Chapter 1.3 In-class Exercise

Info: In-class exercises are meant to introduce you to the new topics of this chapter of the book. Each part will have an introductory description of the content and example(s), followed by practice problems for you to work on.

These assignments are **team assignments** - your team will turn in *one* copy of the exericse. It is up to your team how to appropach the assignments; you can work separately and then check your work together, or you can collaborate on the assignment together.

Work must be clean; points may be deducted if the instructor cannot read the work.

Chapter 1.3 In-class Exercise Instructions

This is the instruction page, make sure to fill out your answers in the worksheet later in the document

1. Propositional Logic

A **proposition** is a statement which has truth value: it is either true (T) or false (F).

The statement doesn't have to necessarily be TRUE, it could also be FALSE, but it has to be unambiguously so.

Statement	Proposition?	Result?
2 + 3 = 5	Yes	True
2 + 2 = 5	Yes	False
This class has 30 students	Yes	$False^b$
Is the movie good?	No	

 $[^]a {\rm From\ https://en.wikibooks.org/wiki/Discrete_Mathematics/Logic}$ $^b {\rm Probably:)}$

Question 1 _____ / 8%

For the following, mark whether the statement is a **proposition** and, if it is, mark whether it is **true** or **false**.

- a. 10 + 20 = 30.
- b. $2 \cdot a$ is always even.
- c. Is 4 < 5?
- d. Pineapple belongs on pizza.¹

¹I'm not going to count off points whether you say true or false:)

2. Compound Propositions

We can also create a **compound proposition** using the logical operators for AND \wedge , OR \vee , and NOT \neg . When we're writing out a compound proposition, we will usually assign each proposition a **propositional** variable.

If we have the propositions p is the proposition "Paul is taking discrete math", q is the proposition, "Paul has a calculator", then we can build the compound propositions like:

 $p \wedge q$: Paul is taking discrete math and Paul has a calculator

 $p \vee q$: Paul is taking discrete math or Paul has a calculator

 $\neg p$: Paul is NOT taking discrete math

 $\neg q$: Paul does NOT have a calculator

The result of a compound proposition depends on the value of each proposition it is made up of:

- 1. A compound proposition $a \wedge b \wedge c$ is **only true** if all propositions are true; it will be **false** if one or more of the propositions is false.
- 2. A compound proposition $a \lor b \lor c$ is **true** if one or more of the propositions is true; it is **only false** if all propositions are false.
- 3. A compound proposition $\neg a$ is **true** only if the proposition is false; it is only **false** if the proposition is true.

Question 2 $___/24\%$

Given the following compound propositions and proposition values, write out whether the full compound proposition is **true** or **false**.

a AND b:

	Compound	Values	Result
a.	$a \wedge b$	a = true, b = true	
b.	$a \wedge b$	a = true, b = false	
c.	$a \wedge b$	a = false, b = true	
d.	$a \wedge b$	a = false, b = false	

a OR b:

	Compound	Values	Result
e.	$a \lor b$	a = true, b = true	
f.	$a \lor b$	a = true, b = false	
g.	$a \lor b$	a = false, b = true	
h.	$a \lor b$	a = false, b = false	

Combinations:

	Compound	Values	Result
i.	$a \wedge \neg b$	a = true, b = false	
j.	$a \vee \neg b$	a = false, b = true	
k.	$\neg a \wedge b$	a = false, b = true	
l.	$\neg a \lor b$	a = false, b = false	

Question 3 _____ / 40%

For the following, "translate" the following English statements into compound propositions.

- p: "The printer is offline"
- q: "The printer is out of paper"
- r: "The document has finished printing"
- a. The printer is not out of paper.
- b. The printer is online.
- c. The printer is offline and it is out of paper
- d. The printer is online and it is not out of paper.
- e. Either the printer is online, or it is out of paper.
- f. The printer is online, but it is out of paper.
- g. The printer is offline or it is out of paper, but not both.
- h. The printer is online and the printer has paper, and the document has not finished printing.

3. Truth tables

When we're working with compound propositional statements, the result of the compound depends on the true/false values of each proposition it is built up of.

We can diagram out all possible states of a compound proposition by using a **truth table**. In a truth table, we list all propositional variables first on the left, as well as all possible combinations of their states, and then the compound statement's result on the right.

p	q	$p \wedge q$
Т	Т	T
Т	F	F
F	Т	F
F	F	F

p	q	$p \wedge q$
Τ	Т	Т
Т	F	F
F	Т	F
F	F	F

Question 4
Complete the following truth tables.

_____ / 12%

	p	q	$\neg q$	$p \land \neg q$
	T	Т	F	
a.	Т	F	T	
	F	Т		
	F	F		

	p	q	$\neg p$	$\neg q$	$\neg p \lor \neg q$
	Τ	Т			
b.	Т	F			
	F	Т			
	F	F			

When you're building out truth tables, there is a specific order you should write out the "T" and "F" states. Begin with all "T" values first, and work your way down to all "F" values first. As you go, change the right-most state from "T" to "F", working your way from right-to-left.

So with two variables: "TT", "TF", "FT", "FF".

Question 5 _____ / 6%

Using the rules above, write out all the states for a truth table with three propositional variables.

p	q	r
T	T	Т
Т	Т	F
T		
Т	F	F
F		
F		
F		
F	F	F

Whenever the final columns of the truth tables for two propositions p and q are the same, we say that p and q are logically equivalent, and we write: $p \equiv q$.

 $^a {\it From\ https://en.wikibooks.org/wiki/Discrete_Mathematics/Logic}$

Question 6 _____ / 10%

Use a truth table to show that the compound propositions,

 $\neg p \land \neg q$ and $\neg (p \lor q)$

are logically equivalent. The final two columns are the compound propositions above.

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p	q		$\neg p$	$\neg q$	$(p \lor q)$	$\neg p \land \neg q$	$\neg(p \lor q)$
Т	Т		F	F			
Т	F		F	Τ			
F	Т		Т	F			
F	F		Т	Т			

Chapter 1.3 In-class Exercise Worksheet

2.

4.

Team: Please write down all people in your team.

Section:

1. 3.

 \square MW 4:30 - 5:45 pm \square M 6:00 - 8:50 pm \square TR 2:00 - 3:15 pm

Team rules:

- Only one worksheet will be turned in per team. Each member of the team will receive the same score.
- You can collaborate on the exercise together, or you can work separately
 and then compare your answers with your team as you fill out the turnin worksheet.

Work rules:

- Fill out your answers on this answer sheet.
- Write cleanly and linearly if I can't make sense of your solution then you won't get credit.
- Write out each step (within reason) if I can't see the logic you followed to get to your answer, you may get points taken off.
- Don't scribble out cancellations I can't read that. For example, if a numerator/denominator cancel out, or a +/- cancels out, don't scribble out the numbers just use a single slash!

Grading: The total amount of points for an in-class exercise is 5 points each. Each question will have a weight assigned to it, and will be given a a point value between 0 and 4:

0	Nothing written
1	Something written, but incorrect
2	Partially correct, but multiple errors
3	Mostly correct, with one or two errors
4	Perfect; correct answer and notation

Answer sheet

For the	question 1: Properties of the following, ark whether is	mark wh	ether the s	statem	nent is a			$\square 2 \square 3$ on and,	
a.	10 + 20 = 3	0.							
b.	$2 \cdot a$ is alway	s even.							
c.	Is $4 < 5$?								
d.	Pineapple be	elongs on	pizza.						
Given	Question the following the full control	g compou	nd proposi	tions a		osition		□2□3	
a.		b		с.			d.		
e.		f		g.			h.		
i.		j		k.			1.		
_									
For the pound p : "T	9% Question he following, d proposition The printer is The document	"transla s. offline",	te" the fol q : "The p	lowing orinter		h stat	emen	$\square \ 2 \ \square \ 3$ ts into	
a	ı.			b.					
C	2.			d.					
е).			f.					

h.

e.

g.

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12%	Question	4:	Truth	tables

|--|

	p	q	$\neg q$	$p \land \neg q$
	Τ	Τ	F	
a.	Т	F	Τ	
	F	Τ		
	F	F		

	p	q	$\neg p$	$\neg q$	$\neg p \lor \neg q$
	Τ	Τ			
b.	Т	F			
	F	Т			
	F	F			

6% Question 5: States

_	\circ	_	4	_	0	_	0	_	4
- 1 1	()	П		11	2	ΙI	.3	- 1 1	-4

Write out all the states for a truth table with three propositional variables.

p	q	r
T	Т	T
T	Т	F
T		
Т	F	F
F		
F		
F		
F	F	F

10% Question 5: Logically equivalent \Box 0 \Box 1 \Box 2 \Box 3 \Box 4 Use a truth table to show that the compound propositions,

$$\neg p \land \neg q$$
 and $\neg (p \lor q)$

are logically equivalent. The final two columns are the compound propositions above.

p	q	$\neg p$	$\neg q$	$(p \lor q)$	$\neg p \land \neg q$	$\neg (p \lor q)$
Τ	Т	F	F			
Т	F	F	Τ			
F	Т	Τ	F			
F	F	Τ	Т			

Grading

Question	Weight	0-4	Adjusted score
1	8%		
2	24%		
3	40%		
4	12%		
5	6%		
6	10%		