Problem (Nguyen Van Huyen). *Let a, b, c, d be positive real numbers. Prove that*

$$\frac{a}{b} + \frac{b}{c} + \frac{c}{d} + \frac{d}{a} \geqslant 4 + \frac{(a-b)^2}{ab + bc + cd + da}.$$