### Abstract

Fetal age and weight estimation plays an important role in pregnant treatments. There are many estimation formulas created by combination of statistics and obstetrics. However, such formulas give optimal estimation if and only if they are applied into specified community. This research proposes a so-called Phoebe framework that supports physicians and scientists to find out most accurate formulas with regard to the community where scientists do their research. The built-in algorithm of Phoebe framework uses statistical regression technique for fetal age and weight estimation based on fetal ultrasound measures such as bi-parietal diameter, head circumference, abdominal circumference, fetal length, arm volume, and thigh volume. This algorithm is based on heuristic assumptions, which aims to produce good estimation formulas as fast as possible. From experimental results, the framework produces optimal formulas with high adequacy and accuracy. Moreover, the framework gives facilities to physicians and scientists for exploiting useful statistical information under pregnant data. Phoebe framework is a computer software available at <http://phoebe.locnguyen.net>.

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**Keywords:** fetal age estimation, fetal weight estimation, ultrasound measures, regression model, estimation formula.

### 1. Introduction

Fetal age and weight estimation is to predict the birth weight or birth age before delivery. It is very important for doctors to diagnose abnormal or diseased cases so that she/he can

decide treatments on such cases. Because this research mentions both age estimation and weight estimation, for convenience, the term “birth estimation” implicates both of them. There are two methods for birth estimation:

- Determining volume of fetal inside mother womb and then, calculating fetal weight based on such volume and mass density of flesh and bone. By the other way, fetal age and weight can be estimated according to size of mother womb.
- Applying statistical regression model: Fetal ultrasound measures such as bi-parietal diameter (*bpd*), head circumference (*hc*), abdominal circumference (*ac*), fetal length (*fl*), arm volume (*arm\_vol*), and thigh volume (*thigh\_vol*) are recorded and considered as input sample for regression analysis which results in a *regression function*. This function is formula for estimating fetal age and weight according to ultrasound measures such as *bpd*, *hc*, *ac*, *fl*, *arm\_vol*, and *thigh\_vol*. Data that is composed of these ultrasound measures is called gestational sample or pregnant sample. Terms: “*sample*” and “*data*” have the same meaning in this research. Sample is representation of population where research takes place.

Because the second method reflects features of population from statistical data, the regression model is chosen for fetal estimation in this research. Note, some terminologies such as *function*, *regression function*, *estimation function*, *regression model*, *estimation model*, *formula*, *regression formula*, and *estimation formula* have the same meaning.

1 There are many estimation formulas resulted from gestational researches such as [1 – 9]. Some of them gain high accuracy but they are only appropriate to population, community or ethnic group where such researches are done. If we apply these formulas into other community such as Vietnam, they are no longer accurate. Moreover, it is very difficult to find out a new and effective estimation formula or the cost of time and (computer) resources of formula discovery is expensive. Therefore, the first goal of this research is to propose an effective built-in algorithm which produces highly accurate formulas that are easy to tune with specified population. The process of producing formulas by such algorithm is as fast as possible. In addition, physicians and researchers always want to discover useful statistical information from measure sample and regression model. Thus, the second goal of this research is to give facilities to physicians and researchers by introducing them a framework that is called *Phoebe framework* or *Phoebe system*. Phoebe framework implements such built-in algorithm in the first goal and provides a tool allowing physicians and researchers to exploit and take advantage of useful information under gestational sample. This tool is programmed as computer software. Moreover, Phoebe framework allows software developers to modify its modules. For example, developers can improve the built-in algorithm by adding heuristic constraints.

This chapter is the improved collection of two our articles “A framework of fetal age and weight estimation” [10] and “Experimental Results of Phoebe Framework: Optimal Formulas for Estimating Fetus Weight and Age” [11]. Section 2 gives an overview of the architecture of Phoebe framework. Section 3 is description of the built-in algorithm to produce optimal formulas which are appropriated to a concrete population like Vietnam.

Such algorithm is the core of Phoebe framework. Section 4 discusses main use cases of the framework with respect to gestational sample. As experimental results, some interesting estimation formulas produced by the framework are described in section 5. Section 6 is conclusions. Note that Phoebe framework used statistic software package "Java Scientific Library" of Michael Thomas Flanagan [12] and parsing package "A Java expression parser" of Jos de Jong [13]. The package "Java Scientific Library" is the most important in the framework. The framework is implemented by Java language [14].

## 2. General architecture of Phoebe framework

Based on clinical data input which includes fetal ultrasound measures such as  $bpd$ ,  $hc$ ,  $ac$ , and  $fl$ , the framework produces optimal formulas for estimating fetal weight and fetal age with highest precision. Moreover, statistical information about fetus and gestation is also described in detailed with two forms: numerical format and graph format. So the framework consists of four components as follows:

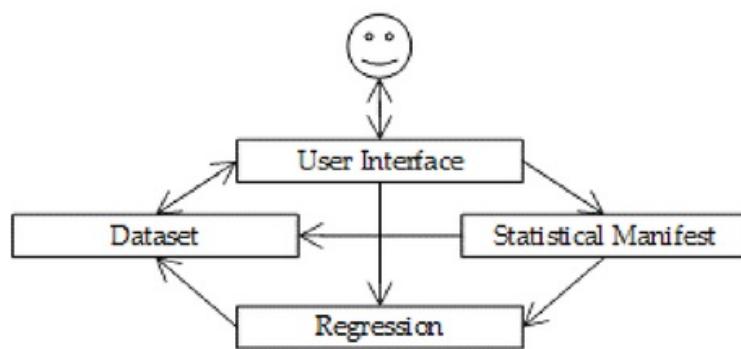
- *Dataset* component is responsible for managing information about fetal ultrasound measures such as  $bpd$ ,  $hc$ ,  $ac$ ,  $fl$  and extra gestational information in reasonable and intelligent manner. This component allows other components to retrieve such information. Gestational information is organized into some abstract structure, e.g., a matrix whose each row represents a sample of  $bpd$ ,  $hc$ ,  $ac$ ,  $fl$  measures. **Table 1** is an example of this abstract structure.
- *Regression* component represents estimation formula or regression function. This component reads ultrasound information from *Dataset* component and builds up optimal estimation formula from such information. The built-in algorithm used to discover and construct estimation formula is discussed in section 3. This component is the most important one because it implements such discovery algorithm.
- *Statistical Manifest* component describes statistical information of both ultrasound measures and regression function, for example: mean and standard deviation of  $bpd$  samples, sum of residuals, correlation coefficient of regression function, and percentile graph of fetal weight. Statistical manifest is organized into two forms such as numerical format and graph format.
- *User Interface (UI)* component is responsible for providing interaction between system and users such as physicians and researchers. A popular use case is that users enter ultrasound measures and requires system to print out both optimal estimation formula and statistical information about such ultrasound measures; moreover users can retrieve other information in *Dataset* component. *UI* component links to all of other components so as to give users as many facilities as possible.

<i>bpd</i>	<i>hc</i>	<i>fl</i>	<i>ac</i>	<i>fetal age (week)</i>	<i>fetal weight (gram)</i>
74	262	51	255	28	900
72	260	51	232	28	900

68	260	50	229	28	900
72	275	52	240	28	900
72	274	52	240	28	950
74	253	50	235	28	950
71	257	52	239	28	950
71	255	53	236	28	950
70	264	52	246	28	950

**Table 1.** An example of gestational sample matrix

Three components: *Dataset*, *Regression* and *Statistical Manifest* are basic components. The fourth component *User Interface* is the bridge among them. **Figure 1** shows general architecture of Phoebe framework.



**Figure 1.** General architecture of Phoebe framework

The framework used statistic software package “Java Scientific Library” of author [12] and parsing package “A Java expression parser” of author [13]. The package “Java Scientific Library” is the most important in the framework. The framework is implemented by Java language [14].

### 3. Built-in algorithm of Phoebe framework

Phoebe framework uses regression model for estimating fetal weight and age. Suppose a linear regression function  $Y = \alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \dots + \alpha_n X_n$  where  $Y$  is fetal weight or age whereas  $X_i$  (s) are gestational ultrasound measures such as *bpd*, *hc*, *ac*, and *fl*. Variable  $Y$  is called response variable or dependent variable. Each  $X_i$  is called *regression variable*, *regressor*, *regression variable*, or *independent variable*. Each  $\alpha_i$  is called *regression coefficient*. Given a set of measure values of  $X_i$  (s), the value of  $Y$  called *Y-estimated* calculated from this regression function is estimated fetal weight (or age) which is compared with real value of  $Y$  measured by ultrasonic machine. The real value of  $Y$  called *Y-real* is fetal weight (or age) available in sample. In this research, the notation  $Y$  refers implicitly to *Y-estimated* if there is no explanation. The deviation between *Y-estimated* and *Y-real* is criterion used to assess the quality or the precision of regression function. This deviation is also called *estimation error*.

The less the deviation is, the better the regression function is. The goal of this research is to find out the optimal regression function or estimation formula whose precision is highest.

A regression function will be good if it meets two conditions as follows:

- The correlation between  $Y\text{-estimated}$  and  $Y\text{-real}$  is large.
- The sum of residuals is small. Note that residual is defined as the square of deviation between  $Y\text{-estimated}$  and  $Y\text{-real}$ . We have:

$$\text{residual} = (Y_{\text{estimated}} - Y_{\text{real}})^2$$

These two conditions are called the *pair of optimal conditions*. A regression function is optimal or best if it satisfies the pair of optimal conditions at most, where correlation between  $Y\text{-estimated}$  and  $Y\text{-real}$  is largest and the sum of residuals is smallest. Given a set of regression variables  $X_i$  (where  $i = 1, 2, \dots, n$ ), we recognize that a regression function is a combination of  $k$  variables  $X_i$  (s) where  $k \leq n$  so that such combination achieves the pair of optimal conditions. Given a set of possible regression variables  $VAR = \{X_1, X_2, \dots, X_n\}$  being ultrasound measures, brute-force algorithm can be used to find out optimal function, which includes three following steps:

1. Let indicator number  $k$  be initialized 1, which responds to  $k$ -combination having  $k$  regression variables.
2. All combinations of  $n$  variables taken  $k$  are created. For each  $k$ -combination, the function built up by  $k$  variables in this  $k$ -combination is evaluated on the pair of optimal conditions; if such function satisfies these conditions at most then, it is optimal function.
3. Indicator  $k$  is increased by 1. If  $k = n$  then algorithm stops, otherwise go back step 2.

The number of combinations which brute-force algorithm browses is:

$$\sum_{k=1}^n \frac{n!}{k!(n-k)!}$$

Where  $n$  is the number of regression variables and notation " $k!$ " denotes factorial of  $k$ . If  $n$  is large enough, there are a huge number of combinations, which causes that the brute-force algorithm never terminates and it is impossible to find out the best function. Moreover there are many kinds of regression function such as linear, quadric, cube, logarithm, exponent, and product. So we propose a new algorithm which overcomes this drawback and always finds out the optimal function. In other words, the termination of the proposed algorithm is determined and the time cost is decreased significantly because the searching space is reduced as small as possible. The proposed algorithm is called *seed germination (SG)* algorithm. SG is built-in algorithm of Phoebe framework, which is the core of Phoebe framework. It is heuristic algorithm, which is based on the *pair of heuristic assumptions* as follows:

- First assumption: regression variables  $X_i$  (s) **1** trends to be mutually independent. It means that any pair of  $X_i$  and  $X_j$  with  $i \neq j$  in an optimal function are mutually independent. The independence is reduced into the looser condition “*the correlation coefficient of any pair of  $X_i$  and  $X_j$  is less than a threshold  $\delta$* ”. This is *minimum assumption*.
- Second assumption: each variable **1** contributes to quality of optimal function. The contribution rate of a variable  $X_i$  is defined as the correlation coefficient between such variable and *Y-real*. The higher the contribution rate is, the more important the respective variable is. Variables with high contribution rate are called *contributive variables*. So optimal function includes only contributive regression variables. The second assumption is stated that “*the correlation coefficient of any regression variable  $X_i$  and real response value *Y-real* is greater than a threshold  $\varepsilon$* ”. This is *maximum assumption*.

SG algorithm tries to find out a combination of regression variables  $X_i$  (s) so that such combination satisfies such pair of heuristic assumptions. In other words, it is expected that this combination can constitute **1** optimal regression function that satisfies the *pair of heuristic conditions*, as follows [10, p. 22]:

- The correlation coefficient of any pair of  $X_i$  and  $X_j$  is less than the minimum threshold  $\delta > 0$ . This condition is corresponding to the minimum assumption, which is called *minimum condition or independence condition*.
- The correlation coefficient of any  $X_i$  and *Y-real* is greater than the maximum threshold  $\varepsilon > 0$ . This condition is corresponding to the maximum assumption, which is called *maximum condition or contribution condition*.

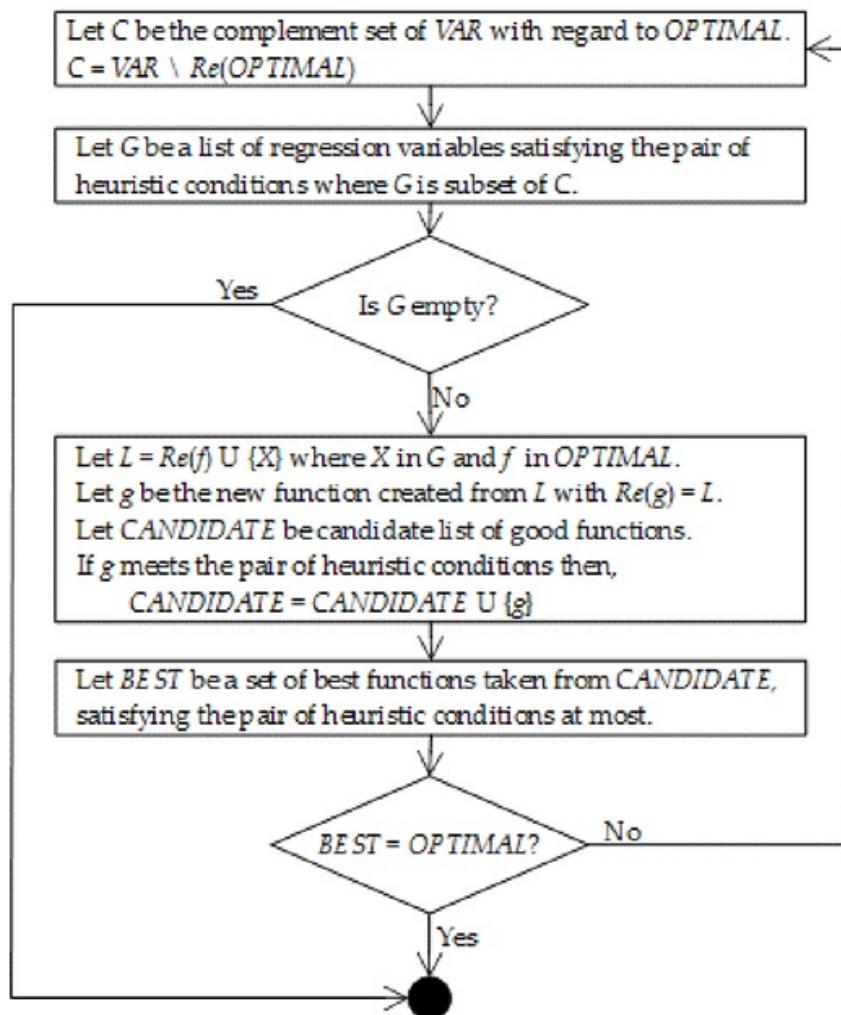
Given a set of possible regression variables  $VAR = \{X_1, X_2, \dots, X_n\}$  being ultrasound measures, let  $f = \alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \dots + \alpha_k X_k$  ( $k \leq n$ ) be the estimation function and let  $Re(f) = \{X_1, X_2, \dots, X_k\}$  be its regression variables. Note that the value of  $f$  is fetal age or fetal weight.  $Re(f)$  is considered as the representation of  $f$ . Let *OPTIMAL* be the output of SG algorithm, which is a set of optimal functions returned. *OPTIMAL* is initialized as empty set. Let  $Re(OPTIMAL)$  be a set of regression variables contained in all optimal functions  $f \in OPTIMAL$ . SG algorithm has four following steps [10, p. 22]:

1. Let  $C$  be the complement set of  $VAR$  with regard to *OPTIMAL*, we have  $C = VAR \setminus Re(OPTIMAL)$  where the backslash “\” denotes complement operator in set theory. It means that  $C$  is in  $VAR$  but not in  $Re(OPTIMAL)$ .
2. Let  $G \subset C$  be a list **1** of regression variables satisfying the pair of heuristic conditions. Note,  $G$  is subset of  $C$ . If  $G$  is empty, the algorithm terminates; otherwise going to step 3.
3. We iterate over  $G$  in order to find out candidate list of good functions. For each regression variable  $X \in G$ , let  $L$  be the union set of optimal regression variables and  $X$ . We have  $L = Re(f) \cup \{X\}$  where  $f \in OPTIMAL$ . Suppose *CANDIDATE* is candidate list of good functions, which is initialized as empty set. Let  $g$  be the new function created from  $L$ ; in other words, regression variables of  $g$  belong to  $L$ ,  $Re(g) = L$ . If function  $g$  meets the

pair of heuristic conditions, it is added into  $CANDIDATE$ ,  $CANDIDATE = CANDIDATE \cup \{g\}$ .

4. Let  $BEST$  be a set of best functions taken from  $CANDIDATE$ . In other words, these functions belong to  $CANDIDATE$  and satisfy the pair of heuristic conditions at most, where correlation is largest and the sum of residuals is smallest. If  $BEST$  equals  $OPTIMAL$  then the algorithm stops; otherwise assigning  $BEST$  to  $OPTIMAL$  and going back step 1. Note that two sets are equal if their elements are the same.

**Figure 2** shows the flow chart of SG algorithm.



**Figure 2.** Flow chart of SG algorithm

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SG algorithm was described in article "A framework of fetal age and weight estimation" [10, pp. 21-23]. It is easy to recognize that the essence of SG algorithm is to reduce search space by choosing regression variables satisfying heuristic assumption as "seeds". Optimal

functions are composed of these seeds. Algorithm always delivers best functions but can lose other good functions. The length of function is defined as the number of its regression variables. Terminated condition is that no more optimal functions can be found out or possible variables are browsed exhaustedly. So the result function is the longest and best one but some other shorter functions may be significantly good.

The current implementation of SG algorithm establishes that the minimum threshold  $\delta$  is arbitrary. It also supports non-linear regression models shown in **Table 2** as follows:

Polynomial	$Y = \alpha_0 + \alpha_1(X_1 + X_2 + \dots + X_n)^k$
Logarithm	$Y = \alpha_0 + \alpha_1 \log(X_1) + \alpha_2 \log(X_2) + \dots + \alpha_n \log(X_n)$
	$Y = \alpha_0 + \alpha_1 \log(X_1 + X_2 + \dots + X_n)$
Exponent	$Y = \exp(\alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \dots + \alpha_n X_n)$
	$Y = \exp(\alpha_0 + \alpha_1(X_1 + X_2 + \dots + X_n))$
Product	$Y = \alpha_0 X_1^{\alpha_1} X_2^{\alpha_2} \dots X_n^{\alpha_n}$

**Table 2.** Non-linear regression models

The notations “exp” and “log” denote exponent function and natural logarithm function, respectively. Most of non-linear regression models can be transformed into linear regression models. For example, given product model, following is an example of linear transformation.

$$\log(Y) = \log(\alpha_0) + \alpha_1 \log(X_1) + \alpha_2 \log(X_2) + \dots + \alpha_n \log(X_n)$$

Let,

$$U = \log(Y), Z_i = \log(X_i), \beta_0 = \log(\alpha_0), \beta_{i \geq 1} = \alpha_i$$

The product model becomes linear model with regard to variables  $U$ ,  $Z_i$  and coefficients  $\beta_i$  as follows:

$$U = \beta_0 + \beta_1 Z_1 + \beta_2 Z_2 + \dots + \beta_n Z_n$$

**Table 3** shows how to transform non-linear models into linear models.

Polynomial transformation	$Y = \alpha_0 + \alpha_1(X_1 + X_2 + \dots + X_n)^k$
	$Y = \alpha_0 + \alpha_1 Z_1$ Where, $Z_1 = (X_1 + X_2 + \dots + X_n)^k$
Logarithm transformation	$Y = \alpha_0 + \alpha_1 \log(X_1) + \alpha_2 \log(X_2) + \dots + \alpha_n \log(X_n)$
	$Y = \alpha_0 + \alpha_1 Z_1 + \alpha_2 Z_2 + \dots + \alpha_n Z_n$

	Where $Z_i = \log(X_i)$
Logarithm transformation	$Y = \alpha_0 + \alpha_1 \log(X_1 + X_2 + \dots + X_n)$
	$Y = \alpha_0 + \alpha_1 Z_1$ Where $Z_1 = \log(X_1 + X_2 + \dots + X_n)$
Exponent transformation	$Y = \exp(\alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \dots + \alpha_n X_n)$
	$U = \alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \dots + \alpha_n X_n$ Where $U = \log(Y)$
Exponent transformation	$Y = \exp(\alpha_0 + \alpha_1 (X_1 + X_2 + \dots + X_n))$
	$U = \alpha_0 + \alpha_1 Z_1$ Where $U = \log(Y)$ and $Z_1 = X_1 + X_2 + \dots + X_n$
Product transformation	$Y = \alpha_0 X_1^{\alpha_1} X_2^{\alpha_2} \dots X_n^{\alpha_n}$
	$U = \beta_0 + \beta_1 Z_1 + \beta_2 Z_2 + \dots + \beta_n Z_n$ Where, $U = \log(Y), Z_i = \log(X_i), \beta_0 = \log(\alpha_0), \beta_{i \geq 1} = \alpha_i$

**Table 3.** Transformation of non-linear models into linear models

With the built-in SG algorithm, Phoebe framework can be totally used for any regression application beyond birth estimation.

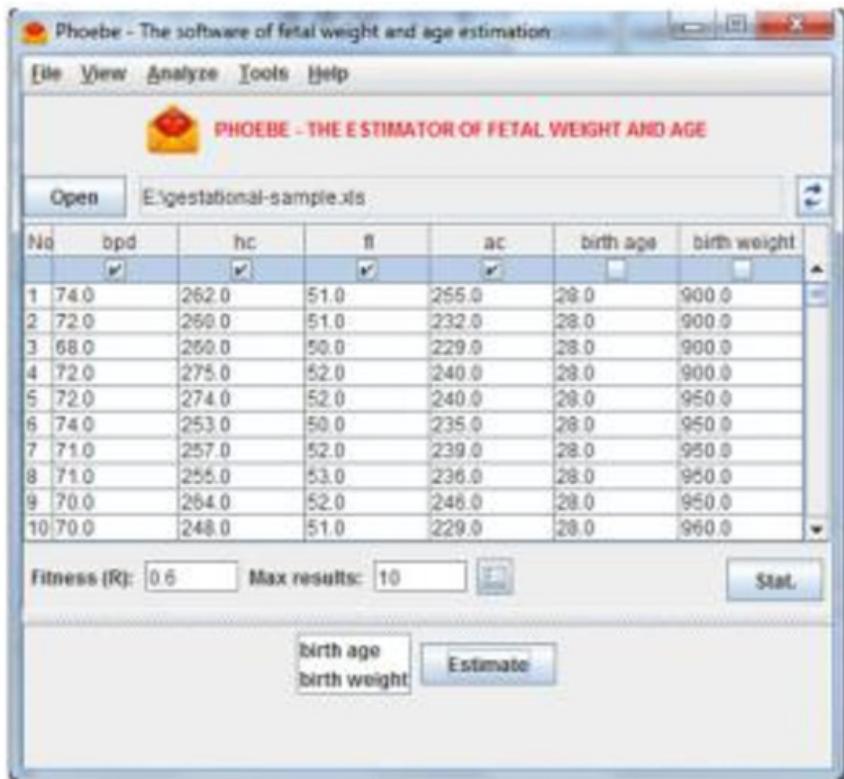
#### 4. Use cases of Phoebe framework

Phoebe framework has three basic use cases realized by three components dataset, regression model and statistical manifest discussed in section 2. Three basic use cases includes:

1. Discovering optimal formulas with high accuracy. Optimal formulas are results of SG algorithm described in section 3.
2. Providing statistical information under gestational sample. Statistical information is in numeric format and graph format.
3. Comparison among different formulas.

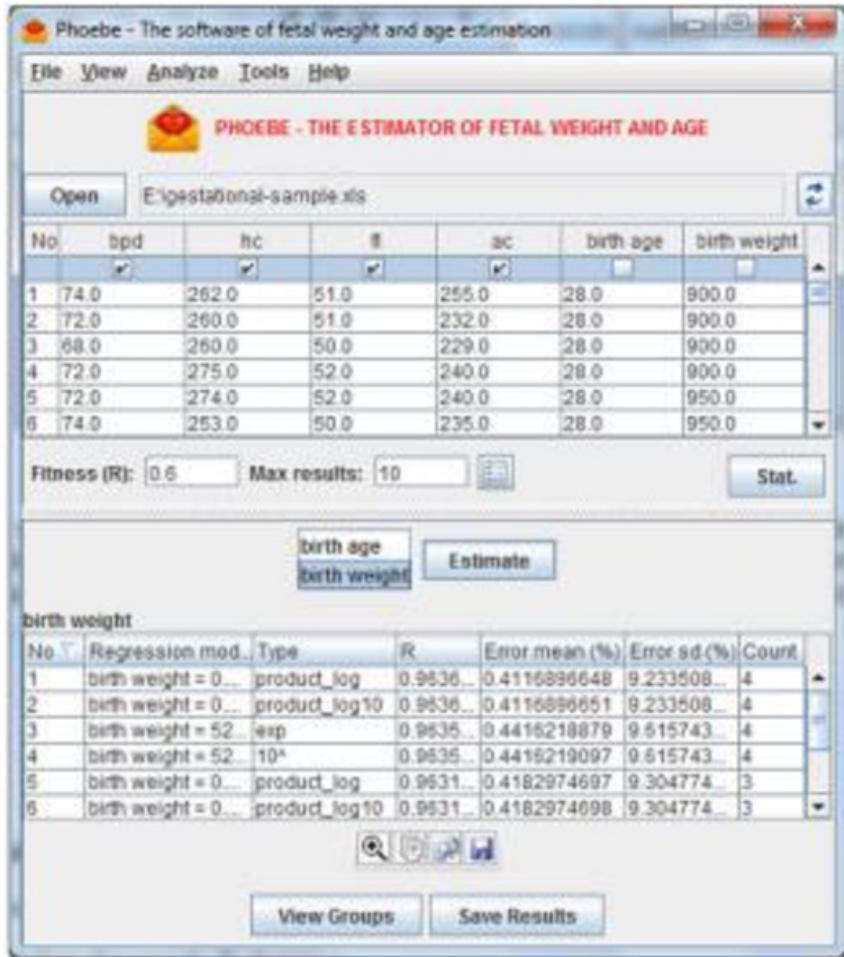
##### Use case 1: Discovering optimal formulas

Given gestational data [15] is composed of 2-dimension ultrasound measures of pregnant women. These measures are taken at Vinh Long General Hospital – Vietnam, which include bi-parietal diameter (*bpd*), head circumference (*hc*), abdominal circumference (*ac*) and fetal length (*fl*). Fetal age is from 28 weeks to 42 weeks. Fetal weight is measured by gram. Gestational sample is shown in **Figure 3**.



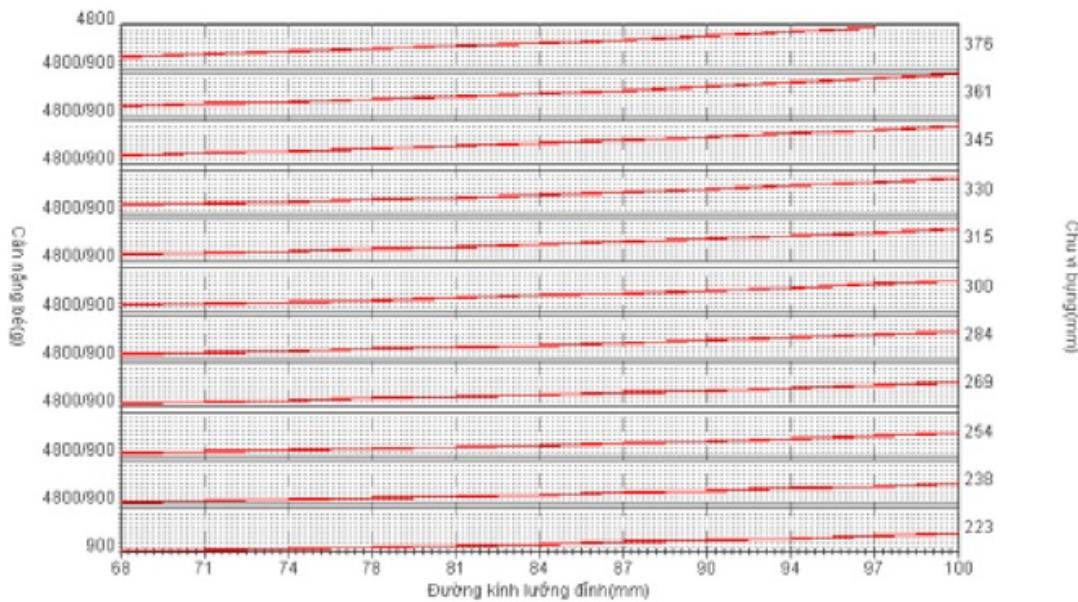
**Figure 3.** Gestational sample

After specifying maximum threshold  $\varepsilon$  (fitness value) and which measures are regression variables and response variable, user presses button "Estimate" to retrieve optimal formulas as results of SG algorithm. Such optimal formulas are shown in **Figure 4**. Note, in **Figure 4**, regression variables are *bpd*, *hc*, *ac*, and *fl* whereas response variable is fetal weight. The threshold  $\varepsilon$  is 0.6.



**Figure 4.** Optimal weight estimation formulas

An estimation formula with one or two regressors (ultrasound measures) can be represented as a graph. In the illustrative **Figure 5**, the horizontal axis indicates the measure *bpd* in millimeter and the right vertical axis indicates the measure *ac* in millimeter. The left vertical axis shows the estimated weight.



**Figure 5.** Estimation graph for estimating fetal weight

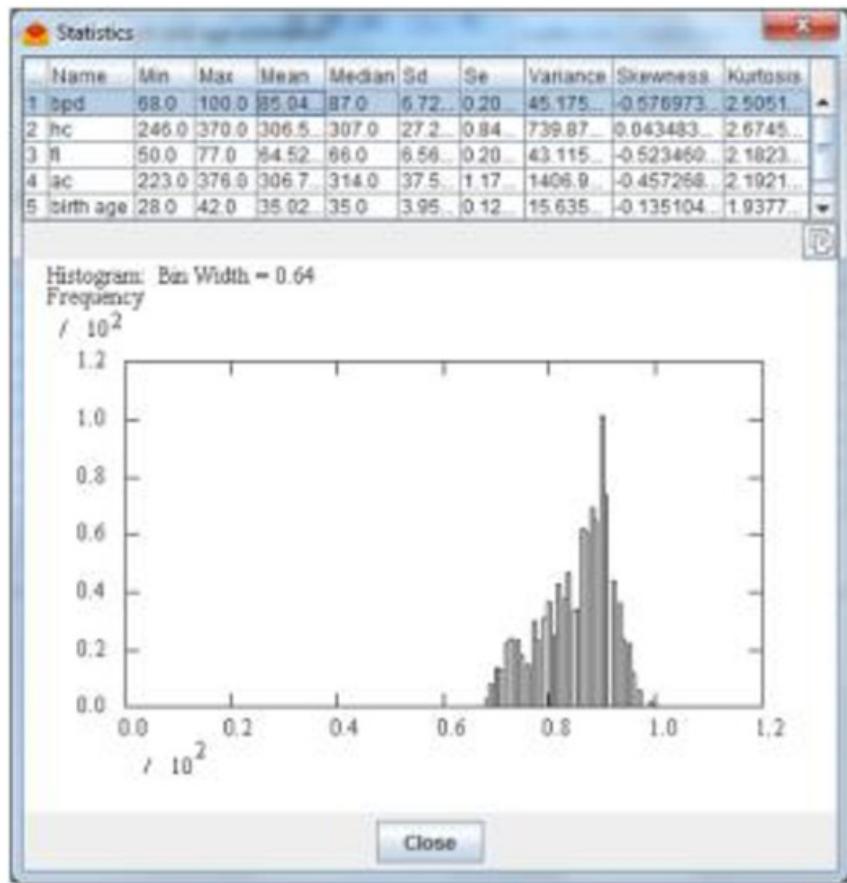
The graph in **Figure 5** has 11 estimation lines represented as internal (red) lines. Each estimation line corresponds to a small interval of  $ac$ . Fetal weight on each estimation line ranges from 900 grams to 4800 grams. This is a way to shows a three-dimension function as a two-dimension graph. For example, given  $bpd = 90$  and  $ac = 300$ , we need to estimate fetal weight. Because  $ac$  is 300 millimeter, we look at the 6<sup>th</sup> estimation line from bottom to up. The intersection point between  $bpd = 90$  and the 6<sup>th</sup> estimation line is projected on the left vertical axis, which results out a fetal weight that approximates to  $(4800 - 900) / 2 + 900 \approx 2850$  grams because such intersection point is near to midpoint of the weight range on the 6<sup>th</sup> estimation line.

### Use case 2: Providing statistical information

Statistical information is classified into two groups: gestational information and estimation information.

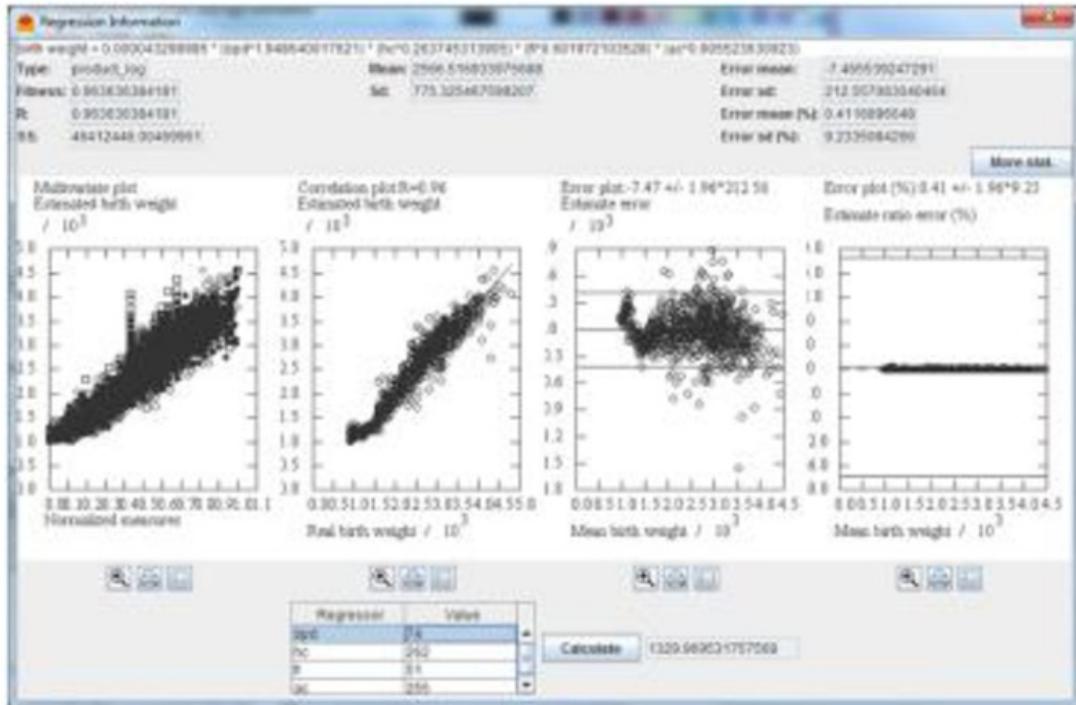
- Gestational information contains statistical attributes about fetal ultrasound measures, for example: mean, median and standard deviation of  $bpd$ .
- Estimation information contains attributes about estimation model, for example: correlation coefficient, sum of residuals and estimation error of estimation formula.

In representation, statistical information is described in two forms: numeric format and graph format. **Figure 6** shows statistical attributes (mean, median, standard deviation, histogram, etc.) of fetal age and ultrasound measures  $bpd$ ,  $hc$ ,  $ac$ ,  $fl$ .



**Figure 6.** Gestational statistical information

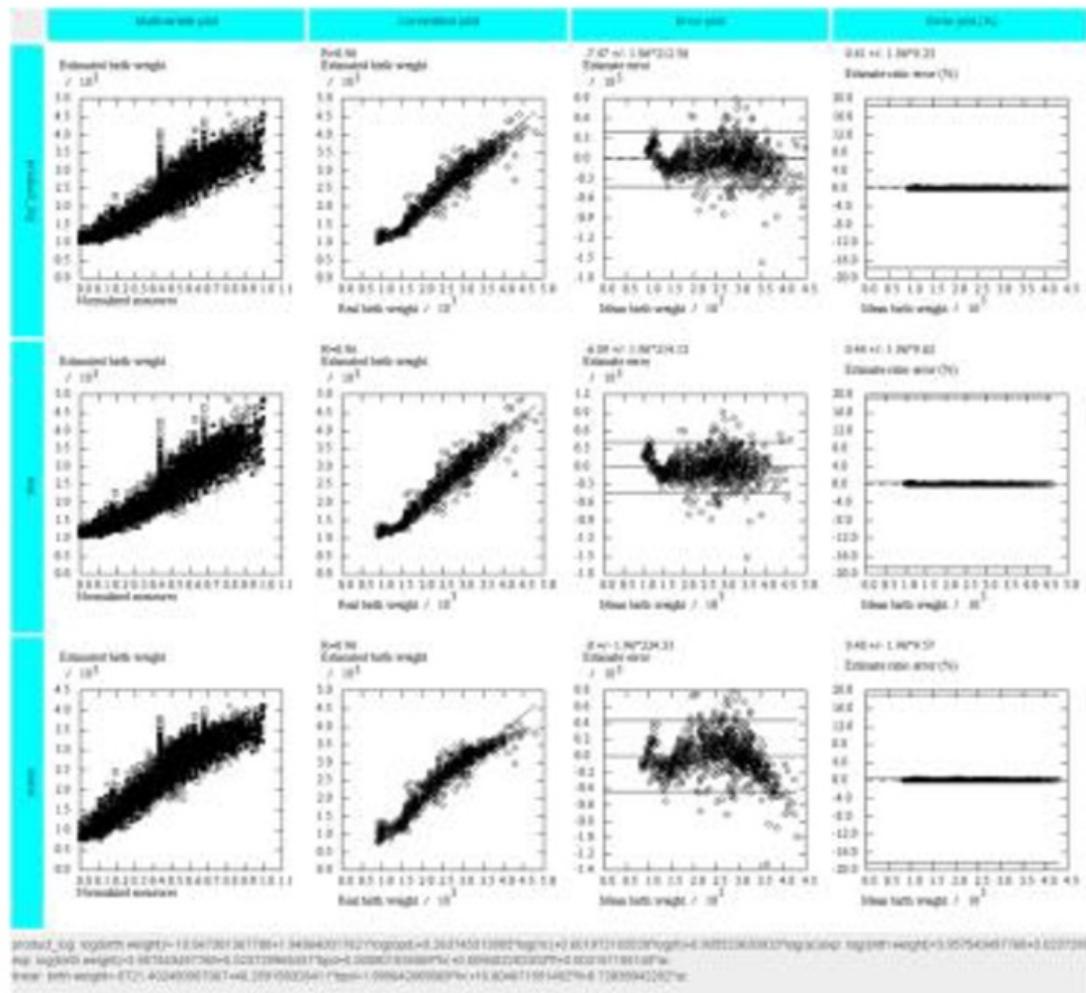
**Figure 7** shows full description of a weight estimation formula:  $weight = 0.000043 * (bpd^{1.948640}) * (hc^{0.263745}) * (fl^{0.601972}) * (ac^{0.905524})$ . For instance, sum of residuals (SS) is 46412446.0047 and estimation error is  $-7.4655 \pm 212.5571$ . Note, the sign “ $\wedge$ ” denotes exponent function, for example  $2^3 = 8$ .



**Figure 7.** Statistical estimation information

### Use case 3: Comparison among different formulas

There are many criteria to evaluate efficiency and accuracy of estimation formulas. These criteria are called evaluation criteria, for example: correlation coefficient, sum of residuals, estimation error. Each formula has individual strong points and drawbacks. A formula is better than another one in terms of some criteria but may be worse than this other one in terms of different criteria. An optimal formula is the one that has more strong points than drawbacks in most criteria. Hence, Phoebe framework supports the comparison among different formulas via *evaluation matrix* represented in **Figure 8**. Each row in evaluation matrix represents a formula whereas each column indicates a criterion. For example, first row, second row and third row represent three formulas in form of logarithm function, exponent function, and linear function, respectively. Four criteria: multivariate correlation, estimation correlation, error range and ratio error range are arranged in three respective columns.



**Figure 8.** Comparison among different formulas

Tables 4, 5, 6, 7, and 8 in the section of experimental results are numeric interpretations of evaluation matrix in Figure 8.

## 5. Experimental Results

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We make experiments based on Phoebe framework in order to find out optimal formulas for estimating fetus weight and ages with note that such formulas are most appropriate to our gestational samples. We use two samples in which the first sample includes 2-dimension (2D) ultrasound measures of 1027 cases and the second sample includes 3-dimension (3D) ultrasound measures of 506 cases. Ho and Phan [15 – 16] collected these samples of pregnant women at Vinh Long General Hospital – Vietnam with obeying strictly all medical ethical criteria. These women and their husbands are Vietnamese. Their periods are regular and their last periods are determined. Each of them has only one alive fetus. Fetal age is

from 28 weeks to 42 weeks. Delivery time is not over 48 hours since ultrasound scan. Measures in 2D sample are *bpd*, *hc*, *ac*, and *fl*. Measures in 3D sample are *bpd*, *hc*, *ac*, *fl*, *thigh\_vol*, *arm\_vol*. The unit of *bpd*, *hc*, *ac*, *fl* is millimeter. The unit of *thigh\_vol* and *arm\_vol* is cm<sup>3</sup>. The units of fetal age and fetal weight are week and gram, respectively. Experimental results mentioned in this section were also published in our article “Experimental Results of Phoebe Framework: Optimal Formulas for Estimating Fetus Weight and Age” [11].

The proposed framework can produce amazing formulas. We compare our optimal formulas with the others according to metrics such as estimation correlation and estimation error range, given such two gestational samples. Let  $Y = \{y_1, y_2, \dots, y_n\}$  and  $Z = \{z_1, z_2, \dots, z_n\}$  be fetal sample age/weight and fetal estimated age/weight, respectively. The estimation correlation denoted  $R$  is correlation coefficient of sample response value and estimated response value, according to Eq. (1). The correlation  $R$  reflects adequacy of a given formula. The larger the  $R$  is, the better the formula is.

$$R = \frac{\sum_{i=1}^n y_i z_i}{\sqrt{\sum_{i=1}^n y_i^2} \sqrt{\sum_{i=1}^n z_i^2}} \quad (1)$$

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An estimation error denoted  $d_i$  is deviation between  $z_i$  and  $y_i$ . The estimation error mean denoted  $\mu$  is mean of errors. The error mean  $\mu$  reflects accuracy of a given formula. The smaller the absolute value of  $\mu$  is, the more accurate the formula is. If  $\mu$  is positive, the respective formula leans to overestimation. If  $\mu$  is negative, the respective formula leans to low estimation. The standard deviation  $\sigma$  of estimation errors reflects stability of a given formula. The smaller the standard deviation  $\sigma$  is, the more stable the formula is. The combination of error mean  $\mu$  and standard deviation  $\sigma$  results out a so-called *error range*. Eq. (2) explains how to calculate  $\mu$ ,  $\sigma$ , and error range.

$$\begin{aligned} d_i &= z_i - y_i \\ \mu &= \frac{1}{n} \sum_{i=1}^n d_i \\ \sigma &= \sqrt{\frac{1}{n-1} \sum_{i=1}^n (d_i - \mu)^2} \\ \text{error\_range} &= [\mu - \sigma, \mu + \sigma] = \mu \pm \sigma \end{aligned} \quad (2)$$

1

For example, if  $\mu = -0.0292$  and  $\sigma = 1.45$  then, the error range is  $-0.0292 \pm 1.45$ , which means that the total average error ranges from  $-1.4792 = -0.0292 - 1.45$  to  $1.4208 = -0.0292 + 1.45$ . The error range reflects both adequacy and accuracy of a given formula.

**Table 4** shows comparison between our best age formula and the others with 2D sample. As a convention, name of each formula is the name of respective author listed in references section. For example, formula “Ho 1” is the first formula of the author Ho [4]. As seen in

**Table 4** our formula is the best with  $R=0.9303$  and error range  $-0.0292\pm1.4500$  week (s). As a convention, our formulas have names with prefix "NH".

1 Formula	Expression	R	Error Range
NH 1	$\log(\text{age}) = 2.419638 + 0.002012 * \text{bpd} + 0.000934 * \text{hc} + 0.00547 * \text{fl} + 0.001042 * \text{ac}$	0.9303	$-0.0292\pm1.4500$
NH 2	$\text{age} = -3.364759 + 0.056285 * \text{bpd} + 0.034697 * \text{hc} + 0.188156 * \text{fl} + 0.035304 * \text{ac}$	0.9285	$0\pm1.4682$
Ho 1	$\text{age} = 331.022308 - 1.611774 * (\text{hc} + \text{ac}) + 0.00278 * ((\text{hc} + \text{ac})^2) - 0.000002 * ((\text{hc} + \text{ac})^3)$	0.9212	$0\pm1.5384$
Varol 6	$\text{age} = 11.769 + 1.275 * \text{fl}/10 + 0.449 * ((\text{fl}/10)^2) - 0.02 * ((\text{fl}/10)^3)$	0.8949	$-1.6807\pm1.8525$
Varol 1	$\text{age} = 5.596 + 0.941 * \text{ac}/10$	0.8941	$-0.5683\pm1.7711$
Varol 5	$\text{age} = 1.863 + 6.280 * \text{fl}/10 - 0.211 * ((\text{fl}/10)^2)$	0.8934	$-1.5182\pm2.1150$

**Table 4.** Comparison of age estimation with 2D sample.

The sign " $\wedge$ " denotes exponent operator. The template of formulas aims to flexibility, which can be input of any computational tool. **Table 5** shows comparison between our best weight formula and the others with 2D sample. As seen in **Table 5**, our formula is the best with  $R=0.9636$  and error range  $-7.4656\pm212.5573$  grams.

1 Formula	Expression	R	Error Range
NH 3	$\log(\text{weight}) = -10.047381 + 1.94864 * \log(\text{bpd}) + 0.263745 * \log(\text{hc}) + 0.601972 * \log(\text{fl}) + 0.905524 * \log(\text{ac})$	0.9636	$-7.4656\pm212.5573$
NH 4	$\log(\text{weight}) = 3.957543 + 0.02373 * \text{bpd} + 0.000802 * \text{hc} + 0.009403 * \text{fl} + 0.003157 * \text{ac}$	0.9635	$-6.0901\pm214.1153$
Sherpard	$\text{weight} = 10^{(1.2508 + 0.166 * \text{bpd}/10 + 0.046 * \text{ac}/10 - 0.002646 * \text{ac} * \text{bpd}/100)}$	0.9619	$-65.8121\pm219.0392$
Ho 2	$\text{weight} = 10^{(1.746 + 0.0124 * \text{bpd} + 0.001906 * \text{ac})}$	0.9602	$-11.5576\pm223.5124$
Hadlock	$\text{weight} = 10^{(1.304 + 0.05281 * \text{ac}/10 + 0.1938 * \text{fl}/10 - 0.004 * \text{ac} * \text{fl}/100)}$	0.9395	$-76.4960\pm272.9474$
Campbell & Wilkin	$\text{weight} = 1000 * \exp(-4.564 + 0.282 * \text{ac}/10 - 0.00331 * \text{ac} * \text{ac}/100)$	0.9215	$68.1261\pm308.5728$

**Table 5.** Comparison of weight estimation with 2D sample.

**Table 6** shows comparison between our best age formula and the others with 3D sample. As seen in **Table 6**, our formula is the best with  $R=0.9970$  and error range  $\pm0.2696$  week.

1 Formula	Expression	R	Error Range
NH 5	$\text{age} = 20.759763 + 0.170859 * (\text{thigh\_vol} + \text{arm\_vol}) - 0.000545 * ((\text{thigh\_vol} + \text{arm\_vol})^2) + 0.000001 * ((\text{thigh\_vol} + \text{arm\_vol})^3)$	0.9970	$0\pm0.2696$
NH 6	$\text{age} = 21.816252 + 0.137531 * (\text{thigh\_vol} + \text{arm\_vol}) -$	0.9969	$0\pm0.2752$

	$0.000228 * ((thigh\_vol + arm\_vol)^2)$		
1 Ho 3	$age = 21.1148 + 0.2381 * thigh\_vol - 0.001 * (thigh\_vol^2) + 0.000002 * (thigh\_vol^3)$	0.9960	-0.0150±0.3173
Ho 4	$age = 167.079079 - 1.553705 * ac + 0.005559 * (ac^2) - 0.000006 * (ac^3)$	0.8482	0.3723±1.8985

**Table 6.** Comparison of age estimation with 3D sample.

**Table 7** shows comparison between our best weight formula and the others with 3D sample. As seen in **Table 7**, our formula is the best with  $R=0.9708$  and error range  $-0.0001 \pm 180.9803$  grams.

1 Formula	Expression	R	Error Range
NH 7	$weight = -3617.936175 + 0.513171 * hc + 1.960176 * ac + 39.804645 * bpd + 17.016936 * fl + 8.366404 * thigh\_vol + 5.828808 * arm\_vol$	0.9708	-0.0001±180.9803
NH 8	$weight = -3626.314419 + 43.426744 * bpd + 23.645338 * fl + 11.414273 * thigh\_vol$	0.9698	0±184.0439
Ho 5	$weight = -3306 + 55.477 * bpd + 13.483 * thigh\_vol$	0.9663	-0.0072±194.0956
Lee 3	$weight = exp(0.5046 + 1.9665 * log(bpd/10) - 0.3040 * (log(bpd/10)^2) + 0.9675 * log(ac/10) + 0.3557 * log(arm\_vol))$	0.9620	247.8761±206.1607
Lee 5	$weight = exp(2.1264 + 1.1461 * log(ac/10) + 0.4314 * log(thigh\_vol))$	0.9514	289.2660±234.0763
Lee 2	$weight = exp(-3.6138 + 4.6761 * log(ac/10) - 0.4959 * (log(ac/10)^2) + 0.3795 * log(arm\_vol))$	0.9472	316.4974±242.7964
Ho 6	$weight = -882.7049 + 73.9955 * thigh\_vol - 0.497 * (thigh\_vol^2) + 0.0014 * (thigh\_vol^3)$	0.9385	-7.5001±260.4596
Lee 4	$weight = exp(4.7806 + 0.7596 * log(thigh\_vol))$	0.9298	737.4932±344.1904
Lee 1	$weight = exp(4.9588 + 1.0721 * log(arm\_vol) - 0.0526 * (log(arm\_vol)^2))$	0.9281	867.0836±309.5779
Chang	$weight = 1080.8735 + 22.44701 * thigh\_vol$	0.9229	456.5168±298.2517

**Table 7.** Comparison of weight estimation with 3D sample.

Within the context of this research, from section of 3D ultrasound in PhD dissertation of Thu-Hang T. Ho [4], I recognize that fetus weight and fetus age are mutually dependent. For instance, when fetus age increases, fetus weight increase too. As a result, weight estimation is improved significantly if fetus age was known before. If fetus age is added into the regression model of fetus weight as a regression variable (regressor), the resulted weight estimation formula, called *dual formula*, is even better than the most optimal ones shown in **Tables 5** and **6**. Such dual formula is not only precise but also practical because many pregnant women knew their gestational age before taking an ultrasound examination. Given 2D sample and 3D sample, **Table 8** shows dual formulas in comparison with the most optimal ones shown in **Tables 5** and **7** with regard to  $R$  and error range. As a convention,

our dual formulas have names with prefix "NHD". Notation "log10" denotes logarithm function with base 10.

1 Formula	Expression	R	Error Range
NHD 1 (2D sample)	$\log10(\text{weight}) = -3.715073 + 1.873457 * \log10(\text{bpd}) + 0.363783 * \log10(\text{fl}) + 0.691683 * \log10(\text{ac}) + 0.722245 * \log10(\text{age})$	0.9674	$-5.6422 \pm 202.0395$
NHD 2 (2D sample)	$\log10(\text{weight}) = -3.761798 + 2.001731 * \log10(\text{bpd}) + 0.811078 * \log10(\text{ac}) + 0.826279 * \log10(\text{age})$	0.9667	$-5.6111 \pm 204.1477$
NHD 3 (3D sample)	$\text{weight} = -4988.000528 + 66.374156 * \text{age} + 0.370084 * \text{hc} + 1.943247 * \text{ac} + 39.464816 * \text{bpd} + 13.215505 * \text{fl} + 3.658463 * \text{thigh\_vol}$	0.9715	$0 \pm 178.8091$
NHD 4 (3D sample)	$\text{weight} = -4982.099978 + 18.089354 * \text{age} + 2.001675 * \text{ac} + 39.85375 * \text{bpd} + 13.229377 * \text{fl} + 3.619405 * \text{thigh\_vol}$	0.9714	$0 \pm 178.9114$
NH 3 (2D sample)	$\log(\text{weight}) = -10.047381 + 1.94864 * \log(\text{bpd}) + 0.263745 * \log(\text{hc}) + 0.601972 * \log(\text{fl}) + 0.905524 * \log(\text{ac})$	0.9636	$-7.4656 \pm 212.5573$
NH 4 (2D sample)	$\log(\text{weight}) = 3.957543 + 0.02373 * \text{bpd} + 0.000802 * \text{hc} + 0.009403 * \text{fl} + 0.003157 * \text{ac}$	0.9635	$-6.0901 \pm 214.1153$
NH 7 (3D sample)	$\text{weight} = -3617.936175 + 0.513171 * \text{hc} + 1.960176 * \text{ac} + 39.804645 * \text{bpd} + 17.016936 * \text{fl} + 8.366404 * \text{thigh\_vol} + 5.828808 * \text{arm\_vol}$	0.9708	$-0.0001 \pm 180.9803$
NH 8 (3D sample)	$\text{weight} = -3626.314419 + 43.426744 * \text{bpd} + 23.645338 * \text{fl} + 11.414273 * \text{thigh\_vol}$	0.9698	$0 \pm 184.0439$

Table 8. Weight estimation dual formulas.

In Table 8, all dual formulas NHD \* are better than normal formulas NH \* with regard to R and error range. Moreover, NHD \* do not need too much regressors. Given 2D sample, NHD 1 and NHD 2 use 4 and 3 regressors including age regressor, respectively whereas both NH 3 and NH 4 uses 4 regressors. Given 3D sample, NHD 3 and NHD 4 use 6 and 5 regressors including age regressor, respectively whereas NH 7 and NH 8 use 5 and 3 regressors, respectively.

Although our formulas are better than all remaining ones with high adequacy (large R) and high accuracy (small error range), other researches are always significant because their formulas are very simple and practical. Moreover, our formulas are not global. If they are applied into other samples collected in other communities, their accuracy may be decreased and they may not be still better than traditional formulas such as Sherppard and Hadlock. However, it is easy to draw from our experimental results that if Phoebe framework is used for the same samples with other researches, it will always produce preeminent formulas. In

order to achieve global optimality with Phoebe framework, followings are two essential suggestions:

- Experimenting on Phoebe framework with many samples.
- Adding more knowledge of pregnancy study, ultrasound technique, and obstetrics into Phoebe framework. In other words, the additional knowledge will be modeled as constraints of SG algorithm.

These suggestions go beyond this research. For my opinion, we cannot reach absolutely the global optimality because Phoebe framework focuses on local optimality with specific communities. Essentially, the suggestions only alleviate the weak point of the built-in SG algorithm in global optimality.

## 6. Conclusions

According to experimental results, there is no doubt that Phoebe framework produces optimal formulas with high adequacy and accuracy; please see **Tables 4, 5, 6, 7, and 8** for more details. However we also recognize the weak point of our research is that the built-in SG algorithm can lose some good formulas due to the heuristic conditions. The suggestive solution is to add more constraints into such conditions; please read the article "A framework of fetal age and weight estimation" [10, pp. 24-25] for more details.

It is really difficult to apply our complex formulas for fast mental calculation because we must pay the price for their high accuracy. In the future, we will embed these formulas into software or hardware of medical ultrasound machine so that users are easy to read estimated values resulted from the machine. The research is available at <http://phoebe.locnguyen.net> so that doctors and researchers are easy to use. We do not know whether they have enjoyed our product. However, we presented Phoebe framework at the Annual Conference of Ho Chi Minh City Society of Reproductive Medicine (HOSREM) held on November 26, 2016, Ho Chi Minh city, Vietnam; so many doctors and researchers knew and concerned it.

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