

## Answer Key

1.
  - a. Is a proposition, is true.
  - b. Is a proposition, is true.
  - c. Not a proposition - it is a question.
  - d. Not a proposition - it is an opinion.
  - e. Not a proposition - because of variables, it is not unambiguously true or false.
  - f. Is a proposition, is false.
2.
  - a. a AND b:

Compound	Values	Result
a. $a \wedge b$	$a = \text{true}, b = \text{true}$	TRUE
b. $a \wedge b$	$a = \text{true}, b = \text{false}$	FALSE
c. $a \wedge b$	$a = \text{false}, b = \text{true}$	FALSE
d. $a \wedge b$	$a = \text{false}, b = \text{false}$	FALSE

- b. a OR b:

Compound	Values	Result
e. $a \vee b$	$a = \text{true}, b = \text{true}$	TRUE
f. $a \vee b$	$a = \text{true}, b = \text{false}$	TRUE
g. $a \vee b$	$a = \text{false}, b = \text{true}$	TRUE
h. $a \vee b$	$a = \text{false}, b = \text{false}$	FALSE

- c. Compound:

Compound	Values	Result
i. $a \wedge \neg b$	$a = \text{true}, b = \text{false}$	TRUE
j. $a \vee \neg b$	$a = \text{false}, b = \text{true}$	FALSE
k. $\neg a \wedge b$	$a = \text{false}, b = \text{true}$	TRUE
l. $\neg a \vee b$	$a = \text{false}, b = \text{false}$	TRUE

3.  $m$ : There is milk in the fridge,  $e$ : There are eggs in the fridge,  $c$ : There is cheese in the fridge.
  - a. There is milk in the fridge, or there is cheese in the fridge.  
 $m \vee c$
  - b. There is milk in the fridge, or there is cheese in the fridge, but not both.  
 $(m \vee c) \wedge (\neg m \vee \neg c)$  or  
 $(m \vee c) \wedge \neg(m \wedge c)$ .

c. There is milk in the fridge but there are no eggs in the fridge.

$$m \wedge \neg e$$

d. There is milk in the fridge and there is either cheese or eggs in the fridge.

$$m \wedge (e \vee c)$$

e. There is not milk in the fridge and there is not cheese in the fridge.

$$\neg m \wedge \neg c$$

f. It is not true that... there is milk or cheese in the fridge.

$$\neg(m \vee c)$$

g. There is not milk in the fridge or there is not cheese in the fridge.

$$\neg m \vee \neg c$$

h. It is not true that... there is milk and cheese in the fridge.

$$\neg(m \wedge c)$$

4a.

$p$	$q$		$\neg q$	$p \wedge \neg q$
T	T		F	F
T	F		T	T
F	T		F	F
F	F		T	F

4b.

$p$	$q$		$\neg p$	$\neg q$	$\neg p \vee \neg q$
T	T		F	F	F
T	F		F	T	T
F	T		T	F	T
F	F		T	T	T

5.

$p$	$q$	$r$
T	T	T
T	T	F
T	F	T
T	F	F
F	T	T
F	T	F
F	F	T
F	F	F

6.

$p$	$q$		$\neg p$	$\neg q$	$(p \vee q)$		$\neg p \wedge \neg q$		$\neg(p \vee q)$
T	T		F	F	T		T		T
T	F		F	T	T		F		F
F	T		T	F	T		F		F
F	F		T	T	F		F		F