

# 52nd—24th INTERNATIONAL-RUDOLF ORTVAY PROBLEM SOLVING CONTEST IN PHYSICS

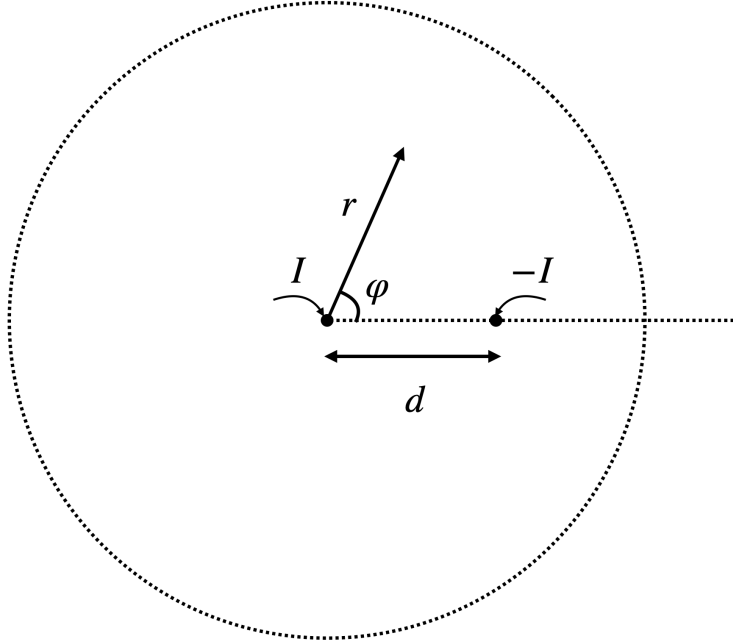
## Problem 18

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We determine the coordinate of a point on conical shell with the spherical coordinate system  $(r, \theta, \varphi)$  where  $\theta = \arcsin\left(\frac{1}{\pi}\right) = \text{const}$ , so we actually only need  $(r, \varphi)$ . Choose this coordinate system so that  $\varphi = 0$  at  $B$  and  $\varphi = \pi$  at  $C$ .

With our coordinate system, if we let  $j'_r = \frac{j_r}{\sin\theta} = \pi j_r$ , the solution of this problem will be the same as when we consider a material of a large, thin, homogeneous metal plate.



In that case, we have:

$$j'_r = \frac{I}{2\pi\delta} \left( \frac{1}{r} - \frac{r - d \cos \varphi}{d^2 + r^2 - 2dr \cos \varphi} \right).$$

$$j_\varphi = \frac{I}{2\pi\delta} \frac{d \sin \varphi}{d^2 + r^2 - 2dr \cos \varphi}.$$

Return to our problem where  $d = \pi R$ , at  $C$ ,  $r = \pi R$  and  $\varphi = \pi$  so the density current is:

$$j_C = \pi j'_C = \frac{I}{4\pi\delta R}.$$