

## PROJECT 7 – NUMERICAL INTEGRATION

**Due by 11pm Wednesday, November 24, 2020:**

For the purposes of this project, a numerical integrator is a procedure which takes four arguments

- a function  $f$
- the left end point  $a$  of the interval over which to integrate
- the right end point  $b$  of the interval over which to integrate
- the number of sub-intervals  $n$  to use in the numerical integration.

- (1) Using a Mathematica command such as

```
numIntegrator[f_,a_,b_,n_] := Module[{ }, ...
```

create a numerical integrator for each of the following rules:

- (a) left end point rule
- (b) right end point rule
- (c) trapazoid rule
- (d) Simpson's rule

- (2) Using Mathematica's `N` and `Integrate` functions, numerically integrate the function  $f(x) = x + \sin x$  over the interval  $[0, 10]$ .
- (3) Using the numerical integrator for the left end point rule that you defined in Part (1a), numerically integrate the function  $f(x) = x + \sin x$  over the interval  $[0, 10]$  using 10 sub-intervals.
- (4) Using the numerical integrator for the right end point rule that you defined in Part (1b), numerically integrate the function  $f(x) = x + \sin x$  over the interval  $[0, 10]$  using 10 sub-intervals.
- (5) Using the numerical integrator for the trapazoid rule that you defined in Part (1c), numerically integrate the function  $f(x) = x + \sin x$  over the interval  $[0, 10]$  using 10 sub-intervals.
- (6) Using the numerical integrator for the Simpson's rule that you defined in Part (1d), numerically integrate the function  $f(x) = x + \sin x$  over the interval  $[0, 10]$  using 10 sub-intervals.
- (7) Create a table which compares the numbers you obtained in parts (2) through (6) above.
- (8) Repeat parts (3) through (7) above using 1000 sub-intervals instead of 10.