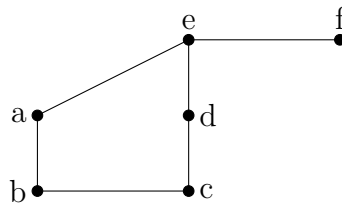


## Question 1

\_\_\_\_\_ / 6

Identify each item for the graph  $G$  given.



- How many nodes (vertices) are there?
- How many edges are there?

- Write down the degree of each node:

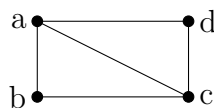
Vertex $v$	$\deg(v)$
$a$	2
$b$	2
$c$	2
$d$	2
$e$	3
$f$	1

- The **maximum degree** of a graph is the highest  $\deg(v)$  value. What is this graph's maximum degree? 3
- The **minimum degree** of a graph is the lowest  $\deg(v)$  value. What is this graph's minimum degree? 1

## Question 2

\_\_\_\_\_ / 3

Answer the following questions, using the graph  $H$  given.

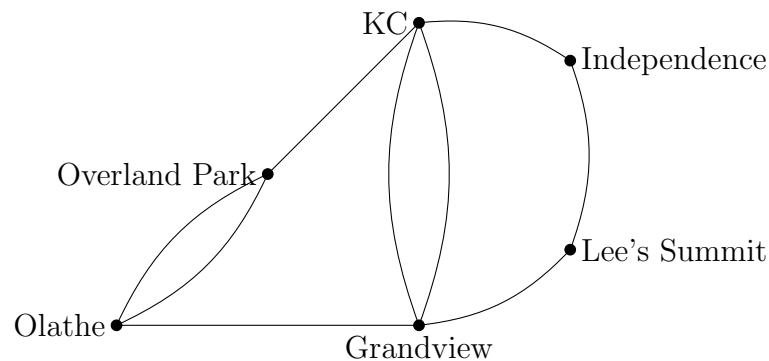


- Come up with several walks from  $a$  to  $c$ . Write all steps (each node visited). Also label the **length** of each walk.  $a \rightarrow b \rightarrow c$  (2) or  $a \rightarrow d \rightarrow c$  (2) or  $a \rightarrow c$  (1).
- Come up with a **closed walk**, beginning and ending at  $a$ . You can choose to visit all nodes or not.
- Come up with a **path**, where no vertices are repeated.

**Question 3**

\_\_\_\_\_ / 5

Answer the following questions, using the graph  $I$  given.



- Come up with a **trail**, a walk with no repeated edges. Example:  $KC \rightarrow Independence \rightarrow Lee's Summit$
- Come up with a **circuit**, a closed trail. Example:  $KC \rightarrow Independence \rightarrow Lee's Summit \rightarrow Grandview \rightarrow KC \rightarrow Overland Park \rightarrow Olathe \rightarrow Grandview$
- Come up with a **cycle**, a circuit where the only repeated node is the first/last one.. Example:  $KC \rightarrow Independence \rightarrow Lee's Summit \rightarrow Grandview \rightarrow KC$
- Identify: Did you come up with any **Eulerian Trails**?  
If not, create one. Example:  $Olathe \rightarrow Overland Park \rightarrow Olathe \rightarrow Grandview \rightarrow KC \rightarrow Grandview \rightarrow Lee's Summit \rightarrow Independence \rightarrow KC \rightarrow Overland Park$
- Identify: Are there any **parallel edges**? Yes:  $Olathe \rightarrow Overland Park$

**Question 4**

\_\_\_\_\_ / 1

Draw a **Directed Graph** using the following list of edges:

$$(1, 2), (2, 1), (3, 3), (4, 2)$$

(Don't confuse these for points on an  $x, y$  plane that are interconnected, each ordered pair is its own set of information - beginning and end nodes.)

Multiple solutions

**Question 5**

\_\_\_\_\_ / 2

Draw a graph that is **not connected**, and draw a **subgraph** of your graph.

Multiple solutions