Chapter 5.1 In-class Exercise

Info: In-class exercises are meant to introduce you to the new topics of this chapter of the book. Each part will have an introductory description of the content and example(s), followed by practice problems for you to work on.

These assignments are **team assignments** - your team will turn in *one* copy of the exericse. It is up to your team how to appropach the assignments; you can work separately and then check your work together, or you can collaborate on the assignment together.

Work must be clean; points may be deducted if the instructor cannot read the work.

Chapter 5.1 In-class Exercise Instructions

This is the instruction page, make sure to fill out your answers in the worksheet later in the document

1. Review: Sets

In CS 210, chapter 3, we worked with **sets** and their properties. When we work with finite sets, there is a limited amount of elements in the set, and it can be written out.

Elements of a set are contained within curly braces $\{ \}$, and are separated by commas. Example: $\{1,2,3\}$.

Additionally, repeated elements in a set does not make it unique from an otherwise same set without the duplicates. In other words, $\{1, 1, 2, 3, 5\}$ is the same as $\{1, 2, 3, 5\}$.

Additionally, order is not important with sets.

- a. The subset of U that contains all the even numbers.
- b. The subset of U that contains all the prime numbers.
- c. The subset of U that contains all the odd numbers less than 4.

2. Types of ordering

For some types of data, we care about the ordering, and for others, we do not. For example, with the above problems, we don't care about the order of numbers listed for our subsets. In other cases, we might care about the order of our elements. For this section, we will look at data and decide whether it should be in an **ordered list** or an **unordered list**.

Question 2 _____ / 8%

At The Ordered Cinema, customers are required to enter in their heights while buying tickets. In any given column of movie seats, customers must be seated according from shortest (in front, at the beginning of the set) to tallest (in back, at the end of the set).

The heights of several patrons awaiting seating are: $\{5'5'', 5'4'', 6'0'', 4'9''\}$

If there are only 2 seats available in each column, how many different ways could these customers be ordered in 2 seats? (Assume other customers will be seated in a different column.)

An ordered list Is a finite list where sequence order matters.

An unordered list Is a finite list where sequence order does not matter.

3. Combinations and Permutaions

Combination In mathematics, a combination is a way of selecting items from a collection, such that (unlike permutations) the order of selection does not matter. a

Permutation In mathematics, the notion of permutation relates to the act of arranging all the members of a set into some sequence or order, or if the set is already ordered, rearranging (reordering) its elements, a process called permuting. These differ from combinations, which are selections of some members of a set where order is disregarded. For example, written as tuples, there are six permutations of the set $\{1,2,3\}$, namely: (1,2,3), (1,3,2), (2,1,3), (2,3,1), (3,1,2), and (3,2,1).

^aFrom https://en.wikipedia.org/wiki/Combination

^bFrom https://en.wikipedia.org/wiki/Permutation

Question 3 _____ / 23%

Four students are buying folders from the campus bookstore, and each need three folders each for English, Discrete Structures, and Biology. Folders are available in different colors: white, green, red, and blue. Each student chooses their folders in different ways: ¹

Uyriah: Grabbed 3 folders without consideration for color.

Orlando: Chose folders in order: First English, second Discrete Structures, and third Biology.

Connie: Chose folders of 3 different colors, but doesn't matter which color for what class.

Pete: Selected folders in order by class like Orlando, and chose separate colors for each like Connie.

- a. In this model, how many different colors were available at the bookstore?
- b. How many folders would each student choose?
- c. In the table below, indicate which student's selection corresponds with each of the two dimensions. (Put the student's initial in the table on the worksheet.)

		Did the order of selection matter		
		YES	NO	
Was color repetition allowed?	YES			
was color repetition anowed:	NO			

- d. For which students were repeating colors acceptable?
- e. For which students were repeating colors not acceptable?
- f. Which students' selections would be an ordered list?
- g. Which students' selections would be an unordered list?

¹Question originally from Jim Van Horn's POGIL exercises

These types of sequences where repetition is not allowed are known are called **permutations** and **combinations**. For permutations the order is important.

- h. Which student's selections demonstrate a permutations?
- i. Which student's selections demonstrate a combination?

Hint: These student names correspond with the representations... Unordered, Ordered, Permutation, and Combination.

When we're flipping a coin, there are two possible outcomes: *heads* or *tails*. If we flip more than one coin, then we end up with more possible outcomes. For example, when flipping two coins, we have four possible outcomes:

	First coin	Second coin
1.	HEADS	HEADS
2.	HEADS	TAILS
3.	TAILS	HEADS
4.	TAILS	TAILS

In this case, order matters and (H,T) is a different result from (T,H).

Question 4 _____ / 14%

We have a pool of four people, {Andrew, Bob, Carly, Diane}, and two prizes will be distributed between two of these people. ²

a. Assuming that prize #1 and prize #2 are different, list out all the ways the prizes can be distributed (i.e., permutations).

Example: (A, A), (A, B), (B, A), ...

b. Assuming that prize #1 and price #2 are both the same, list out all the ways the prizes can be distributed (i.e., sets).

Note: $\{A, B\}$ and $\{B, A\}$ would be considered the same.

²Based on Practice Problem 2 from Discrete Mathematics, Ensley & Crawley

All possible outcomes of rolling a red 6-sided die and a green 6-sided die, in an organized way:

	Green 1	Green 2	Green 3	Green 4	Green 5	Green 6
Red 1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(1,6)
Red 2	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)	(2,6)
Red 3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)
Red 4		(4,2)	(4,3)	(4,4)	(4,5)	(4,6)
Red 5	(5,1)		(5,3)	(5,4)	(5,5)	(5,6)
Red 6	(6,1)	(6,2)	(6,3)	(6,4)	(6,5)	(6,6)

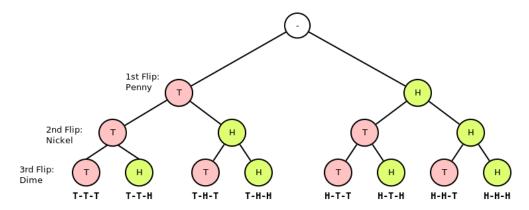
For the given set of data, answer the questions. ³

- a. Of the listed outcomes, how many are "doubles" (both dice have the same value)? What percentage of total outcomes does this represent? (You can write it as a fraction)
- b. How many are doubles *and* have the sum of two dice values less than 4? (You can write it as a fraction)
- c. How many have a 5 on exactly one of the dice?
- d. How many have a 5 on at least one of the dice?

³Based on Exercise 5.1 #6 from Discrete Mathematics, Ensley & Crawley

Question 6 _____ / 20%

The following tree lists all possible outcomes of tossing a penny, a nickel, and a dime together:



For the given set of data, answer the questions. ⁴

- a. Of the outcomes shown, for how many does the result on the penny match the result on the dime?
- b. Which is more likely, that the result on the penny matches the result on the dime, or that they do not match?
- c. For how many of the outcomes do all three coins match?
- d. For how many of the outcomes do exactly two of the coins match?
- e. For how many outcomes is the number of tails less than the number of heads?

 $^{^4\}mathrm{Based}$ on Exercise 5.1 #8 from Discrete Mathematics, Ensley & Crawley

Answer sheet

15% Question 1: Subsets of $U = \{1, 2, 3, 4, 5, 6\}$

- $\square \ 0 \ \square \ 1 \ \square \ 2 \ \square \ 3 \ \square \ 4$
- a. The subset of U that contains all the even numbers.
- b. The subset of U that contains all the prime numbers.
- c. The subset of U that contains all the odd numbers less than 4.

8% Question 2: Movie seating

 $\square \ 0 \ \square \ 1 \ \square \ 2 \ \square \ 3 \ \square \ 4$

List all combinations for any 2 customers, make sure shorter people come before taller people.

23% Question 3: Student folders

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Ω	\Box	1 —	19	3	4

- a. In this model, how many different colors were available at the bookstore?
- b. How many folders would each student choose?
- c. In the table below, indicate which student's selection corresponds with each of the two dimensions. (Put the student's initial in the table on the worksheet.)

		Did the orde	er of selection matter?
		YES	NO
Was color repetition allowed?	YES		
was color repetition anowed:	NO		

- d. For which students were repeating colors acceptable?
- e. For which students were repeating colors *not* acceptable?
- f. Which students' selections would be an ordered list?
- g. Which students' selections would be an unordered list?
- h. Which student's selections demonstrate a permutations?
- i. Which student's selections demonstrate a combination?

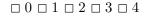
14% Question 4: 2 Prizes for 4 People

 $\square \ 0 \ \square \ 1 \ \square \ 2 \ \square \ 3 \ \square \ 4$

a. Different prizes:

b. Same prizes:

20% Question 5: Red and green dice



- a. Of the listed outcomes, how many are "doubles" (both dice have the same value)? What percentage of total outcomes does this represent? (You can write it as a fraction) _____
- b. How many are doubles *and* have the sum of two dice values less than 4? (You can write it as a fraction) _____
- c. How many have a 5 on exactly one of the dice?
- d. How many have a 5 on at least one of the dice?

20%	Question 6:	Coin toss	

a.	Of the	outcomes	shown,	for	how	many	${\rm does}$	the	${\it result}$	on	the	penny
	match	the result	on the o	lime	? _							

b.	Which is r	more likely,	that the	result on	the penny	matches	the 1	result
	on the dim	ne, or that the	ney do no	t match?				

- c. For how many of the outcomes do all three coins match?
- d. For how many of the outcomes do exactly two of the coins match?
- e. For how many outcomes is the number of tails less than the number of heads? _____

Grading

Question	Weight	0-4	Adjusted score
1	15%		
2	8%		
3	23%		
4	14%		
5	20%		
6	20%		

 $3 \square 4$