

Running trials in code

Let's write a recursive function to run these types of trials for us and get a simulated average value.

In Visual Studio create a new **Empty Project**, and add one source file to it. Make sure to include the following libraries:

```
#include <iostream>    // output
#include <cstdlib>     // random
#include <ctime>       // time
using namespace std;  // standard library
```

Start with the following shell function:

```
int RunTrial( int min, int max, int stopAtFirst, int trialCount )
{
}
```

And main():

```
int main()
{
    srand( time( NULL ) );
    int min, max, stopAtFirst, count;

    return 0;
}
```

Starter code

```
1 #include <iostream>      // output
2 #include <cstdlib>       // random
3 #include <ctime>         // time
4 using namespace std;    // standard library
5
6 int RunTrial(    int min, int max,
7                 int stopAtFirst, int trialCount )
8 {
9 }
10
11 int main()
12 {
13     // seed the random # generator
14     srand( time( NULL ) );
15     int min, max, stopAtFirst, count;
16
17     return 0;
18 }
```

In C++, you can display text to the screen with a `cout` statement...

```
cout << "Message";
```

And you can get input with a `cin` statement, storing it in a variable...

```
cin >> min;
```

Get user input: Ask the user to enter the **Minimum value**, **Maximum value**, **Which value to stop at**, and **How many times to run it**. Store these in the variables declared at the top of `main()`.

When running the program, the user can enter the following to simulate a die roll or a coin flip:

	min	max
Die	1	6
Coin	1	2

Total trials: Create an integer variable that will store the total amount of trials that were run across all experiments. Make sure to initialize it to 0.

Experiment run: After getting the user's input, you will need to write a for-loop to run the experiment the specified amount of times.

Calling the function: Within the for-loop, you will call the `RunTrial` function. The output of this function is the total amount of trials that were ran before getting the specified value for the first time. You will add this value onto the `totalTrials` variable.

Calculating the average: Once the experiments has completed (the for-loop is over), you will calculate the average amount of trials that were ran. Create a float variable called `average` and divide the `totalTrials` by the `count`. Make sure you're doing float division or it won't turn out correctly.

See the next page for the `main()` code so far.

```
1  int main()
2  {
3      // seed the random # generator
4      srand( time( NULL ) );
5      int min, max, stopAtFirst, count;
6
7      cout << "Minimum value: ";
8      cin >> min;
9
10     cout << "Maximum value: ";
11     cin >> max;
12
13     cout << "Stop at what: ";
14     cin >> stopAtFirst;
15
16     cout << "How many times to run: ";
17     cin >> count;
18
19     int totalTrials = 0;
20
21     for ( int i = 0; i < count; i++ )
22     {
23         cout << endl;
24         cout << "Running trial set " << i << "... \t";
25         int trials = RunTrial( min, max,
26                               stopAtFirst, 1 );
27         totalTrials += trials;
28         cout << "\t" << trials << " trials ran";
29     }
30
31     float averageTrials =
32         float( totalTrials ) / float( count );
33
34     cout << "Average trials ran: " << averageTrials
35         << endl << endl;
36
37     return 0;
38 }
```

Now to work on the recursive function.

```
int RunTrial( int min, int max, int stopAtFirst, int trialCount )
{
}
```

A **Recursive Function** is a function that will call itself until the job is done. It is useful for breaking a problem into pieces.

At the top of this function, you will get a random value with the following:

```
// Get a random value between MIN and MAX, inclusive
int diff = (max + 1 - min);
int n = rand() % diff + min;
cout << n << " ";
```

Recursive functions need a **Base-case**, which is the scenario where it will end. In our case, the function stops once we get the **stopAtFirst** value. Use an if statement to check if the value of **n** is equal to **stopAtFirst**. If it is, return the current value of the **trialCount**.

Otherwise, we will call the recursive function. All the variables are the same, except we add 1 to the trial count.

```
return RunTrial( min, max, stopAtFirst, trialCount + 1 );
```

Altogether, it will look like this:

```
1  int RunTrial( int min, int max,
2      int stopAtFirst, int trialCount )
3  {
4      int diff = (max + 1 - min);
5      int n = rand() % diff + min;
6
7      cout << n << " ";
8
9      if ( n == stopAtFirst ) // Base case
10     {
11         return trialCount;
12     }
13
14     return RunTrial( min, max,
15         stopAtFirst, trialCount + 1 );
16 }
```

When the program is run, we can execute the experiment a large amount of times to see if the average that comes out is close to the expected value we calculate.

```
Minimum value: 1
Maximum value: 2
Stop at what: 1
How many times to run: 10000

(...)

Running trial set 9989... 1 1 trials ran
Running trial set 9990... 1 1 trials ran
Running trial set 9991... 1 1 trials ran
Running trial set 9992... 1 1 trials ran
Running trial set 9993... 1 1 trials ran
Running trial set 9994... 2 2 2 1 4 trials ran
Running trial set 9995... 2 1 2 trials ran
Running trial set 9996... 2 2 1 3 trials ran
Running trial set 9997... 2 1 2 trials ran
Running trial set 9998... 2 2 1 3 trials ran
Running trial set 9999... 2 1 2 trials ranAverage
trials ran: 2.0233
```

From the example above, our $E[X]$ was 2, so this is pretty close.