#19: Program Sketching and CEGIS

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EECS 700: Introduction to Program Synthesis



Program Sketching

Search strategy

enumerative constraint-based deductive

Behavioral constraints

reference impl assertions types pre/post-conditions

Program space

imperative programs w/ loops
recursive functional programs
recursive pointer-manipulating programs

+ bounded guarantees

Constraint-based synthesis

Behavioral constraints

encoding

 $\exists C . spec(C)$

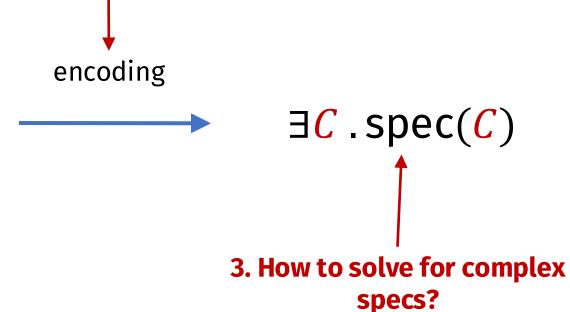
Structural constraints

CBS for complex programs

2. How to encode the behavior of complex programs?

Behavioral constraints
= assertions / reference
implementation

Structural constraints



1. How to specify for complex programs?

Program Sketching

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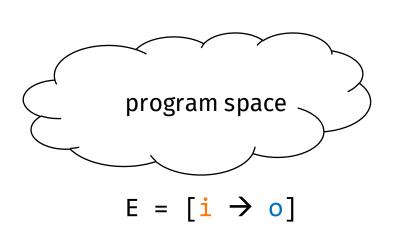
encoding $\exists C . \operatorname{spec}(C)$ \uparrow 3. How to solve for complex specs?

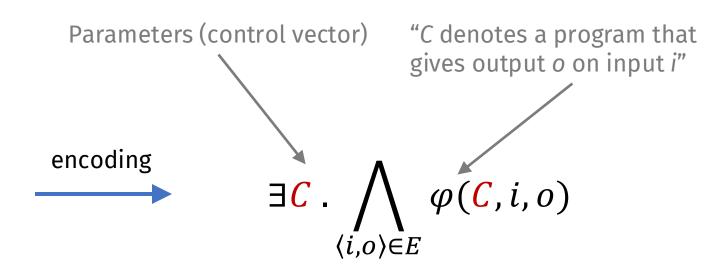
CEGIS

Symbolic execution

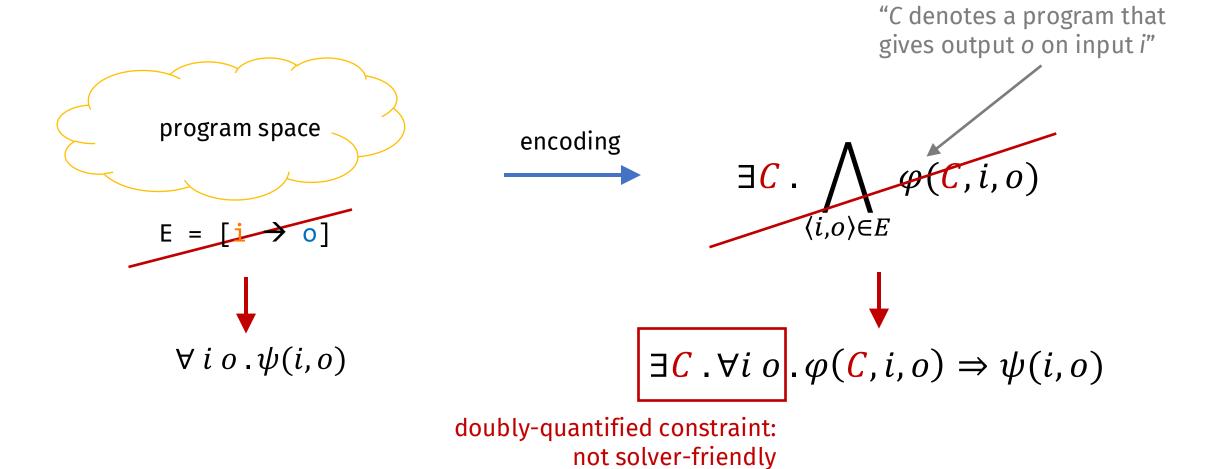
1. How to specify for complex programs? Sketches

CBS from examples





CBS from specifications



Example

```
harness void main(int x) { int y := ?? * x + ??; assert y - 1 == x + x; } \exists c_1 c_2 . \forall x \ y . \ y = c_1 * x + c_2 \\ \Rightarrow y - 1 = x + x \exists c_1 c_2 . \forall x \ y . \ y = c_1 * x + c_2 \exists c_1 c_2 . \forall x \ c_1 * x + c_2 - 1 = x + x
```

How do we solve this constraint?

 $\exists C . \forall i o . \varphi(C, i, o) \Rightarrow \psi(i, o)$

CEGIS

$$\exists c . \forall x . Q(c, x)$$

• Idea 1: Bounded Observation Hypothesis

• Assume there exists a small set of inputs $X = \{x_1, x_2, ... x_n\}$ such that

whenever c satisfies

$$\bigwedge_{i \in 1..n} Q(\mathbf{c}, x_i)$$

No quantifiers here, can give to SAT / SMT

$$\forall x. Q(c, x)$$

Example

$$\exists c_1c_2 . \forall x . c_1 * x + c_2 - 1 = x + x$$

$$Q(c_1, c_2, 0) \equiv c_2 - 1 = 0$$

$$Q(c_1, c_2, 1) \equiv c_1 + c_2 - 1 = 2$$

$$\{c_1 \rightarrow 2, c_2 \rightarrow 1\}$$

$$\begin{cases} c_1 \rightarrow 2, c_2 \rightarrow 1 \end{cases}$$

$$\begin{cases} \text{harness void main(int } x) \\ \text{int } y := 2 * x + 1; \\ \text{assert } y - 1 := x + x; \end{cases}$$

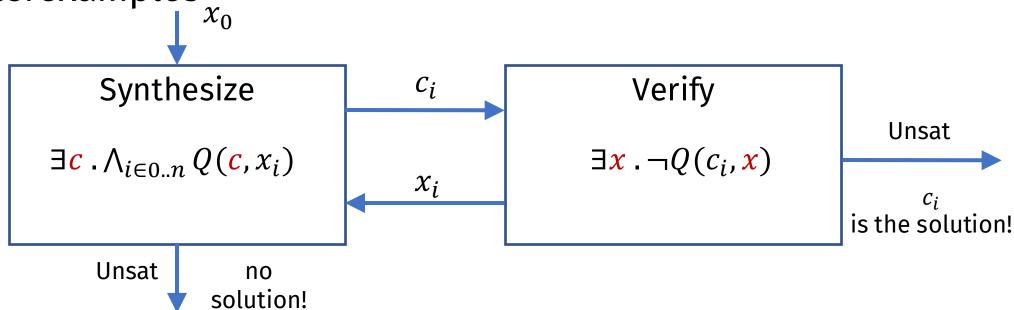
This is a linear constraint,

How do we find X in a general case?

CEGIS

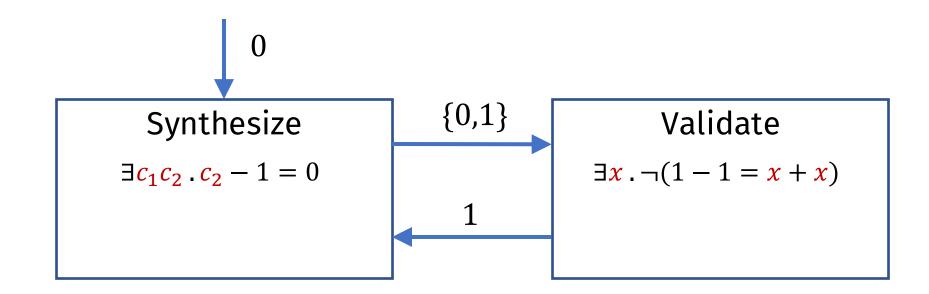
$$\exists c . \forall x . Q(c, x)$$

• Idea 2: Rely on verification oracle to generate counterexamples



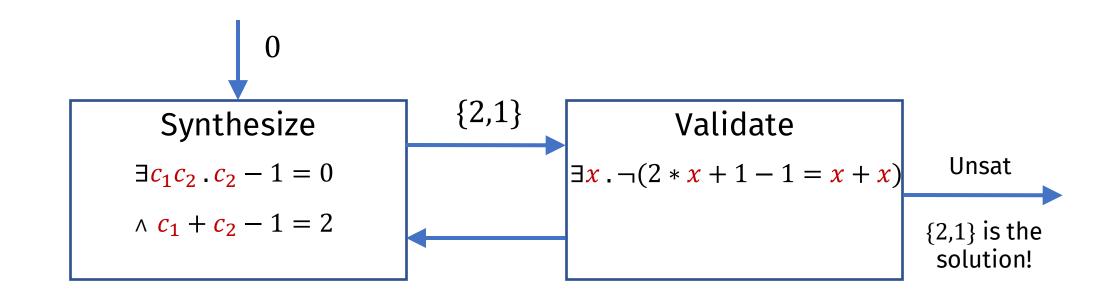
Example

$$\exists c_1 c_2 . \forall x . c_1 * x + c_2 - 1 = x + x$$



Example

$$\exists c_1 c_2 . \forall x . c_1 * x + c_2 - 1 = x + x$$



Program Sketching

2. How to encode the behavior of complex programs?

Behavioral constraints = assertions / reference implementation

Symbolic execution encoding

Structural constraints

 $\exists C . \forall x . Q(C, x)$

3. How to solve for complex specs?

CEGIS

1. How to specify for complex programs? Sketches

Structural constraints in Sketch

- Different constraints good for different problems
 - CFGs
 - Components
 - Just figure out the constants
- Idea: Allow the programmer to encode all kinds of constraints using... programs (duh!)

Language Design Strategy

Extend base language with one construct

Constant hole: ??

```
int bar (int x)
{
   int t = x * ??;
   assert t == x + x;
   return t;
}
int bar (int x)
{
   int t = x * 2;
   assert t == x + x;
   return t;
}
```

Synthesizer replaces ?? with a natural number

Constant holes → **sets of expressions**

- Expressions with ?? == sets of expressions
 - linear expressions
 - polynomials
 - sets of variables

```
x * ?? + y * ??
x * x * ?? + x * ?? + ??
?? ? x : y
```

Example: swap without a temporary

Swap two integers without an extra temporary

```
void swap(ref int x, ref int y){
    x = ... // sum or difference of x and y
    y = ... // sum or difference of x and y
    x = ... // sum or difference of x and y
}

harness void main(int x, int y){
    int tx = x; int ty = y;
    swap(x, y);
    assert x==ty && y == tx;
}
```

Syntactic sugar

• {| RegExp |}

- RegExp supports choice '|' and optional '?'
 - can be used arbitrarily within an expression

```
    to select operands
        {| (x | y | z) + 1 |}
    to select operators
        {| x (+ | -) y |}
    to select fields
        {| n(.prev | .next)? |}
    to select arguments
        {| foo( x | y, z) |}
```

- Set must respect the type system
 - all expressions in the set must type-check
 - all must be of the same type

Complex program spaces

- Idea: To build complex program spaces from simple program spaces, borrow abstraction devices from programming languages
- Function: abstracts expressions
- Generator: abstracts set of expressions
 - Like a function with holes...
 - ...but different invocations → different code

Example: swap without a temporary

```
generator int sign() {
   if ?? {return 1;} else {return -1;}
void swap(ref int x, ref int y){
   x = x + sign()*y; \rightarrow 1
   y = x + sign()*y;  \rightarrow -1
   x = x + sign()*y;
harness void main(int x, int y){
   int tx = x; int ty = y;
   swap(x, y);
   assert x==ty && y == tx;
```

Recursive generators

Can generators encode a CFG?

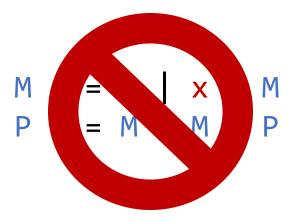
```
M ::= n | x * M
P ::= M | M + P
```

```
generator int mono(int x) {
    if (??) {return ??;}
    else {return x * mono(x);}
}

generator int poly(int x) {
    if (??) {return mono(x);}
    else {return mono(x) + poly(x);}
}
```

Recursive generators

 What if monomial of every degree can occur at most once?



```
generator int mono(int x, int n) {
   if (n <= 0) {return ??;}
   else {return x * mono(x, n - 1);}
}

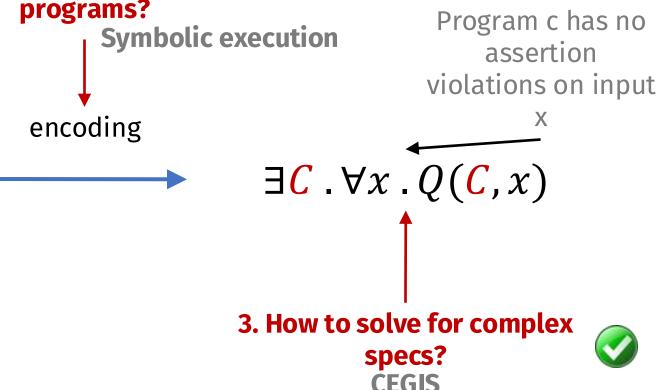
generator int poly(int x, int n) {
   if (n <= 0) {return mono(x,0);}
   else {return mono(x,n) + poly(x, n - 1);}
}</pre>
```

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