#### **Section 1: Cartesian Products**

The result of a Cartesian Product is an ordered pair, such as (a, b) – like what you would see in Algebra.

For some sets of numbers A and B, the result of  $A \times B$  will be a combination of all of each set's elements together.  $A \times B = \{(a,b) : a \in A, b \in B\}$ 

For example, for  $A = \{ 1, 2 \}$  and  $B = \{ 4, 5, 6 \}$ , The elements of  $A \times B$  are:

B → A ↓	4	5	6
1	(1,4)	(1,5)	(1,6)
2	(2,4)	(2,5)	(2,6)

**So**  $A \times B = \{(1,4), (1,5), (1,6), (2,4), (2,5), (2,6)\}$ 

1. Given the following sets, calculate each Cartesian Product. Write it out as a table, like above.  $A = \{1, 2\}$   $B = \{3, 4\}$ 

a.  $A \times B$  (\_\_\_/2)

$\begin{array}{ccc} B & \rightarrow & \\ A & \downarrow & \end{array}$	3	4
1		
2		

**b.**  $B \times A$  (\_\_\_/2)

$\begin{array}{ccc} A & \rightarrow \\ B & \downarrow \end{array}$	1	2
3		
4		

2. Calculate the Cartesian Product. Write it out as a table.

$$A = \{ 2, 4, 6 \}$$
  $B = \{ 1, 3 \}$ 

a.  $A \times B$  (\_\_/2)

$\begin{array}{ccc} B & \rightarrow & \\ A & \downarrow & \end{array}$	1	3
2		
4		
6		

**b.** *B*×*A* (\_\_\_/2)

$\begin{array}{c} A \rightarrow \\ B \downarrow \end{array}$	2	4	6
1			
3			

3. Calculate the Cartesian Products. Write it out as a set of coordinate pairs.

$$A = \{ 2, 4 \}$$

$$B = \{ 1, 3 \}$$

$$C = \{ 3, 4, 5, 6 \}$$

a.  $A \times B$  (\_\_\_/2)

**b.**  $A \times C$  (\_\_/2)

c.  $B \times C$  (\_\_/2)

d.  $C \times B$  (\_\_\_/2)

e. 
$$A^2$$
 (aka  $A \times A$  ) (\_\_\_/2)

4. For the given sets, find the intersections, unions, and differences.

$$A = \{1\}$$
  $B = \{3,5,7\}$   $C = \{3,5,9,11\}$   $A \times B = \{(1,3),(1,5),(1,7)\}$   $A \times C = \{(1,3),(1,5),(1,9),(1,11)\}$ 

**a.**  $(A \times B) - (A \times C)$  remember, the result is the first set's elements, but none of the elements that are shared by the second set. (\_\_\_/2)

**b.** 
$$(A \times C) - (A \times B)$$

c. 
$$A \times (B \cup C)$$

**d.** 
$$A \times (B \cup C) \cap (A \times B)$$

e. 
$$(A \times B) \cup (A \times C)$$

# **Section 2: Partitions**

The Partition of a together, form the	a set, usually denoted by <b>S</b> , is a set of subsets that, when co ne original set.	mbined
Definition: For a set A, a par called a part of S	rtition of A is a set $S = \{ S_{1,}S_{2,}S_{3,} \}$ of subsets of A (each so), such that:	set $S_i$ is
2. For all <i>i</i> and nothing in comm		rts have
1 2 3		{3, 4} }
_	n be any combination of subsets of whatever size, so long as sted in the partition.	all elements
5. For the given set,	write out all possible partitions. $A = \{1, 2\}$	(/1
Partition 1:	Partition 2:	
=	write out all possible partitions. $\mathbf{B} = \{1, 2, 3\}$ . Remember that set do not matter. ( $\{\{2, 3\}, \{1\}\}$ and $\{\{1\}, \{2, 3\}\}$ is the same	·
Partition 1:	Partition 2:	
Partition 3:	Partition 4:	
Partition 5:		

 $(_{/2})$ 

answer).	$A = \{ 1, 2, 3, 4, 5, 6 \}$		
a. Find a partition	where each part has the same s	size.	(/1)
b. Find a partition	where no two parts have the sa	ime size.	(/1)
c. Write out the pa	artition that has as many parts a	as possible.	(/1)
d. Write out the pa	artition that has as few parts as	possible.	(/1)
8. Which of the foll	lowing are partitions of the set A	A = { 1, 2, 4, 8, 16, 32, 64, 12	8 }? For those that

7. For the given set, find partitions that meet the requirements. (There could be more than one

are not, explain why.

a. { 1, 2, { 4, 8, 16 }, { 32, 64, 128 } }

### **Section 3: Power Sets**

The Power Set of A is defined as  $\wp(A) = \{S : S \subseteq A\}$  . For example, A =  $\{1, 2, 3, 4\}$ ,  $\wp(A)$ 

$$= \{ \emptyset, \{1\}, \{2\}, \{3\}, \{4\}, \{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 3\}, \{2, 4\}, \{3, 4\}, \{1, 2, 3\}, \{1, 2, 4\}, \{1, 3, 4\}, \{2, 3, 4\}, \{1, 2, 3, 4\} \}$$

Essentially, all the possible subsets of A.

As a simpler example, the Power Set  $\wp(\{1\}) = \{ \emptyset, \{1\} \}$ 

#### 9. Find the Power Set for each set.

**a.** 
$$\wp(\{1,2\})$$
 (\_\_\_/1)

**b.** 
$$\wp({3,4})$$

c. 
$$\wp(\{1,2,3\})$$

#### **Team Members:**

1. 2.

3. 4.

**Section:** TR 12:30 pm T 6:00 pm

#### Team Rules:

- Work through these exercises with a team in class.
- **Only one answer sheet will be turned in.** Each member of the team will receive the same score.

#### **Work Rules:**

- Fill out your answers on the **answer sheet!**
- Write cleanly and linearly! If I can't make sense of your solution, you won't get credit. You can also type out your answers if you'd prefer.
- Write out each step If I can't see the logic you used to get from one step to another, you might get points off.
- <u>Don't scribble out cancellations</u> I can't read that. If a numerator / denominator cancel out, or if there is a +/- that cancels out, don't scribble just use a single slash, or add an extra step!

#### **Grading:**

Each question as a weight, and all questions can receive a score between 0 and 4:

Nothing written	Something attempted, but incorrect	Partially correct, but multiple errors.	Mostly correct, with one or two errors.	Perfect. Correct answer and notation
0	1	2	3	4

# **Answer Sheet**

Exercise 1a				(/2)
$\begin{array}{ccc} B & \rightarrow & \\ A & \downarrow & \end{array}$	3	•	4	
1				
2				
Exercise 1b		1		(/2)
$\begin{array}{c} A \rightarrow \\ B \downarrow \end{array}$	1		2	
3				
4				
Exercise 2a		1		(/2)
$\begin{array}{c} A \rightarrow \\ B \downarrow \end{array}$	1		3	
2				
4				
6				
Exercise 2b		I		(/2)
$\begin{array}{ccc} A & \rightarrow \\ B & \downarrow \end{array}$	2	4	6	
1				
3				

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Exercise 3a (\_\_\_/2)

 $A \times B =$ 

Exercise 3b (\_\_\_/2)

 $A \times C =$ 

Exercise 3c (\_\_\_/2)

 $B \times C =$ 

Exercise 3d (\_\_\_/2)

 $C \times B =$ 

Exercise 3e (\_\_\_/2)

 $A^2 =$ 

Exercise 4a  $(A \times B) - (A \times C)$  (\_\_\_/2)

Exercise 4b  $(A \times C) - (A \times B)$  (\_\_\_/2)

Exercise 4c  $A \times (B \cup C)$  (\_\_/2)

Exercise 4d  $A \times (B \cup C) \cap (A \times B)$  (\_\_\_/2)

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Exercise 5	(/1)
Partition 1:	
Partition 2:	
Exercise 6	(/2)
Partition 1:	
Partition 2:	
Partition 3:	
Partition 4:	
Partition 5:	
Exercise 7a	(/1)
Exercise 7b	(/1)
Exercise 7c	(/1)
Exercise 7c	(/1)

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Exercise 8a	/	2)	
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Exercise 9a 
$$\wp(\{1,2\})$$
 (\_\_\_/1)

Exercise 9b 
$$\wp({3,4})$$
 (\_\_/1)

Exercise 9c 
$$\wp(\{1,2,3\})$$
 (\_\_/2)