

Report

Project 2



Nguyễn Văn Hậu –20127493

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1

Introduce

1.1 Student information:

ID	Full name
20127493	Nguyễn Văn Hậu

Completion level: 100%

1.2 Information report:

- In this project, students research and implement the adversarial searching algorithm
- In addition, students implement an application (tic-tac-toe problem) and apply the adversarial technique to solve that tic-tac-toe.

2

Description of the algorithm

Minimax algorithm :

- Mini-max algorithm is a recursive or backtracking algorithm which is used in decision-making and game theory. It provides an optimal move for the player assuming that opponent is also playing optimally
- Mini-max mostly used for the game playing with AI such as chess,tic tac toe
- The minimax algorithm performs a depth-first search algorithm for the exploration of the complete game tree
- **Properties of Mini-Max**
 - Complete: algorithm is complete. If finite search tree or definitely find a solution (if exist)
 - Optimal: yes
 - Time complexity : $O(b^m)$ b:the legal move, m: maximum of depth
 - Space complexity: $O(bm)$ b:the legal move, m: maximum of depth
- **Pseudo code**

function MINIMAX-DECISION(*state*) **returns** an action
return $\arg \max_{a \in \text{ACTIONS}(s)} \text{MIN-VALUE}(\text{RESULT}(state, a))$

function MAX-VALUE(*state*) **returns** a utility value
if TERMINAL-TEST(*state*) **then return** UTILITY(*state*)
 $v \leftarrow -\infty$
for each *a* **in** ACTIONS(*state*) **do**
 $v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a)))$
return *v*

function MIN-VALUE(*state*) **returns** a utility value
if TERMINAL-TEST(*state*) **then return** UTILITY(*state*)
 $v \leftarrow \infty$
for each *a* **in** ACTIONS(*state*) **do**
 $v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a)))$
return *v*

○ **principles:**

- In this algorithm two players play the game, one is called MAX and other is called MIN.
- Both Players of the game are opponent of each other, where MAX will select the maximized value and MIN will select the minimized value.
- The minimax algorithm performs a depth-first search algorithm for the exploration of the complete game tree.
- The minimax algorithm proceeds all the way down to the terminal node of the tree, then backtrack the tree as the recursion.

Pruning Alpha-Beta:

- Alpha-beta pruning is a modified version of the minimax algorithm. It is an optimization technique for the minimax algorithm
- Pruning Alpha-Beta is a technique by which without checking each node of search tree we can compute the correct mini-max decision, based on 2 parameters: alpha, beta
- Alpha: The best (highest-value) choice we have found so far at any point along the path of Maximizer. The initial value of alpha is $-\infty$.
- Beta: The best (lowest-value) choice we have found so far at any point along the path of Minimizer. The

initial value of beta is $+\infty$.

- The algorithm will remove all the nodes which are not really affecting the final decision but making algorithm slow

○ Pseudo code

function ALPHA-BETA-SEARCH(*state*) **returns** an action

$v \leftarrow \text{MAX-VALUE}(\text{state}, -\infty, +\infty)$

return the action in $\text{ACTIONS}(\text{state})$ with value v

function MAX-VALUE(*state*, α , β) **returns** a utility value

if $\text{TERMINAL-TEST}(\text{state})$ **then return** $\text{UTILITY}(\text{state})$

$v \leftarrow -\infty$

for each a **in** $\text{ACTIONS}(\text{state})$ **do**

$v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$

if $v \geq \beta$ **then return** v

$\alpha \leftarrow \text{MAX}(\alpha, v)$

return v

function MIN-VALUE(*state*, α , β) **returns** a utility value

if $\text{TERMINAL-TEST}(\text{state})$ **then return** $\text{UTILITY}(\text{state})$

$v \leftarrow +\infty$

for each a **in** $\text{ACTIONS}(\text{state})$ **do**

$v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$

if $v \leq \alpha$ **then return** v

$\beta \leftarrow \text{MIN}(\beta, v)$

return v

○ Case

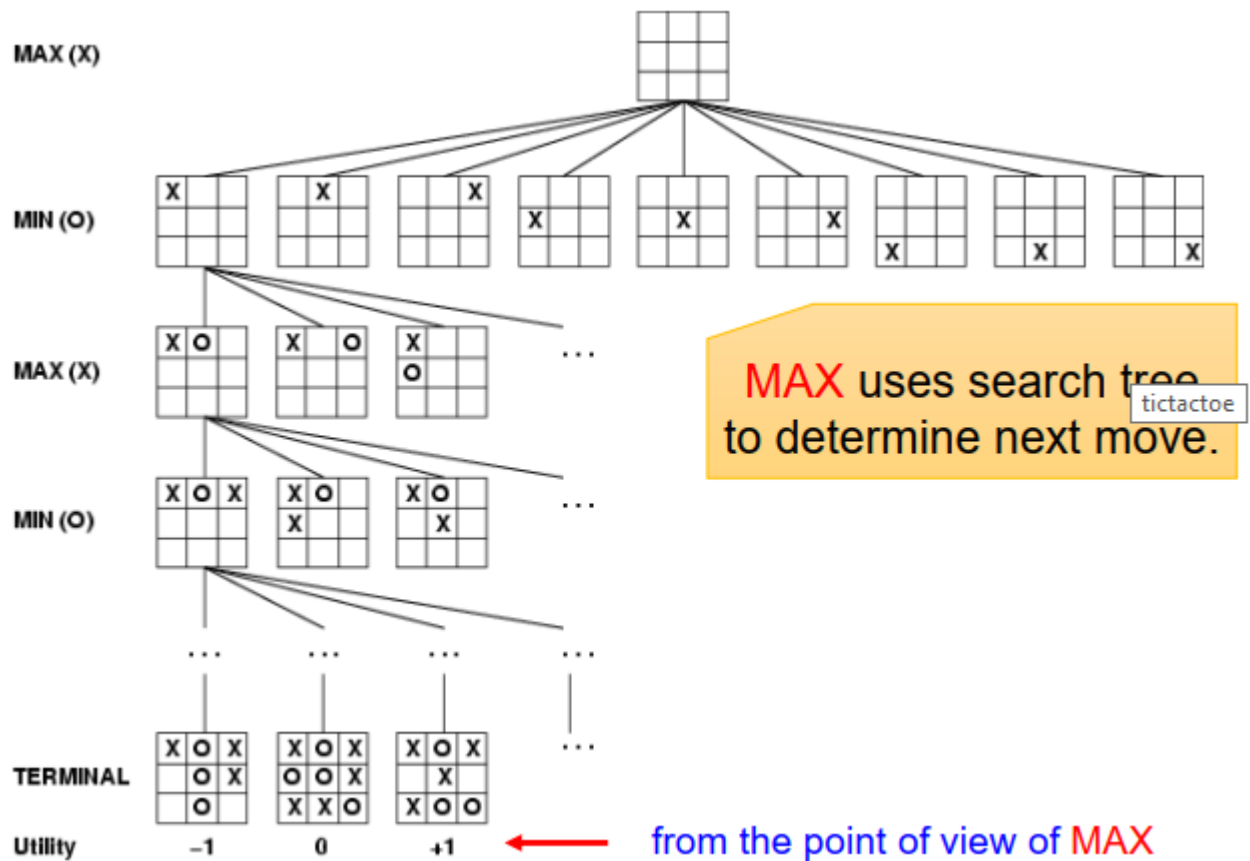
- Good move ordering: time complexity $O(b^{(m/2)}) \rightarrow \times 2$ search depth
- Worst move ordering: time complexity $O(b^m)$

3 Apply algorithm to the tic tac toe

In this project, I will use mini-max algorithm

- Initial state: It specifies how the game is set up at the start.
- Player(s): It specifies which player has moved in the state space.
- Action(s): It returns the set of legal moves in state space
- Result(s,a): It is the transition model, which specifies the result of moves in the state space.
- Terminal-Test(s): true if the game is over, else it is false at any case.
- Utility(s,p): for tic-tac-toe, utility values are +1, -1, and 0.

Game tree:



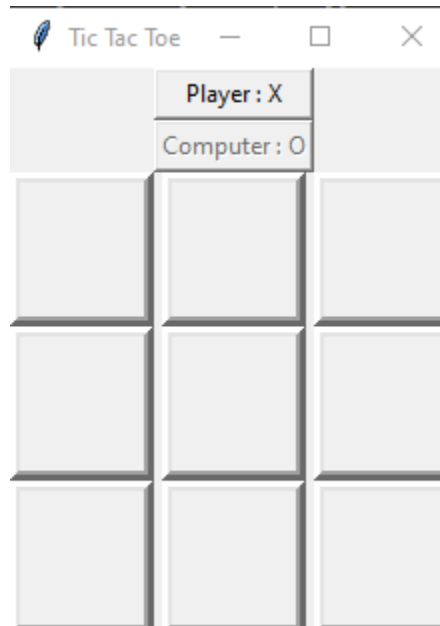
4 User manual

1. Run program
2. The gui of game will appear

- Play(player): player play first
- Play(robot): robot play first
- Exit : is to exit the game



3. Interface



5 Reference

1. Interface Game: <https://www.geeksforgeeks.org/tic-tac-toe-game-with-gui-using-tkinter-in-python/>
2. Minimax algorithm: <https://github.com/javacodingcommunity/TicTacToeAI-with-Minimax>
3. Report: <https://www.javatpoint.com/ai-adversarial-search>
4. Video demo: https://drive.google.com/file/d/1AqXOgDMYX_qAQRNfp4Np0IbKXFm6Xjib/view?usp=sharing