

Answer Key

1.
 - a. $9 \bmod 7$
 $9 \bmod 7 = 2; \quad 9 = 7 \cdot 1 + 2$
 - b. $5 \bmod 2$
 $5 \bmod 2 = 1; \quad 5 = 2 \cdot 2 + 1$
 - c. $15 \bmod 3$
 $15 \bmod 3 = 0; \quad 15 = 3 \cdot 5 + 0$
 - d. $-7 \bmod 2$
 $-7 \bmod 2 = 1; \quad -7 = 2 \cdot -4 + 1$
2.
 - a. If a divides b and a divides c , then a divides $b + c$.¹
 $b = ak, c = aj \quad \Rightarrow b + c = ak + aj \quad \Rightarrow a(k + j)$
 - b. If a divides b and c divides d , then ac divides bd .²
 $b = ak, d = cj \quad \Rightarrow bd = (ak)(cj) \quad \Rightarrow (ac)(kj)$

¹From Discrete Mathematics by Ensley and Crawley

²From Discrete Mathematics by Ensley and Crawley