

Problem1:

1. The relation instance does not satisfy the functional dependency $AB \rightarrow C$ because when $A = B = 1$, there are two different values of C (2 and 3)
2. All functional dependencies that are satisfied by the given relation instance:
 $ABC \rightarrow ABC, ABC \rightarrow AB, ABC \rightarrow AC, ABC \rightarrow BC, ABC \rightarrow A, ABC \rightarrow B, ABC \rightarrow C$
 $AB \rightarrow ABC, AB \rightarrow AB, AB \rightarrow AC, AB \rightarrow BC, AB \rightarrow A, AB \rightarrow B, AB \rightarrow C$
 $AC \rightarrow AC, AC \rightarrow A, AC \rightarrow C$
 $BC \rightarrow ABC, BC \rightarrow AB, BC \rightarrow AC, BC \rightarrow BC, BC \rightarrow A, BC \rightarrow B, BC \rightarrow C$
 $A \rightarrow A$
 $B \rightarrow ABC, B \rightarrow AB, B \rightarrow AC, B \rightarrow BC, B \rightarrow A, B \rightarrow B, B \rightarrow C$
 $C \rightarrow AC, C \rightarrow A, C \rightarrow C$

Problem2:

1. $A \rightarrow B$ Given
2. $B \rightarrow C$ Given
3. $A \rightarrow C$ Transitivity of 1 and 2
4. $AB \rightarrow CB$ Augmentation of 3 with B

Problem3:

1. $X \rightarrow YZ$ given
2. $YZ \rightarrow Y$ Reflexivity $Y \subseteq YZ$
3. $YZ \rightarrow Z$ Reflexivity $Z \subseteq YZ$
4. $X \rightarrow Y$ Transitivity of 1 and 2
5. $X \rightarrow Z$ Transitivity of 1 and 3

Problem4:

Let $X = A, Y = B, Z = C$. Consider the following table:

A	B	C
1	2	1
1	2	2
2	3	3

According to the above table, $A \rightarrow B$ and $C \rightarrow B$ are satisfied but $A \rightarrow C$ is not.

Problem5:

1. The set of all functional dependencies that are entailed by F :
 Functional dependencies that are trivial:
 $ABC \rightarrow ABC, ABC \rightarrow AB, ABC \rightarrow AC, ABC \rightarrow BC, ABC \rightarrow A, ABC \rightarrow B, ABC \rightarrow C$
 $AB \rightarrow AB, AB \rightarrow A, AB \rightarrow B, AC \rightarrow AC, AC \rightarrow A, AC \rightarrow C, BC \rightarrow BC, BC \rightarrow B, BC \rightarrow C$
 $A \rightarrow A, B \rightarrow B, C \rightarrow C$
 Functional dependencies that are non-trivial:

AB→ABC, AC→ABC, AC→AB, AC→BC, AC→A, AB→AB, AB→B

2. Superkeys are: ABC, AC, BC
Candidate keys are: AC, BC

Problem6:

1. A is the superkey of ABC and ADE ⇒ (A,B,C) and (A,D,E) is a lossless-join decomposition of R
2. C is neither the superkey of ABC or CDE ⇒ (A,B,C) and (C,D,E) is not a lossless join decomposition of R
3. (B,D) and (A,B,C,E)

Problem7:

1. key of V is: (Date,P#)
2. V is not BCNF because there are three functional dependencies whose left-hand-side are not superkey:
P#→Pname, E#→Ename, Diagnosis→Cost
3. V1=(Date, P#, Pname) is not BCNF because the functional dependency P#→Pname whose left-hand-side is not a superkey
4. V2=(Date, E#, Ename, Diagnosis, Cost) is not BCNF because its functional dependencies (Diagnosis→Cost), (E#→Ename) whose left-hand-sides are not superkey
5. V1 and V2 is not a lossless-join decomposition because its common attribute (Date) neither the superkey of V1 nor V2
6. (Diagnosis, Cost), (E#,Ename), (P#,Pname), (Date,P#, E#,Diagnosis)

Problem8:

1. PatId→PatName,
SurgId→SurgName
(SurgId, AppDate) → SurgLoc
(AppDate, SurgLoc) → SurgId
(PatId, AppDate, AppTime) → SurgLoc
(SurgLoc, AppDate, AppTime) → PatId
(SurgId, AppDate, AppTime) → PatId
(PatId, AppDate, AppTime) → SurgId
2. Negative aspects of the initial relation:
 - Waste of space when PatId is repeated unnecessarily in the (PatId, AppDate, AppTime) → SurgLoc and (PatId, AppDate, AppTime) → SurgId
 - Multiple updates to if AppTime or AppDate changes
 - Waste of space when SurgId is repeated unnecessarily in the (SurgId, AppDate) → SurgLoc and (SurgId, AppDate, AppTime) → PatId
- 3.

(PatId, PatName), (SurgId, SurgName), (SurgId, AppDate, SurgLoc), (PatId, SurgId,
AppDate, AppTime)