

TRƯỜNG ĐẠI HỌC BÁCH KHOA HÀ NỘI VIỆN ĐIỆN TỬ - VIỄN THÔNG

BỘ MÔN ĐIỆN TỬ HÀNG KHÔNG VŨ TRỤ

Môn học:

LÝ THUYẾT MẬT MÃ CRYPTOGRAPHY THEORY ET3310

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Mục tiêu học phần

Cung cấp kiến thức cơ bản về mật mã đảm bảo an toàn và bảo mật thông tin:

- ✓ Các phương pháp mật mã khóa đối xứng; Phương pháp mật mã khóa công khai;
- ✓ Các hệ mật dòng và vấn đề tạo dãy giả ngẫu nhiên;
- ✓ Lược đồ chữ ký số Elgamal và chuẩn chữ ký số ECDSA;
- ✓ Độ phức tạp xử lý và độ phức tạp dữ liệu của một tấn công cụ thể vào hệ thống mật mã;
- ✓ Đặc trưng an toàn của phương thức mã hóa;
- ✓ Thám mã tuyến tính, thám mã vi sai và các vấn đề về xây dựng hệ mã bảo mật cho các ứng dụng.



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Tài liệu tham khảo

- 1. A. J. Menezes, P. C. Van Oorschot, S. A. Vanstone, *Handbook of applied cryptography*, CRC Press 1998.
- 2. B. Schneier, Applied Cryptography. John Wiley Press 1996.
- 3. M. R. A. Huth, *Secure Communicating Systems*, Cambridge University Press 2001.
- 4. W. Stallings, Network Security Essentials, Applications and Standards, Prentice Hall. 2000.

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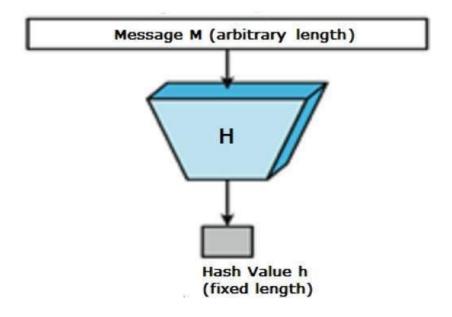


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A cryptographic hash function takes a message of arbitrary length and creates a message digest of fixed length. The ultimate goal of this chapter is to discuss the details of the two most promising cryptographic hash algorithms: SHA-512 and Whirlpool.

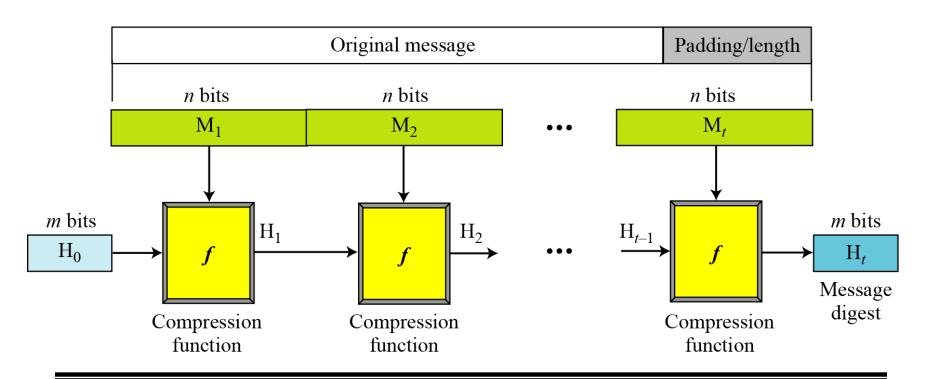


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Iterated Hash Function

Merkle-Damgard Scheme





The scheme uses the following steps:

- The message length and padding are appended to the message to create an augmented message that can be evenly divided into blocks of n bits, where n is the size of the block to be processed by the compression function.
- The message is then considered as t blocks, each of n bits. We call each block M₁, M₂,..., M_t. We call the digest created at t iterations H₁, H₂,..., H_t.
- Before starting the iteration, the digest H₀ is set to a fixed value, normally called IV (initial value or initial vector).
- The compression function at each iteration operates on H_{i-1} and M_i to create a new H_i. In other words, we have H_i = f(H_{i-1}, M_i), where f is the compression function.
- 5. H_t is the cryptographic hash function of the original message, that is, h(M).



Two Groups of Compression Functions

1. The compression function is made from scratch.

Message Digest (MD)

2. A symmetric-key block cipher serves as a compression function.

Whirlpool



A set of cryptographic hash functions uses compression functions that are made from scratch. These compression functions are specifically designed for the purposes they serve.

Message Digest (MD) Several hash algorithms were designed by Ron Rivest. These are referred to as MD2, MD4, and MD5, where MD stands for Message Digest. The last version, MD5, is a strengthened version of MD4 that divides the message into blocks of 512 bits and creates a 128-bit digest. It turned out that a message digest of size 128 bits is too small to resist collision attack.

Secure Hash Algorithm (SHA) The Secure Hash Algorithm (SHA) is a standard that was developed by the National Institute of Standards and Technology (NIST) and published as a Federal Information Processing standard (FIP 180). It is sometimes referred to as Secure Hash Standard (SHS). The standard is mostly based on MD5. The standard was revised in 1995 under FIP 180-1, which includes SHA-1. It was revised later under FIP 180-2, which defines four new versions: SHA-224, SHA-256, SHA-384, and SHA-512.



Other Algorithms RACE Integrity Primitives Evaluation Message Digest (RIPMED) has several versions. RIPEMD-160 is a hash algorithm with a 160-bit message digest. RIPEMD-160 uses the same structure as MD5 but uses two parallel lines of execution. HAVAL is a variable-length hashing algorithm with a message digest of size 128, 160, 192, 224, and 256. The block size is 1024 bits.

	MD5	SHA-1	RIPEMD-160
Digest length	128 bits	160 bits	160 bits
Basic unit of processing	512 bits	512 bits	512 bits
Number of steps	64 (4 rounds of 16)	80 (4 rounds of 20)	160 (5 paired rounds of 16)
Maximum message size	8	2 ⁶⁴ – 1 bits	2 ⁶⁴ – 1 bits
Primitive logical functions	4	4	5
Additive constants used	64	4	9
Endianness	Little-endian	Big-endian	Little-endian



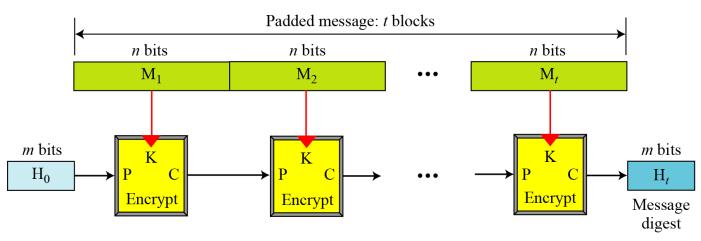
Hash Functions Based on Block Ciphers

An iterated cryptographic hash function can use a symmetric-key block cipher as a compression function. The whole idea is that there are several secure symmetric-key block ciphers, such as triple DES or AES, that can be used to make a one-way function instead of creating a new compression function.

Characteristics	SHA-1	SHA-224	SHA-256	SHA-384	SHA-512
Maximum Message size	$2^{64} - 1$	$2^{64} - 1$	$2^{64} - 1$	$2^{128} - 1$	$2^{128}-1$
Block size	512	512	512	1024	1024
Message digest size	160	224	256	384	512
Number of rounds	80	64	64	80	80
Word size	32	32	32	64	64



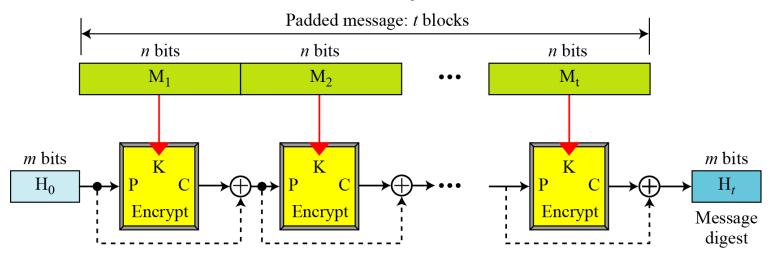
Rabin Scheme



Rabin Scheme The iterated hash function proposed by Rabin is very simple. The Rabin scheme is based on the Merkle-Damgard scheme. The compression function is replaced by any encrypting cipher. The message block is used as the key; the previously created digest is used as the plaintext. The ciphertext is the new message digest. Note that the size of the digest is the size of data block cipher in the underlying cryptosystem. For example, if DES is used as the block cipher, the size of the digest is only 64 bits.



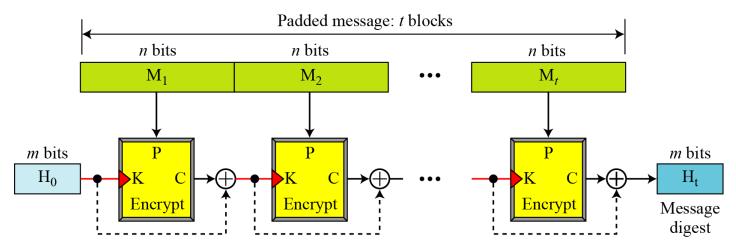
Davies-Meyer Scheme



Davies-Meyer Scheme The Davies-Meyer scheme is basically the same as the Rabin scheme except that it uses forward feed to protect against meet-in-the-middle attack.



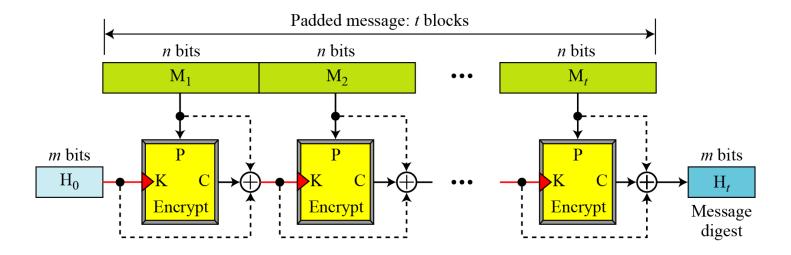
Matyas-Meyer-Oseas Scheme



Matyas-Meyer-Oseas Scheme The Matyas-Meyer-Oseas scheme is a dual version of the Davies-Meyer scheme: the message block is used as the key to the cryptosystem.



Miyaguchi-Preneel Scheme



Miyaguchi-Preneel Scheme The Miyaguchi-Preneel scheme is an extended version of Matyas-Meyer-Oscas. To make the algorithm stronger against attack, the plaintext, the cipher key, and the ciphertext are all exclusive-ored together to create the new digest. This is the scheme used by the Whirlpool hash function.

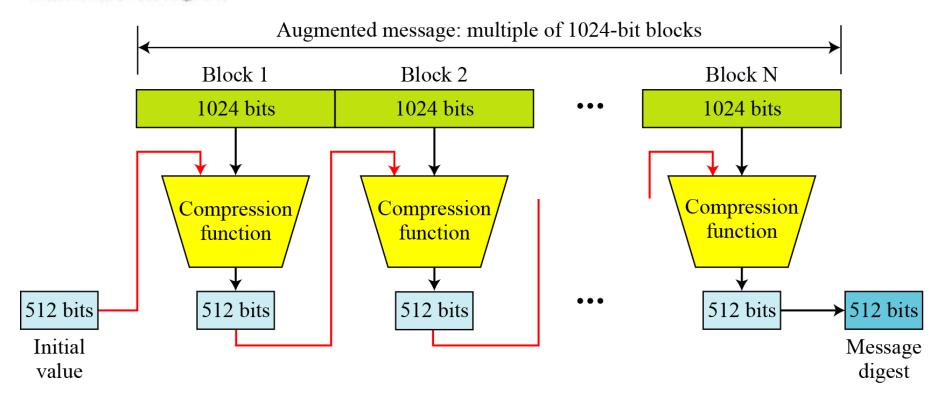


SHA-512 is the version of SHA with a 512-bit message digest. This version, like the others in the SHA family of algorithms, is based on the Merkle-Damgard scheme.

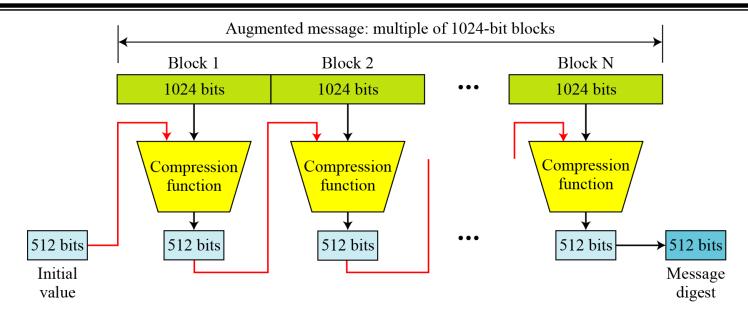




SHA-512 creates a digest of 512 bits from a multiple-block message. Each block is 1024 bits in length,







The digest is initialized to a predetermined value of 512 bits. The algorithm mixes this initial value with the first block of the message to create the first intermediate message digest of 512 bits. This digest is then mixed with the second block to create the second intermediate digest. Finally, the (N-1)th digest is mixed with the Nth block to create the Nth digest. When the last block is processed, the resulting digest is the message digest for the entire message.



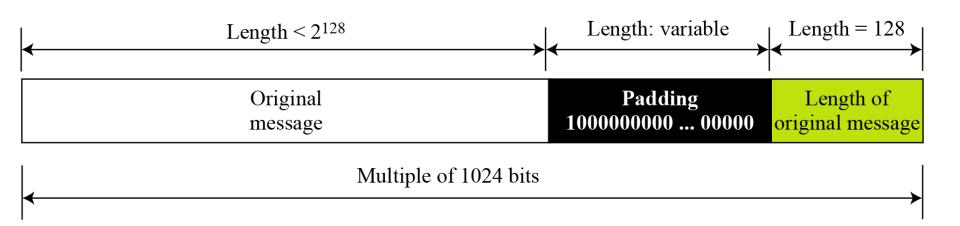
Message Preparation

SHA-512 insists that the length of the original message be less than 2^{128} bits.

SHA-512 creates a 512-bit message digest out of a message less than 2¹²⁸.



Padding and length field in SHA-512



 $(|M| + |P| + 128) = 0 \mod 1024$ $\rightarrow |P| = (-|M| - 128) \mod 1024$





What is the number of padding bits if the length of the original message is 2590 bits?

What is the number of padding bits if the length of the original message is 2590 bits?

Solution

We can calculate the number of padding bits as follows:

$$|P| = (-2590 - 128) \mod 1024 = -2718 \mod 1024 = 354$$

The padding consists of one 1 followed by 353 0's.





Do we need padding if the length of the original message is already a multiple of 1024 bits?



Do we need padding if the length of the original message is already a multiple of 1024 bits?

Solution

Yes we do, because we need to add the length field. So padding is needed to make the new block a multiple of 1024 bits.



What is the (a) minimum and (b) maximum number of padding bits that can be added to a message?



What is the minimum and maximum number of padding bits that can be added to a message?

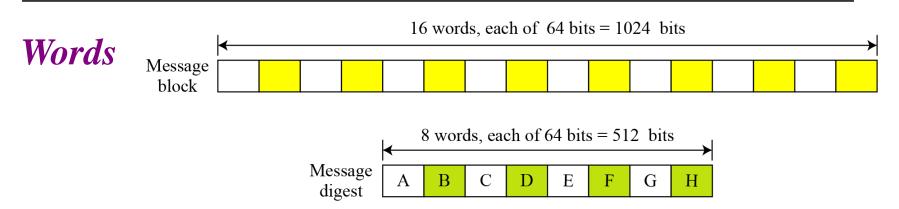
Solution

a. The minimum length of padding is 0 and it happens when (-M-128) mod 1024 is 0. This means that |M|=-128 mod 1024 = 896 mod 1024 bits. In other words, the last block in the original message is 896 bits. We add a 128-bit length field to make the block complete.

Continued

b) The maximum length of padding is 1023 and it happens when $(-|M|-128)=1023 \mod 1024$. This means that the length of the original message is $|M|=(-128-1023) \mod 1024$ or the length is $|M|=897 \mod 1024$. In this case, we cannot just add the length field because the length of the last block exceeds one bit more than 1024. So we need to add 897 bits to complete this block and create a second block of 896 bits. Now the length can be added to make this block complete.





SHA-512 operates on words; it is **word oriented**. A word is defined as 64 bits. This means that, after the padding and the length field are added to the message, each block of the message consists of sixteen 64-bit words. The message digest is also made of 64-bit words, but the message digest is only eight words and the words are named A, B, C, D, E, F, G, and H,

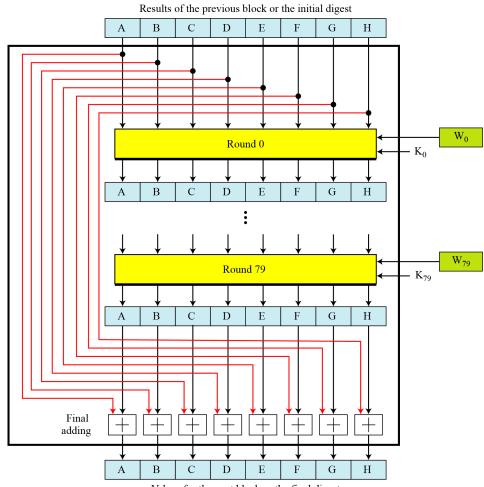


Message Digest Initialization

Buffer	Value (in hexadecimal)	Buffer	Value (in hexadecimal)
A_0	6A09E667F3BCC908	E_0	510E527FADE682D1
B_0	BB67AE8584CAA73B	F_0	9B05688C2B3E6C1F
C_0	3C6EF372EF94F828	G_0	1F83D9ABFB41BD6B
D_0	A54FE53A5F1D36F1	H_0	5BE0CD19137E2179



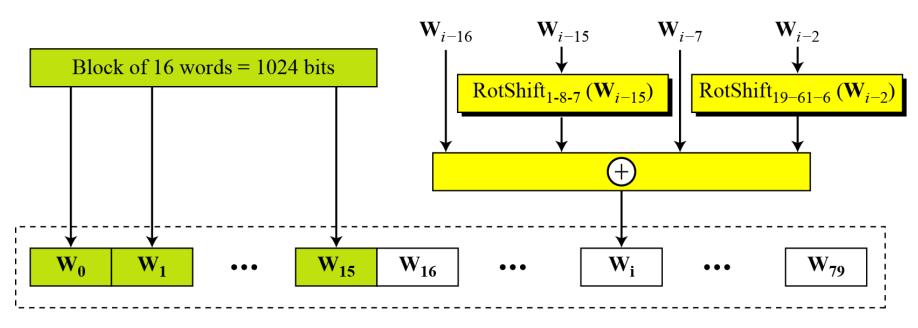
Compression function in SHA-512



Values for the next block or the final digest



Word Expansion

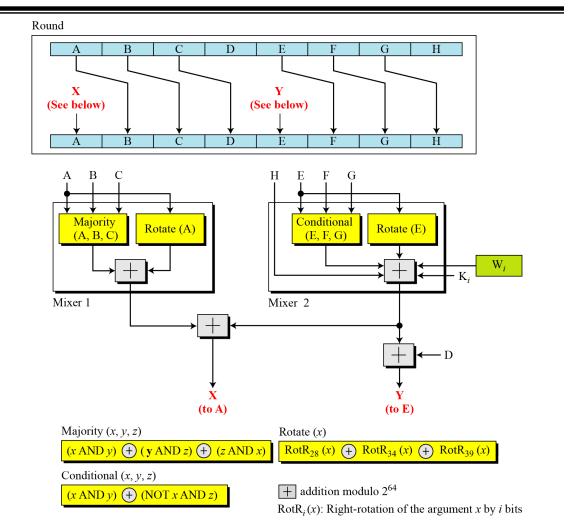


 $RotShift_{I-m-n}(x): RotR_I(x) \oplus RotR_m(x) \oplus ShL_n(x)$

 $RotR_i(x)$: Right-rotation of the argument x by i bits

 $ShL_i(x)$: Shift-left of the argument x by i bits and padding the left by 0's.





Structure of each round in SHA-512



Majority Function

 $(A_j AND B_j) \oplus (B_j AND C_j) \oplus (C_j AND A_j)$

Conditional Function

 $(\mathbf{E}_j \mathbf{AND} \mathbf{F}_j) \oplus (\mathbf{NOT} \mathbf{E}_j \mathbf{AND} \mathbf{G}_j)$

Rotate Functions

Rotate (A): $RotR_{28}(A) \oplus RotR_{34}(A) \oplus RotR_{29}(A)$

Rotate (E): $RotR_{28}(E) \oplus RotR_{34}(E) \oplus RotR_{29}(E)$



428A2F98D728AE22 3956C25BF348B538 D807AA98A3030242 72BE5D74F27B896F E49B69C19EF14AD2 2DE92C6F592B0275 983E5152EE66DFAB C6E00BF33DA88FC2 27B70A8546D22FFC 650A73548BAF63DE A2BFE8A14CF10364 D192E819D6EF5218 19A4C116B8D2D0C8 391C0CB3C5C95A63 748F82EE5DEFB2FC 90BEFFFA23631E28 CA273ECEEA26619C 06F067AA72176FBA 28DB77F523047D84 4CC5D4BECB3E42B6

7137449123EF65CD 59F111F1B605D019 12835B0145706FBE 80DEB1FE3B1696B1 EFBE4786384F25E3 4A7484AA6EA6E483 A831C66D2DB43210 D5A79147930AA725 2E1B21385C26C926 766A0ABB3C77B2A8 A81A664BBC423001 D69906245565A910 1E376C085141AB53 4ED8AA4AE3418ACB 78A5636F43172F60 A4506CEBDE82BDE9 D186B8C721C0C207 0A637DC5A2C898A6 32CAAB7B40C72493 4597F299CFC657E2

B5C0FBCFEC4D3B2F 923F82A4AF194F9B 243185BE4EE4B28C 9BDC06A725C71235 0FC19DC68B8CD5B5 5CBOA9DCBD41FBD4 B00327C898FB213F 06CA6351E003826F 4D2C6DFC5AC42AED 81C2C92E47EDAEE6 C24B8B70D0F89791 F40E35855771202A 2748774CDF8EEB99 5B9CCA4F7763E373 84C87814A1F0AB72 BEF9A3F7B2C67915 EADA7DD6CDE0EB1E 113F9804BEF90DAE 3C9EBEOA15C9BEBC 5FCB6FAB3AD6FAEC

E9B5DBA58189DBBC AB1C5ED5DA6D8118 550C7DC3D5FFB4E2 C19BF174CF692694 240CA1CC77AC9C65 76F988DA831153B5 BF597FC7BEEF0EE4 142929670A0E6E70 53380D139D95B3DF 92722C851482353B C76C51A30654BE30 106AA07032BBD1B8 34B0BCB5E19B48A8 682E6FF3D6B2B8A3 8CC702081A6439EC C67178F2E372532B F57D4F7FEE6ED178 1B710B35131C471B 431D67C49C100D4C 6C44198C4A475817



There are 80 constants, K_0 to K_{79} , each of 64 bits. Similar These values are calculated from the first 80 prime numbers (2, 3,..., 409). For example, the 80th prime is 409, with the cubic root $(409)^{1/3} = 7.42291412044$. Converting this number to binary with only 64 bits in the fraction part, we get

 $(111.0110\ 1100\ 0100\ 0100\ \dots\ 0111)_2 \ \to \ (7.6\text{C}44198\text{C}4\text{A}475817)_{16}$

The fraction part: (6C44198C4A475817)₁₆



Ví dụ

We apply the Majority function on buffers A, B, and C. If the leftmost hexadecimal digits of these buffers are 0x7, 0xA, and 0xE, respectively, what is the leftmost digit of the result?



Ví dụ

We apply the Majority function on buffers A, B, and C. If the leftmost hexadecimal digits of these buffers are 0x7, 0xA, and 0xE, respectively, what is the leftmost digit of the result?

Solution

The digits in binary are 0111, 1010, and 1110.

- a. The first bits are 0, 1, and 1. The majority is 1.
- b. The second bits are 1, 0, and 1. The majority is 1.
- c. The third bits are 1, 1, and 1. The majority is 1.
- d. The fourth bits are 1, 0, and 0. The majority is 0.

The result is 1110, or 0xE in hexadecimal.





We apply the Conditional function on E, F, and G buffers. If the leftmost hexadecimal digits of these buffers are 0x9, 0xA, and 0xF respectively, what is the leftmost digit of the result?



Ví dụ

We apply the Conditional function on E, F, and G buffers. If the leftmost hexadecimal digits of these buffers are 0x9, 0xA, and 0xF respectively, what is the leftmost digit of the result?

Solution

The digits in binary are 1001, 1010, and 1111.

- a. The first bits are 1, 1, and 1. The result is F_1 , which is 1.
- b. The second bits are 0, 0, and 1. The result is G_2 , which is 1.
- c. The third bits are 0, 1, and 1. The result is $G_3,$ which is 1.
- d. The fourth bits are 1, 0, and 1. The result is F_4 , which is 0.

The result is 1110, or 0xE in hexadecimal.



With a message digest of 512 bits, SHA-512 expected to be resistant to all attacks, including collision attacks.

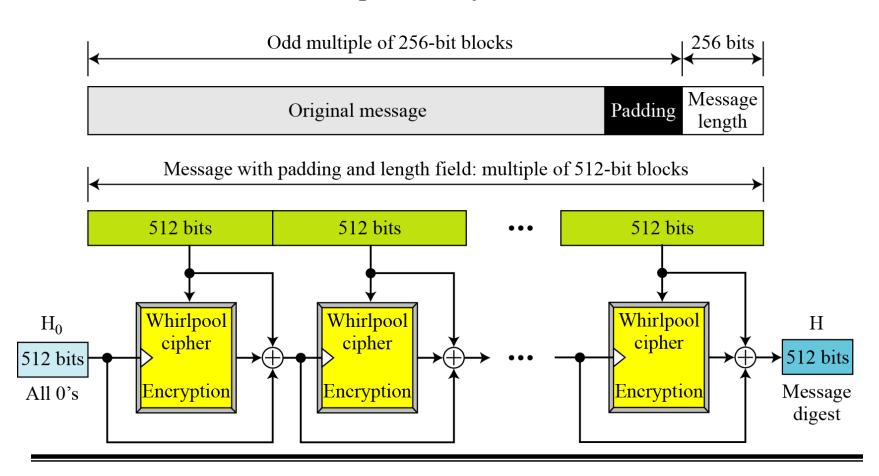


Whirlpool is an iterated cryptographic hash function, based on the Miyaguchi-Preneel scheme, that uses a symmetric-key block cipher in place of the compression function. The block cipher is a modified AES cipher that has been tailored for this purpose.



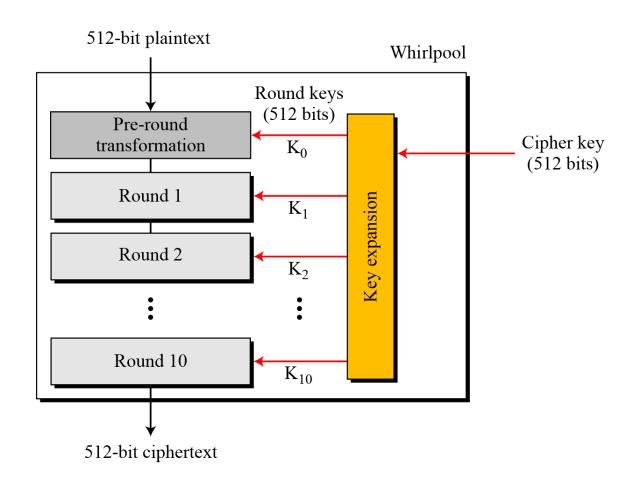


Whirlpool hash function



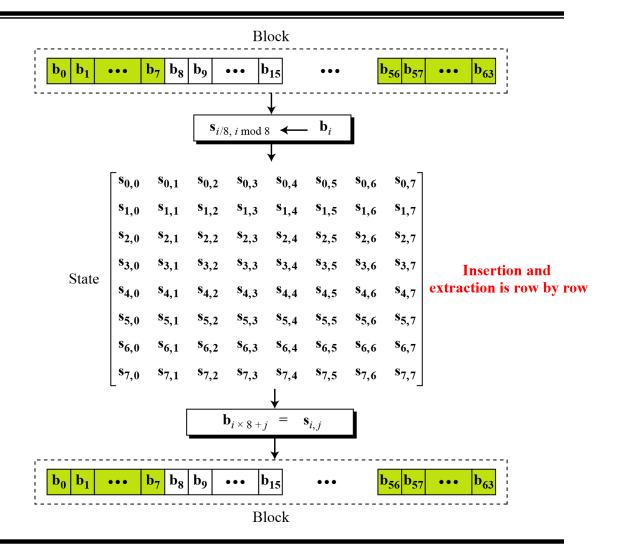


General idea of the Whirlpool cipher



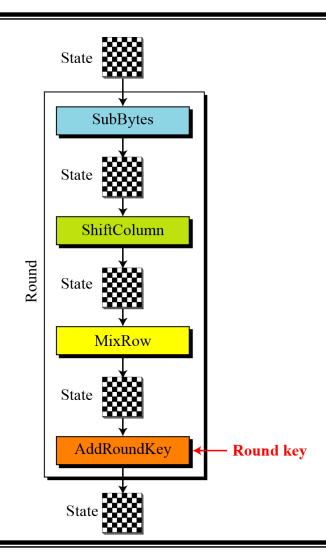


Block and state in the Whirlpool cipher



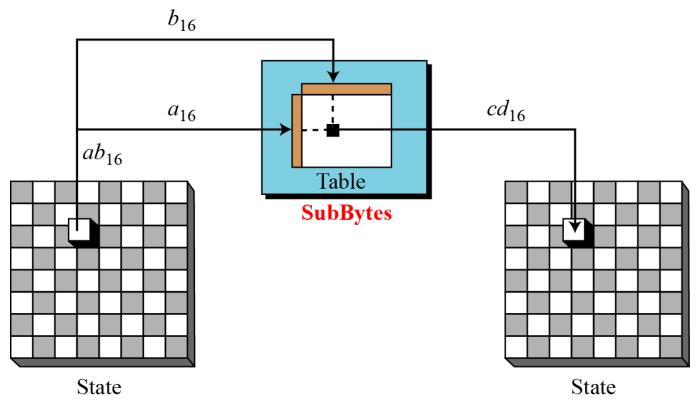


Structure of Each Round Each round uses four transformations.





SubBytes Like in AES, SubBytes provide a nonlinear transformation.



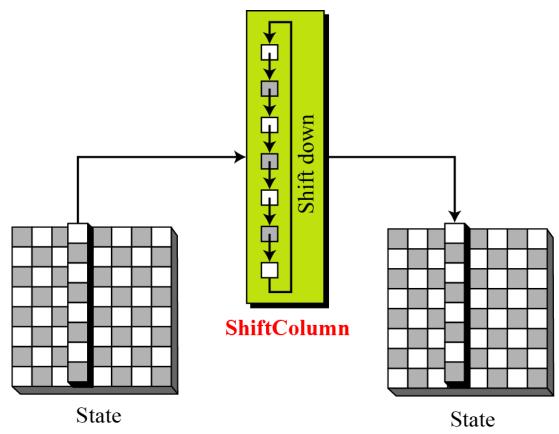


SubBytes transformation table (S-Box)

	0	1	2	3	4	5	6	7	8	9	\boldsymbol{A}	В	C	D	\boldsymbol{E}	\boldsymbol{F}
0	18	23	C6	E8	87	B8	01	4F	36	A6	D2	F5	79	6F	91	52
1	16	ВС	9B	8E	A3	0C	7B	35	1D	E0	D7	C2	2E	4B	FE	57
2	15	77	37	E5	9F	F0	4A	CA	58	C9	29	0A	B1	A0	6B	85
3	BD	5D	10	F4	СВ	3E	05	67	E4	27	41	8B	A7	7D	95	C8
4	FB	EF	7C	66	DD	17	47	9E	CA	2D	BF	07	AD	5A	83	33
5	63	02	AA	71	C8	19	49	C9	F2	ЕЗ	5B	88	9A	26	32	В0
6	E9	0F	D5	80	BE	CD	34	48	FF	7A	90	5F	20	68	1A	AE
7	B4	54	93	22	64	F1	73	12	40	08	C3	EC	DB	A1	8D	3D
8	97	00	CF	2B	76	82	D6	1B	В5	AF	6A	50	45	F3	30	EF
9	3F	55	A2	EA	65	BA	2F	C0	DE	1C	FD	4D	92	75	06	8A
A	B2	E6	0E	1F	62	D4	A8	96	F9	C5	25	59	84	72	39	4C
В	5E	78	38	8C	C1	A5	E2	61	В3	21	9C	1E	43	C7	FC	04
<i>C</i>	51	99	6D	0D	FA	DF	7E	24	3B	AB	CE	11	8F	4E	В7	ЕВ
D	3C	81	94	F7	9B	13	2C	D3	E7	6E	C4	03	56	44	7E	A9
E	2A	BB	C1	53	DC	0B	9D	6C	31	74	F6	46	AC	89	14	E1
F	16	3A	69	09	70	B6	C0	ED	CC	42	98	A4	28	5C	F8	86

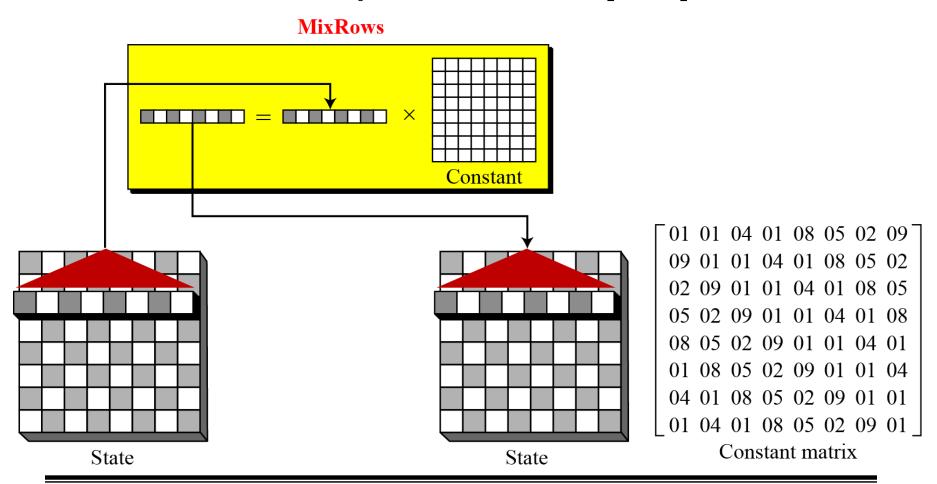


ShiftColumns

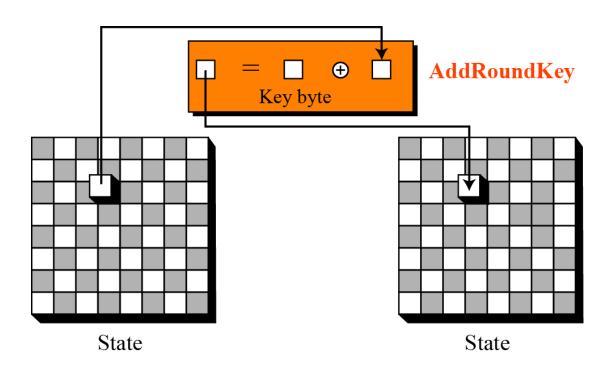




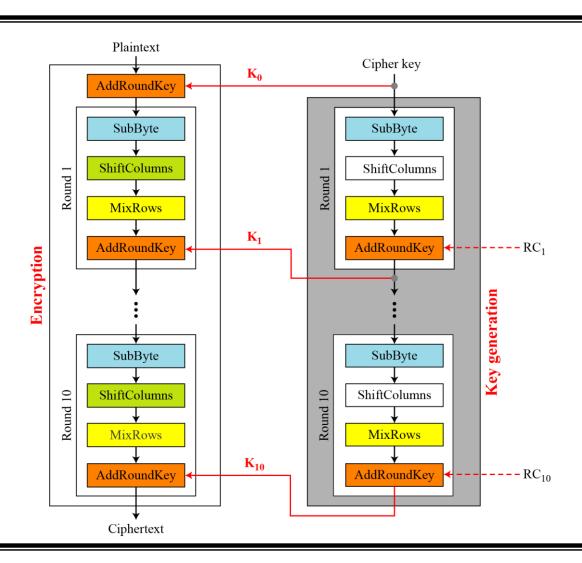
MixRows transformation in the Whirlpool cipher













A conventional signature is included in the document; it is part of the document. But when we sign a document digitally, we send the signature as a separate document.

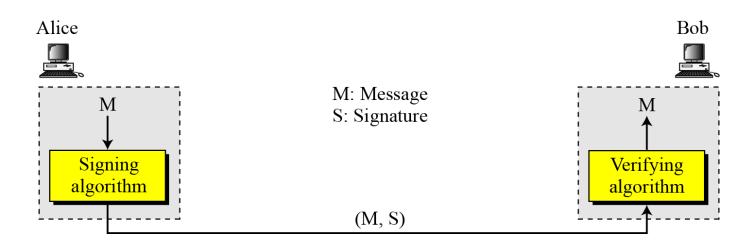
For a conventional signature, when the recipient receives a document, she compares the signature on the document with the signature on file. For a digital signature, the recipient receives the message and the signature. The recipient needs to apply a verification technique to the combination of the message and the signature to verify the authenticity.



For a conventional signature, there is normally a one-to-many relationship between a signature and documents. For a digital signature, there is a one-to-one relationship between a signature and a message.

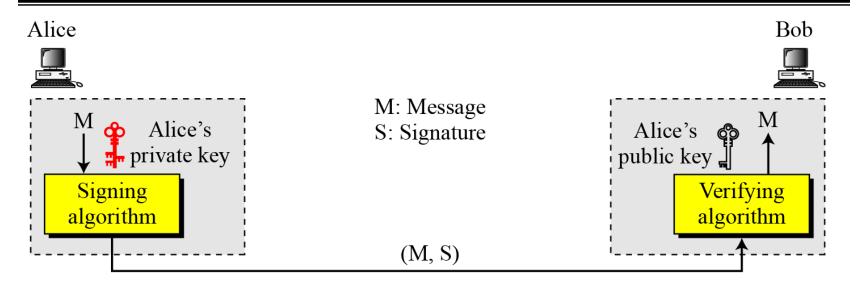
In conventional signature, a copy of the signed document can be distinguished from the original one on file. In digital signature, there is no such distinction unless there is a factor of time on the document.





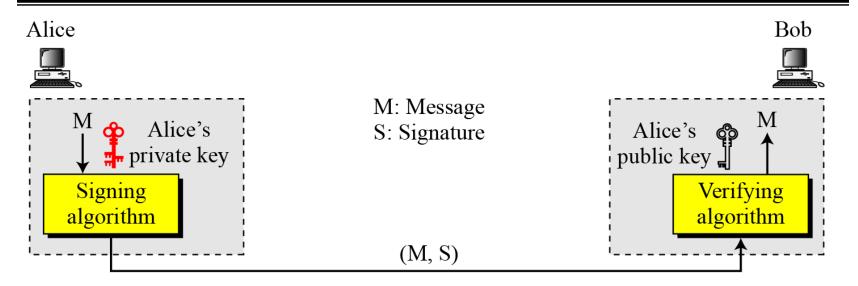
This figure shows the digital signature process. The sender uses a signing algorithm to sign the message. The message and the signature are sent to the receiver. The receiver receives the message and the signature and applies the verifying algorithm to the combination. If the result is true, the message is accepted; otherwise, it is rejected.





A digital signature needs a public-key system. The signer signs with her private key; the verifier verifies with the signer's public key.





A digital signature needs a public-key system. The signer signs with her private key; the verifier verifies with the signer's public key.



A secure digital signature scheme, like a secure conventional signature can provide message authentication.

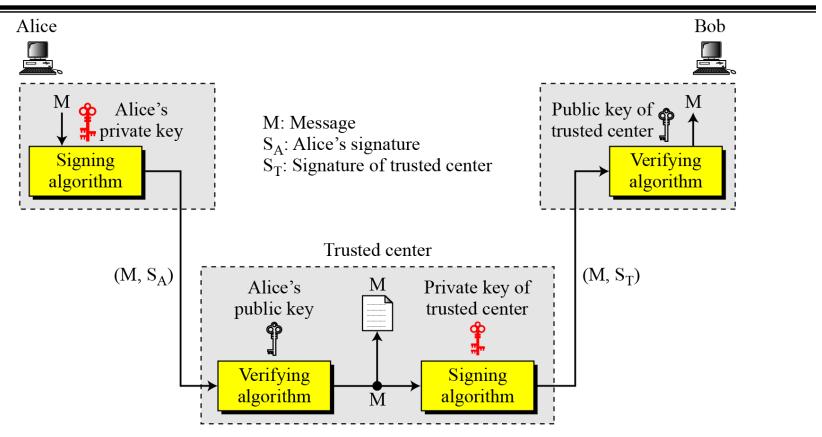
A digital signature provides message authentication.



The integrity of the message is preserved even if we sign the whole message because we cannot get the same signature if the message is changed.

A digital signature provides message integrity.





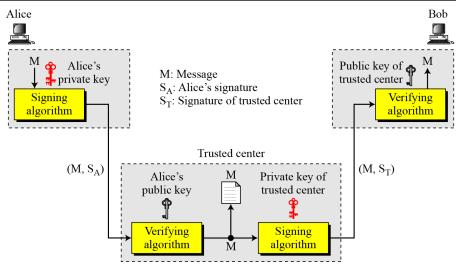
Nonrepudiation can be provided using a trusted party.



If Alice signs a message and then denies it, can Bob later prove that Alice actually signed it? For example, if Alice sends a message to a bank (Bob) and asks to transfer \$10,000 from her account to Ted's account, can Alice later deny that she sent this message? With the scheme we have presented so far, Bob might have a problem. Bob must keep the signature on file and later use Alice's public key to create the original message to prove the message in the file and the newly created message are the same. This is not feasible because Alice may have changed her private or public key during this time; she may also claim that the file containing the signature is not authentic.

One solution is a trusted third party. People can create an established trusted party among themselves.





Alice creates a signature from her message (S_A) and sends the message, her identity, Bob's identity, and the signature to the center. The center, after checking that Alice's public key is valid, verifies through Alice's public key that the message came from Alice. The center then saves a copy of the message with the sender identity, recipient identity, and a timestamp in its archive. The center uses its private key to create another signature (S_T) from the message. The center then sends the message, the new signature, Alice's identity, and Bob's identity to Bob. Bob verifies the message using the public key of the trusted center.



6.6. Các kiểu phá hoại chữ ký số

Key-Only Attack

Known-Message Attack

Chosen-Message Attack

Existential Forgery

Selective Forgery