

## Answer Key

- 1a. First, check if  $P(1, 1) = 1$  works out.

$$\begin{aligned}
 P(1, 1) &= 1 \cdot P((1-1), (1-1)) \\
 &= 1 \cdot P(0, 0) = 1 \cdot \frac{0!}{0!} = 1 \cdot \frac{1}{1} = 1 \cdot 1 \\
 &= 1 \quad \checkmark \quad \text{Checks out}
 \end{aligned}$$

Next, check for  $P(n, 1) = n \dots$

$$\begin{aligned}
 P(n, 1) &= n \cdot P((n-1), (1-1)) \\
 &= n \cdot P(n-1, 1) = n \cdot \frac{(n-1)!}{(n-1)!} = n \cdot 1 \\
 &= n \quad \checkmark
 \end{aligned}$$

- 1b.  $P(1, 1)$  has been checked in part (a).

Check for  $P(n, 2) = n \cdot (n-1) \dots$

$$\begin{aligned}
 P(n, 2) &= n \cdot P((n-1), (2-1)) \\
 &= n \cdot \frac{(n-1)!}{(n-1-1)!} = n \cdot \frac{(n-1)!}{(n-2)!} \\
 &= n \cdot \frac{(n-1) \cdot (n-2)!}{(n-2)!} \quad \text{Expanded } (n-1)! \text{ in the numerator to } (n-1) \cdot (n-2)! \\
 &= n \cdot (n-1) \quad \checkmark
 \end{aligned}$$

- 1c.  $P(1, 1)$  has been checked in part (a).

Check for  $P(n, 3) = n \cdot (n-1) \cdot (n-2) \dots$

$$\begin{aligned}
 P(n, 3) &= n \cdot P((n-1), (3-1)) \\
 &= n \cdot \frac{(n-1)!}{(n-1-2)!} = n \cdot \frac{(n-1)!}{(n-3)!} \quad \text{Expand } (n-1) \text{ again...} \\
 &= n \cdot \frac{(n-1)(n-2)(n-3)!}{(n-3)!} \\
 &= n \cdot (n-1) \cdot (n-2) \quad \checkmark
 \end{aligned}$$