

# OOP Design and Specification

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## Preface

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## Chapter 1

## Introduction

This book will guide you through the fundamentals of constructing high-quality software using a modern **object-oriented programming** (OOP) approach. We will use *Python* for demonstration, but the concepts can be applied to any object-oriented programming language. The goal is to develop programs that are reliable, efficient, and easy to understand, modify, and maintain.

#### 1.1 Decomposition

As the size of a program increases, it becomes essential to *decompose* the program into smaller, independent programs (or functions or modules). This decomposition process allows for easier management of the program, especially when multiple developers are involved. This makes the program easier to understand and maintain.

Decomposition is the process of breaking a complex program into smaller, independent, more manageable programs, i.e., "divide and conquer". It allows programmer to focus on one part of the problem at a time, without worrying about the rest of the program.

**Example** Fig. 1.1 shows a Python implementation of *Merge Sort*, a classic example of problem decomposition. It breaks the problem of sorting a list into simpler problems of sorting smaller lists and merging them.

#### 1.2 Abstraction

Abstraction is a key concept in OOP that allows programmers to hide the implementation details of a program and focus on the essential features. In an OOP language such as Python, you can abstract problems by creating functions, classes, and modules that hide the underlying implementation details.

```
def merge_sort(lst):
                                          def merge(left, right):
    if len(lst) <= 1:</pre>
                                              result = []
       return 1st
                                              i = j = 0
    mid = len(lst) // 2
                                              while i < len(left) and j < len(right):</pre>
    left = merge_sort(lst[:mid])
                                                  if left[i] < right[j]:</pre>
    right = merge_sort(lst[mid:])
                                                       result.append(left[i])
    return merge(left, right)
                                                       i += 1
                                                       result.append(right[j])
                                                       j += 1
                                              result.extend(left[i:])
                                              result.extend(right[j:])
                                              return result
                     Fig. 1.1: Decomposition example: Mergesort
                                          class Dog(Mammal):
class Mammal:
    def __init__(self, name):
                                              def speak(self): return "Woof!"
        self.name = name
                                          class Cat(Mammal):
                                              def speak(self): return "Meow!"
    def speak(self): pass
```

Fig. 1.2: Decomposition example: Mergesort

**Example** Fig. 1.2 demonstrates an abstraction for different types of mammals. Mammals such as Dog and Cat share common behaviors such as making noise (speak). We can create a class Mammal that defines these common behaviors, and then subclasses Dog and Cat that inherit from Mammal and define their own unique behaviors.

## Chapter 2

### Procedural Abstraction

Procedural abstraction is a fundamental concept in programming that allows developers to create functions (methods) that hide the implementation details of a program. By abstracting away the details, developers can focus on the essential features of the program, making it easier to understand, modify, and maintain.

By separating procedure definition and invocation, we make two important methods of abstraction: abstraction by parameterization and abstraction by specification.

**Abstraction by Parameterization** This generalizes a function by using *parameters*. This allows the function to be used with different input values, making it more versatile and reusable. Fig. 2.1 shows an example of abstract parameterization. The cal\_area function calculates the area of a rectangle given its length and width, which are passed as parameters.

```
def cal_area(length, width):
    return length * width

# can be used with different values for length and width.
area1 = cal_area(5, 10)
area2 = cal_area(7, 3)
```

Fig. 2.1: Example: Abstract Parameterization

**Abstraction by Specification** This specifies on what the function does (e.g., sorting), instead of how it does it (e.g., using quicksort or mergsort algorithms, implemented in C). By defining a function's behavior through *specifications*, developers can implement the function in different ways as long as it fulfills the specifications. Similarly, the user can use the function without knowing the implementation details.

Fig. 2.2 shows an example of abstraction by specification. The exists method return true if the target item is found in a list of sorted items. The user only needs to provide a sorted list and a target, but does not need to know what algorithm is used or implemented to determine if the item exists in the list.

```
def exists(items:List[int], target:int) -> bool:
    """
    Find an item in a list of sorted items.

Pre: List of sorted items
    Post: True if the target is found, False otherwise.
    """
    ...

# The user only needs to know that this function checks
# for the existence of an item in a sorted list.
# They don't need to know the search algorithm or implementation.
```

Fig. 2.2: Abstraction by Specification

#### 2.1 Specifications

We define abstractions through specifications, which describe what the abstraction is intended to do rather than how it should be implemented. This allows specifications to be much more concise and easier to read than the corresponding code.

Specifications which can be written in either formal or informal languages. Formal specifications have the advantage of being precise and unambiguous. However, in practice, we often use informal specifications, describing the behavior of the abstraction in plain English (e.g., the sorting example in Fig. 2.2). Note that a specification is not a programming language or a program. Thus, our specifications won't be written in code (e.g., in Python or Java)

#### 2.1.1 Specifications of a Function

The specification of a function consists of a *header* and a *description* of its behavior. The header gives the signature of the function, including its name, parameters, and return type. The description describes the function's behavior, including its preconditions and postconditions.

**Header** The header provides the *name* of the function, the number, order, and types of its *parameters* (inputs), and the type of its return value (output). For instance, the headers for the sort\_items function in Fig. 2.2 and the cal\_area function in Fig. 2.1 are as follows

```
def exists(items: list) -> bool: ...
def calc_area(length: float, width: float) -> float: ...
```

Note that in a language like Java, the header also provides *exceptions* that the function may throw.

**Preconditions and Postconditions** A typical function specification in an OOP language such as Python includes: *Preconditions* (also called the "requires" clause)

and *Postconditions* (also called the "effects" clause). Preconditions describe the conditions that must be true before the function is called. Typically these state the constraints or assumptions about the input parameters. If there are no preconditions, the clause is often written as None.

Postconditions, under the assumption that the preconditions are satisfied, describe the conditions that will be true after the function is called. These typically state the expected results or outcomes of the function. Moreover, they often describe the relationship between the inputs and outputs.

The clauses are usually written as *comments* above the function definition, making them easily accessible within the code.

```
def calc_area(length: float, width: float) -> float:
    """
    Calculates the area of a rectangle given its length and width.
    Pre: None
    Post: The area of the rectangle.
    """
    ...
```

For example, the specification of the calc\_area function in Fig. 2.1 has (i) no preconditions and (ii) the postcondition that the function returns the area of a rectangle given its length and width. Similarly, the exists function in Fig. 2.2 has the specification that given a list of sorted items (precondition), it returns true if the item is found in the list, and false otherwise (postcondition). Note how the specification is written in plain English, making it easy to understand for both developers and users of the function.

**Modifies** Another common clause in a function specification is *modifies*, which describes the inputs that the function modifies. This is particularly useful for functions that modify their input parameters.

```
def add_to_list(input_list, value):
    """
    Adds a value to the input list.

Pre: None
    Post: Value is added to the input list.
    Modifies: the input list
    """
    ...
```

#### 2.1.2 In-class Exercise: User Equality

This exercise touches on some thorny issues with inheritance. There is a lot going on in this example, but it is a good exercise to understand the subtleties of inheritance.

1. First, look at the Javadoc to understand the behaviors equals() (while the specification is for Java, the idea is the same in Python).

```
class User:
   def __init__(self, name):
        self.name = name
    def __eq__(self, other):
        if not isinstance(other, User):
           return False
        return self.name == other.name
                           Fig. 2.3: User class
class SpecialUser(User):
    """Don't do this until you've done with User"""
    def __init__(self, name, id):
        super().__init__(name)
        self.id = id
    def __eq__(self, other):
        if not isinstance(other, SpecialUser):
           return False
        return super().__eq__(other) and self.id == other.id
```

Fig. 2.4: SpecialUser class

- Specifically, read carefully the *symmetric*, *reflexive*, and *transitive* properties of equals().
- Ignore *consistency*, which requires that if two objects are equal, they remain equal.
- 2. For the User class in Fig. 2.3, does equals() satisfy the three equivalence relation properties? If not, what is the problem?
  - Come up with several concrete test cases (e.g., create various User instances) to check the properties.
  - If there is a problem, show the test case that demonstrates the problem.
  - Explain why the problem occurs and come up with a fix.
- 3. So the same analysis for the SpecialUser class in Fig. 2.4.

### 2.2 Designing Specifications

When designing specifications, it is important to consider several factors to ensure that the function is well-defined and can be used effectively. These factors include the *strength* of the pre- and post-conditions, whether the function is *total* or *partial*, and the *avoiding implementation details* in the specification.

#### 2.2.1 Weak Pre-conditions

For pre-conditions, we want as weak a constraint as possible to make the function more versatile, allowing it to handle a larger class of inputs. A condition is weaker than another if it is implied by the other or having less constraints than the other. For example, the condition  $x \leq 5$  is weaker than  $x \leq 10$  or that the input list is not sorted is weaker than the list is sorted (which is weaker than the list that is both sorted and has no duplicates). The *weakest* precondition is True, which indicates no constraints on the input.

#### 2.2.2 Strong Post-conditions

In contrast, for post-conditions, we want as strong a condition as possible to ensure that the function behaves as expected. A condition is stronger than another if it implies the other or that its constraints are a strict subset of the other. For example, the condition  $x \leq 10$  is stronger than  $x \leq 5$  or that the input list is sorted is stronger than the list is not sorted.

#### 2.2.3 Total vs Partial Functions

A function is *total* if it is defined for all legal inputs; otherwise, it is *partial*. Thus a function with no precondition is total, while a function with the strongest possible precondition is partial. Total functions are preferred because they can be used in more situations, especially when the function is used publicly or in a library where the user may not know the input constraints. Partial functions can be used when the function is used internally, e.g., a helper or auxiliary function and the caller is knowledgeable and can ensure its preconditions are satisfied.

The functions calc\_area function in Fig. 2.1 and add\_to\_list in Fig. 2.2 are total because they can be called with any input. The exists function in Fig. 2.2 is partial because it only works with sorted lists.

Turning Partial Functions into Total Functions It is often possible to turn a partial function into a total function in two steps. First, we move preconditions into postconditions and specify the expected behavior when the precondition is not satisfied, e.g., throws an Exception. Second, we modify the function to satisfy the new specification, i.e., handling the cases when the preconditions are not satisfied. For example, the exists function in Fig. 2.2 is turned into the total function shown in Fig. 2.5.

#### 2.2.4 In-class Exercise: Partial and Total Specifications for tail

Consider the following code:

```
def tail(my_list):
    result = my_list.copy()
```

• What does the implementation of tail do in each of the following cases? You might want to see the Python document for pop. How do you know: Running the code or reading Python document?

```
- list = None
- list = []
- list = [1]
- list = [1, 2, 3]
```

result.pop(0)
return result

- Write a partial specification for tail
- Rewrite the specification to be total. Use exceptions as needed.

#### 2.2.5 No implementation details

The specification should not include any implementation details, such as the algorithm used or the data structures employed. This improves flexibility as it allows the function to be implemented in different ways as long as it satisfies the specification. For example, the exists function in Fig. 2.2 does not specify the search algorithm used to find the item in the list.

Some common examples to avoid include the mentioning of specific data structures (e.g., arrays, indices), algorithms (e.g., quicksort or mergesort), and exceptions (e.g., related to IndexError). Instead, focus on the behavior of the function, such as the input and output relationships, the constraints on the input, and the expected results. Also avoid specifications mentioning indices because this implies the use of arrays.

#### 2.3 Exercise

#### 2.3.1 Specification for Sorting

Write the specification for the generic ascending\_sort method below. The specification should include preconditions and postconditions.

```
def ascending_sort(my_list):
    # REQUIRES/PRE:
    # EFFECTS/POST:
```

#### 2.3.2 Specification of Binary Search

Come up with the specification for a binary search implementation whose header is given below. Remember for precondition you want something as weak as possible and for postcondition as strong as possible. Note that binary search returns the location (an non-neg integer) of the target value if found, and returns -1 if target is not found.

```
def binary_search(arr: List[int], target: int) -> int:
    """
    PRE/REQUIRES:
    POST/EFFECTS:
    """
    ...
```

#### 2.3.3 Loan Calculator

Consider a function that calculates the number of months needed to pay off a loan of a given size at a fixed annual interest rate and a fixed monthly payment. For example, a \$100,000 loan at an 8% annual rate would take 166 months to discharge at a monthly payment of \$1,000, and 141 months to discharge at a monthly payment of \$1,100. (In both cases, the final payment is smaller than the others; we round 165.34 up to 166 and 140.20 up to 141.) Continuing the example, the loan would never be paid off at a monthly payment of \$100, since the principal would grow rather than shrink.

• Implementation satisfying given specification: Define a Python class called 'Loan'. In that class, write a function that satisfies the following specification:

```
class Loan:
    @staticmethod
    def months(principal: int, rate: float, payment: int) -> int:
        """
        Calculate the number of months required to pay off a loan.

    param principal: Amount of the initial principal (in dollars)
    param rate: Annual interest rate (e.g., 0.08 for 8%)
    param payment: Amount of the monthly payment (in dollars)
```

```
Requires/Pre: principal, rate, and payment all positive and payment is sufficiently large to drive the principal to zero. Effects/Post: return the number of months required to pay off the principal
```

Note that the precondition is quite strong, which makes implementing the method easy. The key step in your calculation is to change the principal on each iteration with the following formula (which amounts to monthly compounding):

```
new_principal = old_principal * (1 + monthly_interest_rate) - payment
```

- To make sure you understand the point about preconditions, your code is required to be *minimal*. Specifically, if it is possible to delete parts of your implementation and still have it satisfy the requirements, you'll earn less than full credit.
- *Total* specification: Now change the specification to *total* in which the post-condition handles violations of the preconditions using *exceptions*. In addition, provide a new implementation month that satisfies the new specification.

#### 2.3.4 Partial and Total Functions

- 1. Write the partial specifications for the below two functions.
- 2. Modify the specifications to make the functions total.
- 3. Modify the implementations of the two functions to satisfy the total specification.

Recall that specifications do not deal with types (which are taken care by the function signature and enforced by the type system of compiler/interpreter). In other words, you do not need to worry about types here and can assume conditions about types are satisfied.

```
def divide(a:float, b:float) -> float:
    """
    PRE:
    POST:
    """
    return a / b

def get_average(numbers: list[float]) -> float:
    """
    PRE:
    POST:
    """
    total = sum(numbers)
    return divide(total, len(numbers))
```

## Chapter 3

## Data Abstraction

This chapter focuses on abstract data type (ADT), a foundation of OOP and key concept in programming that allows developers to separate how data is implemented from how it behaves. Through ADT, programmers can create new data types relevant to their application. These ADTs consist of objects and associated operations.

### 3.1 Specifications of an ADT

The specification of ADT explains what the operations on the data type do, allowing users to interact with objects only via methods, rather than accessing the internal representation. As with functions (§2), the specification for an ADT defines its behaviors without being tied to a specific implementation.

**Structure of an ADT** In a modern OOP language such as Python or Java, data abstractions are defined using *classes*. Each class defines a name for the data type, along with its constructors and methods.

```
class DataType:
    """
    OVERVIEW: A brief description of the data type and its objects.

def __init__(self, ...):
    """
    Constructor to initialize a new object.
    """

def method1(self, ...):
    """
    Method to perform an operation on the object.
    """
```

Fig. 3.1: Abstract Data Type template

Fig. 3.1 shows a class template in Python, which consists of three main parts. The overview describes the abstract data type in terms of well-understood concepts, like mathematical models or real-world entities. For example, a stack could be described using mathematical sequences. The overview can also indicate whether the objects of this type are mutable (their state can change) or immutable. The Constructor initializes a new object, setting up any initial state required for the instance. Finally, methods define operations users can perform on the objects. These methods allow users to interact with the object without needing to know its internal representation. In Python, self is used to refer to the object itself, similar to this in Java or C++.

Note that as with procedural specification (§2), the specifications of constructors and methods of an ADT do not include implementation details. They only describe what the operation does, not how it is done. Moreover, they are written in plain English as code comment.

#### 3.1.1 Example: IntSet ADT

Fig. 3.2 gives the specification for an IntSet ADT, which represents unbounded set of integers. IntSet includes a constructor to initialize an empty set, and methods to insert, remove, check membership, get the size, and choose an element from the set. IntSet is also mutable, as it allows elements to be added or removed. *mutator* insert and remmove are mutator methods and have a MODIFIES clause. In contrast, is\_in, size, and choose are *observer* methods that do not modify the object.

### 3.2 Implementing ADT

To implement an ADT, we first choose a representation (rep) for its objects, then design constructors to initialize it correctly, and methods to interact with and modify the rep. For example, we can use a list (or vector) as the rep of IntSet in Fig. 3.2. We could use other data structures, such as a set or dict, as the rep, but a list is a simple choice for demonstration.

To aid understanding and reasoning of the rep of an ADT, we use two key concepts: representation invariant and abstraction function.

#### 3.2.1 Representation Invariant (Rep-Inv)

Because the rep might not be necessarily related to the ADT itself (e.g., the list has different properties compared to a set), we need to ensure that our use of the rep is consistent with the ADT's behavior. To do this, we use *representation invariant* (**rep-inv**) to specify the constraints for the rep of the ADT to capture its behavior.

For example, the rep-inv for a stack is that the last element added is the first to be removed and the rep-inv for a binary search tree is that the left child is less than the parent, and the right child is greater. The rep-inv for our IntSet ADT in Fig. 3.2 is that all elements in the list are unique.

```
class IntSet:
    OVERVIEW: IntSets are unbounded, mutable sets of integers.
   This implementation uses a list to store the elements, ensuring no duplicates.
    def __init__(self):
        Constructor
        EFFECTS: Initializes this to be an empty set.
        self.els = [] # the representation (list)
    def insert(self, x: int) -> None:
        MODIFIES: self
        EFFECTS: Adds x to the elements of this set if not already present.
        if not self.is_in(x): self.els.append(x)
    def remove(self, x: int) -> int:
        MODIFIES: self
        EFFECTS: Removes x from this set if it exists. Also returns
        the index of x in the list.
        i = self.find_idx(x)
        if i != -1:
            # Remove the element at index i
            self.els = self.els[:i] + self.els[i+1:]
        return i
    def is_in(self, x: int) -> (bool, int):
        {\tt EFFECTS}\colon If x is in this set, return True. Otherwise False.
        return True if find_index(x) != -1 else False
    def find_idx(self, x:int)->int:
        EFFECTS: If x is in this set, return its index. Otherwise returns -1.
        for i, element in enumerate(self.els):
            if x == element:
               return i
        return -1
    def size(self) -> int:
        EFFECTS: Returns the number of elements in this set (its cardinality).
        return len(self.els)
    def choose(self) -> int:
        EFFECTS: If this set is empty, raises an Exception.
        Otherwise, returns an arbitrary element of this set.
        0.00
        if len(self.els) == 0:
            raise Exception(...)
        return self.els[-1] # Returns the last element arbitrarily
    def __str__(self) -> str:
        Abstract function (AF) that returns a string representation of this set.
        EFFECTS: Returns a string representation of this set.
        0.00
        return str(self.els)
```

Fig. 3.2: The IntSet ADT

```
# Rep-inv:
# els is not null, only contains integers and has no duplicates.
```

The rep-inv must be preserved by all methods (more precisely, *mutator* methods). It must hold true before and after the method is called. The rep-inv might be violated temporarily during the method execution, but it must be restored before the method returns. For IntSet Notice that the mutator insert method ensures that the element is not already in the list before adding it.

The rep-inv is decided by the designer and specified in the ADT documentation as part of the specification (just like pre/post conditions) so that it is ensured at the end of each method (like the postcondition). Moreover, because rep-inv is so important, it is not only documented in comments but also checked at runtime. This is done by invoking a repOK, discussed later, method at the start and end of each method.

#### In-Class Exercise: Checking Rep-Invs

```
class Members:
    Overview: Members is a mutable record of organization membership.
    AF: Collect the list as a set.
       - rep-inv1: members != None
        - rep-inv2: members != None and no duplicates in members.
       For simplicity, assume None can be a member.
    def __init__(self):
        """Constructor: Initializes the membership list."""
        self.members = [] # The representation
    def join(self, person):
        Post: person becomes a member.
        MODIFIES: self
        EFFECTS: Adds a person to the membership list.
        self.members.append(person)
    def leave(self, person):
        Post: person is no longer a member.
        MODIFIES: self
        EFFECTS: Removes a person from the membership list.
        self.members.remove(person)
```

- 1. Analyze these four questions for rep-inv 1.
  - Does join() maintain rep-inv?
  - Does join() satisfy its specification?

- Does leave() maintain rep-inv?
- Does leave() satisfy its specification?
- 2. Repeat for rep-inv 2.
- 3. Recode join() to make the verification go through. Which rep-invariant do you use?
- 4. Recode leave() to make the verification go through. Which rep-invariant do you use?

#### 3.2.2 Abstraction Function (AF)

It can be difficult to understand the ADT by looking at the rep directly. For example, we might not be able to visualize or reason about a binary tree or a graph ADT when using list as the rep. To aid understanding, abstraction function (**AF**) provides a mapping between the rep and the ADT. Specifically, the AF maps from a concrete state (i.e., the else els) to an abstract state (i.e., the set). AF is also a many-to-one mapping, as multiple concrete states can map to the same abstract state, e.g., the list [1, 2, 3] and [3, 2, 1] both map to the same set {1, 2, 3}.

Just as with rep-inv, the AF is documented in the class specification. Modern OOP languages often provide methods implementing the AF, in particular developer overrides the <code>\_\_str\_\_</code> method in Python and toString in Java to return a string representation of the object. For example, the <code>\_\_str\_\_</code> method in Fig. 3.2 returns a string representation of the set.

#### 3.2.3 In-Class Excercise: Stack

In this exercise, you will implement a Stack ADT. A stack is a common data structure that follows the Last-In-First-Out (LIFO) principle. You will:

- 1. Choose a Representation (rep) for the stack.
- 2. Define a Representation invariant (rep-inv)
- 3. Write a repOK method
- 4. Provide the specifications of basic stack operations (push, pop, is\_empty) and implement these methods accordingly.
- 5. Define an Abstraction Function (AF)
- 6. Implement \_\_str\_\_() to return a string representation of the stack based on the AF

#### 3.3 Mutability vs. Immutability

An ADT can be either mutable or immutable, depending on whether their objects' values can change over time. An ADT should be immutable if the objects it models naturally have unchanging values, such as mathematical objects like integers, polynomials (Polys), or complex numbers. On the other hand, an ADT should be mutable if it models real-world entities that undergo changes, such as an automobile in a simulation, which might be running or stopped, or contain passengers, or if the ADT models data storage, like arrays or sets.

Immutability is beneficial because it offers greater safety and allows sharing of subparts without the risk of unexpected changes. Moreover, immutability can simplify the design by ensuring the object's state is fixed once created. However, immutable objects can be less efficient, as creating a new object for each change can be costly in terms of memory and time.

Converting from mutable to immutable Given a mutable ADT, it is possible to convert it to an immutable one by ensuring that the rep is not modified by any method. This can be achieved by making the rep private and only allowing read-only access to it. In Python, this can be done by using the Oproperty decorator to create read-only properties. For example, the els list in Fig. 3.2 can be made read-only by defining a property method elements that returns a copy of the list.

```
class IntSet:
    def __init__(self):
        self.__els = [] # Private rep
    @property
    def self.els(self):
        return self.__els
```

Moreover, we need to convert mutator methods into observer methods, which make a copy of the rep, modify it, and return the modified rep object.

```
def insert_immutable(self, x: int) -> IntSet:
    new_set = self.els.copy()
    if not self.is_in(x):
        new_set = new_set.append(x)
    return new_set
```

If the mutator returns a value v, then our new method returns a tuple consisting of (i) the new rep object and the return the value v.

```
def remove_immutable(self, x: int): -> (IntSet, int):
    i = self.find_idx(x)
    new_set = self.els.copy()
    if i != -1:
        # Remove the element at index i
        new_set = self.els[:i] + self.els[i+1:]
    return (new_set, i)
```

If you do not want to return multiple values (e.g., like in Java), then you can create two methods, one for returning the value and the other for returning the new

rep object. For example, a mutator pop method of a Stack would result into two methods: pop2 returns the top element and pop3 returns the new stack with the top element removed.

Finally, it is important that while it is possible to convert a mutable ADT to an immutable one as shown, mutability or immutability should be the property of the ADT type itself, not its implementation. Thus, it should be decided at the design stage and documented in the ADT specification.

#### 3.3.1 In-class Exercise: Immutable Queue

Consider the mutable Queue implementation in Fig. 3.3. Rewrite Queue to be *immutable*. Keep the representation variables elements and size.

#### 3.4 Exercise

#### 3.4.1 Polynomial ADT

Use the Poly ADT in Fig. 3.4 to answer the following question. Use the Stack ADT in Fig. B.1 as an example.

- 1. Write an Overview that describes what Poly does. You must provide some examples to demonstrate (e.g., Poly(2,3) means what?).
- 2. Provide the specifications for all methods in the ADT.
- 3. Write the **rep** used in this code. Describe how this rep represents Poly2.
- 4. Provide the **rep-inv** for the Poly2 ADT. Note, this would be the constraints over the rep variable(s).
- 5. Write a RepOK method that checks the rep-inv.
- 6. Describe the AF in this code. Use \_\_str\_\_ to help.

```
class Queue:
    A generic Queue implementation using a list.
   def __init__(self):
        Constructor
        Initializes an empty queue.
       self.elements = []
        self.size = 0
    def enqueue(self, e):
        MODIFIES: self
        EFFECTS: Adds element e to the end of the queue.
        self.elements.append(e)
        self.size += 1
    def dequeue(self):
        MODIFIES: self
        {\tt EFFECTS:} Removes and returns the element at the front of the queue.
        If the queue is empty, raises an {\tt IllegalStateException}.
        if self.size == 0:
            raise Exception(...)
        result = self.elements.pop(0) # Removes and returns the first element
        self.size -= 1
        return result
    def is_empty(self):
        EFFECTS: Returns True if the queue is empty, False otherwise.
        return self.size == 0
```

Fig. 3.3: Mutable Queue

```
class Poly:
    def __init__(self, c=0, n=0):
        if n < 0:
           raise ValueError("Poly(int, int) constructor: n must be >= 0")
        self.trms = {}
        if c != 0:
            self.trms[n] = c
    def degree(self):
        if len(self.trms) > 0:
            return next(reversed(self.trms.keys()))
        return 0
    def coeff(self, d):
        if d < 0:
            raise ValueError("Poly.coeff: d must be >= 0")
        return self.trms.get(d, 0)
    def sub(self, q):
        if q is None:
            raise ValueError("Poly.sub: q is None")
        return self.add(q.minus())
    def minus(self):
        result = Poly()
        for n, c in self.trms.items():
            result.trms[n] = -c
        return result
    def add(self, q):
        if q is None:
            raise ValueError("Poly.add: q is None")
        non_zero = set(self.trms.keys()).union(q.trms.keys())
        result = Poly()
        for n in non_zero:
            new_coeff = self.coeff(n) + q.coeff(n)
            if new_coeff != 0:
               result.trms[n] = new_coeff
        return result
    def mul(self, q):
        if q is None:
            raise ValueError("Poly.mul: q is None")
        result = Poly()
        for n1, c1 in self.trms.items():
            for n2, c2 in q.trms.items():
                result = result.add(Poly(c1 * c2, n1 + n2))
        return result
    def __str__(self):
        r = "Poly:"
        if len(self.trms) == 0:
            r += " 0"
        for n, c in self.trms.items():
            if c < 0:
               r += f'' - \{-c\}x^{n}''
            else:
               r += f" + {c}x^{n}"
        return r
```

Fig. 3.4: Polynomial ADT

## Chapter 4

## Iterators and Generators

Appendix A

Miscs

## Appendix B

## Answers

B.1 ADT

B.1.1 Stack ADT

```
class Stack:
OVERVIEW: Stack is a mutable ADT that represents a collection of elements in LIFO.
AF(c) = the sequence of elements in the stack in sorted order from bottom to top.
rep-inv:
   1. elements is a list (could be empty list, which represents and empty stack).
   2. The top of the stack is always the last element in the list.
def __init__(self):
    Constructor
   EFFECTS: Initializes an empty stack.
   MODIFIES: self
   self.elements = []
def repOK(self):
   EFFECTS: Returns True if the rep-invariant holds, otherwise False.
   The invariant checks:
   1. elements is a list.
   2. If the stack is non-empty, the top of the stack is the last element in the list.
   # Check that elements is a list
   if not isinstance(self.elements, list):
        return False
   # If the stack is not empty, ensure that the top is the last element in the list.
    # This is implicitly guaranteed by the use of 'list.append' for push and 'list.pop' for
    # so no further explicit check is needed for the "top as last element."
   return True
def push(self, value):
    MODIFIES: self
   EFFECTS: Adds value to the top of the stack.
    self.elements.append(value)
def pop(self):
    MODIFIES: self
   EFFECTS: Removes and returns the top element from the stack.
   Raises an exception if the stack is empty.
    if self.is_empty():
       raise Exception("Stack is empty")
    return self.elements.pop()
def is_empty(self):
    EFFECTS: Returns True if the stack is empty, otherwise False.
   return len(self.elements) == 0
def __str__(self):
   {\tt EFFECTS: \ Returns \ a \ string \ representation \ of \ the \ stack}\,,
             showing the elements from bottom to top.
   \# The abstraction function maps the list of elements to a stack view
   return f"Stack({self.elements})"
```

Fig. B.1: Stack ADT