```
        conv_w2 = tf.zeros((3, 3, 6, 9))
        conv_b2 = tf.zeros((9,))
        fc_w = tf.zeros((32 * 32 * 9, 10))
        fc_b = tf.zeros((10,))
        params = [conv_w1, conv_b1, conv_w2, conv_b2, fc_w, fc_b]
        scores = three_layer_convnet(x, params)

    # Inputs to convolutional layers are 4-dimensional arrays with shape
    # [batch_size, height, width, channels]
    print('scores_np has shape: ', scores.shape)

three_layer_convnet_test()
```

```
scores_np has shape:  (64, 10)
```

Barebones TensorFlow: Training Step

We now define the `training_step` function performs a single training step. This will take three basic steps:

1. Compute the loss
2. Compute the gradient of the loss with respect to all network weights
3. Make a weight update step using (stochastic) gradient descent.

We need to use a few new TensorFlow functions to do all of this:

- For computing the cross-entropy loss we'll use `tf.nn.sparse_softmax_cross_entropy_with_logits`: https://www.tensorflow.org/versions/r2.0/api_docs/python/tf/nn/sparse_softmax_cross_entropy_with_logits
- For averaging the loss across a minibatch of data we'll use `tf.reduce_mean`: https://www.tensorflow.org/versions/r2.0/api_docs/python/tf/reduce_mean
- For computing gradients of the loss with respect to the weights we'll use `tf.GradientTape` (useful for Eager execution): https://www.tensorflow.org/versions/r2.0/api_docs/python/tf/GradientTape
- We'll mutate the weight values stored in a TensorFlow Tensor using `tf.assign_sub` ("sub" is for subtraction): https://www.tensorflow.org/api_docs/python/tf/assign_sub

In [12]:
```python
def training_step(model_fn, x, y, params, learning_rate):
    with tf.GradientTape() as tape:
        scores = model_fn(x, params) # Forward pass of the model
        loss = tf.nn.sparse_softmax_cross_entropy_with_logits(labels=y, logits=scores)
        total_loss = tf.reduce_mean(loss)
        grad_params = tape.gradient(total_loss, params)

        # Make a vanilla gradient descent step on all of the model parameters
        # Manually update the weights using assign_sub()
        for w, grad_w in zip(params, grad_params):
            w.assign_sub(learning_rate * grad_w)

        return total_loss
```

In [13]:
```python
def train_part2(model_fn, init_fn, learning_rate, epochs):
    """
    Train a model on CIFAR-10.

    Inputs:
    - model_fn: A Python function that performs the forward pass of the model
      using TensorFlow; it should have the following signature:
      scores = model_fn(x, params) where x is a TensorFlow Tensor giving a
      minibatch of image data, params is a list of TensorFlow Tensors holding
      the model weights, and scores is a TensorFlow Tensor of shape (N, C)
      giving scores for all elements of x.
    - init_fn: A Python function that initializes the parameters of the model.
      It should have the signature params = init_fn() where params is a list
      of TensorFlow Tensors holding the (randomly initialized) weights of the
      model.
    - learning_rate: Python float giving the learning rate to use for SGD.
    """


    params = init_fn()  # Initialize the model parameters
    for e in range(epochs):
        for t, (x_np, y_np) in enumerate(train_dset):
            # Run the graph on a batch of training data.
            loss = training_step(model_fn, x_np, y_np, params, learning_rate)

            # Periodically print the loss and check accuracy on the val set.
            if t % print_every == 0:
                print('Epoch %d, iteration %d, loss = %.4f' % (e, t, loss))
                print('Validation:')
                check_accuracy(val_dset, model_fn, params)
    return params
```

In [14]:
```python
def check_accuracy(dset, model_fn, params):
    """
    Check accuracy on a classification model, e.g. for validation.

    Inputs:
    - dset: A Dataset object against which to check accuracy
    - x: A TensorFlow placeholder Tensor where input images should be fed
    - model_fn: the Model we will be calling to make predictions on x
    - params: parameters for the model_fn to work with

    Returns: Nothing, but prints the accuracy of the model
    """
    num_correct, num_samples = 0, 0
    for x_batch, y_batch in dset:
        scores_np = model_fn(x_batch, params).numpy()
        y_pred = scores_np.argmax(axis=1)
        num_samples += x_batch.shape[0]
        num_correct += (y_pred == y_batch).sum()
    acc = float(num_correct) / num_samples
    print('     Got %d / %d correct (%.2f%%)' % (num_correct, num_samples, 100 * acc))
```

Barebones TensorFlow: Initialization

We'll use the following utility method to initialize the weight matrices for our models using Kaiming's normalization method.

[1] He et al, *Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification*, ICCV 2015, https://arxiv.org/abs/1502.01852

In [15]:
```python
def create_matrix_with_kaiming_normal(shape):
    if len(shape) == 2:
        fan_in, fan_out = shape[0], shape[1]
    elif len(shape) == 4:
        fan_in, fan_out = np.prod(shape[:3]), shape[3]
    return tf.keras.backend.random_normal(shape) * np.sqrt(2.0 / fan_in)
```

Barebones TensorFlow: Train a Two-Layer Network

We are finally ready to use all of the pieces defined above to train a two-layer fully-connected network on CIFAR-10.

We just need to define a function to initialize the weights of the model, and call `train_part2`.

Defining the weights of the network introduces another important piece of TensorFlow API: `tf.Variable`. A TensorFlow Variable is a Tensor whose value is stored in the graph and persists across runs of the computational graph; however unlike constants defined with `tf.zeros` or `tf.random_normal`, the values of a Variable can be mutated as the graph runs; these mutations will persist across graph runs. Learnable parameters of the network are usually stored in Variables.

You don't need to tune any hyperparameters, but you should achieve validation accuracies above 40% after one epoch of training.

In [16]:
```python
def two_layer_fc_init():
    """
    Initialize the weights of a two-layer network, for use with the
    two_layer_network function defined above.
    You can use the `create_matrix_with_kaiming_normal` helper!

    Inputs: None

    Returns: A list of:
    - w1: TensorFlow tf.Variable giving the weights for the first layer
    - w2: TensorFlow tf.Variable giving the weights for the second layer
    """
    hidden_layer_size = 4000
    w1 = tf.Variable(create_matrix_with_kaiming_normal((3 * 32 * 32, 4000)))
    w2 = tf.Variable(create_matrix_with_kaiming_normal((4000, 10)))
    return [w1, w2]

learning_rate = 1e-2
print('Train')
trained_params = train_part2(two_layer_fc, two_layer_fc_init, learning_rate,5)
print('Done!')
```

```
Train
Epoch 0, iteration 0, loss = 3.2669
Validation:
     Got 153 / 1000 correct (15.30%)
Epoch 0, iteration 100, loss = 1.9611
Validation:
     Got 381 / 1000 correct (38.10%)
Epoch 0, iteration 200, loss = 1.4588
Validation:
     Got 395 / 1000 correct (39.50%)
Epoch 0, iteration 300, loss = 1.7816
Validation:
     Got 379 / 1000 correct (37.90%)
Epoch 0, iteration 400, loss = 1.8149
Validation:
     Got 412 / 1000 correct (41.20%)
Epoch 0, iteration 500, loss = 1.7826
Validation:
     Got 431 / 1000 correct (43.10%)
Epoch 0, iteration 600, loss = 1.8439
Validation:
     Got 414 / 1000 correct (41.40%)
Epoch 0, iteration 700, loss = 2.0024
Validation:
     Got 439 / 1000 correct (43.90%)
Epoch 1, iteration 0, loss = 1.4206
Validation:
     Got 432 / 1000 correct (43.20%)
Epoch 1, iteration 100, loss = 1.5589
Validation:
     Got 471 / 1000 correct (47.10%)
Epoch 1, iteration 200, loss = 1.2061
Validation:
     Got 451 / 1000 correct (45.10%)
Epoch 1, iteration 300, loss = 1.5479
Validation:
     Got 430 / 1000 correct (43.00%)
Epoch 1, iteration 400, loss = 1.4992
Validation:
     Got 442 / 1000 correct (44.20%)
Epoch 1, iteration 500, loss = 1.5921
Validation:
     Got 475 / 1000 correct (47.50%)
Epoch 1, iteration 600, loss = 1.6357
Validation:
     Got 470 / 1000 correct (47.00%)
Epoch 1, iteration 700, loss = 1.7241
Validation:
     Got 468 / 1000 correct (46.80%)
Epoch 2, iteration 0, loss = 1.2329
Validation:
     Got 460 / 1000 correct (46.00%)
Epoch 2, iteration 100, loss = 1.4329
Validation:
     Got 503 / 1000 correct (50.30%)
Epoch 2, iteration 200, loss = 1.0665
Validation:
     Got 478 / 1000 correct (47.80%)
Epoch 2, iteration 300, loss = 1.4302
Validation:
     Got 460 / 1000 correct (46.00%)
Epoch 2, iteration 400, loss = 1.3164
Validation:
     Got 462 / 1000 correct (46.20%)
Epoch 2, iteration 500, loss = 1.4798
Validation:
     Got 485 / 1000 correct (48.50%)
Epoch 2, iteration 600, loss = 1.4967
Validation:
     Got 485 / 1000 correct (48.50%)
Epoch 2, iteration 700, loss = 1.5729
Validation:
     Got 494 / 1000 correct (49.40%)
Epoch 3, iteration 0, loss = 1.1198
Validation:
     Got 476 / 1000 correct (47.60%)
Epoch 3, iteration 100, loss = 1.3349
Validation:
     Got 504 / 1000 correct (50.40%)
Epoch 3, iteration 200, loss = 0.9685
Validation:
     Got 500 / 1000 correct (50.00%)
Epoch 3, iteration 300, loss = 1.3316
Validation:
     Got 474 / 1000 correct (47.40%)
Epoch 3, iteration 400, loss = 1.1783
Validation:
     Got 469 / 1000 correct (46.90%)
Epoch 3, iteration 500, loss = 1.4002
Validation:
     Got 496 / 1000 correct (49.60%)
Epoch 3, iteration 600, loss = 1.3765
Validation:
     Got 487 / 1000 correct (48.70%)
Epoch 3, iteration 700, loss = 1.4655
Validation:
     Got 504 / 1000 correct (50.40%)
Epoch 4, iteration 0, loss = 1.0279
Validation:
     Got 477 / 1000 correct (47.70%)
Epoch 4, iteration 100, loss = 1.2462
Validation:
     Got 513 / 1000 correct (51.30%)
Epoch 4, iteration 200, loss = 0.8884
Validation:
     Got 505 / 1000 correct (50.50%)
Epoch 4, iteration 300, loss = 1.2518
Validation:
     Got 473 / 1000 correct (47.30%)
Epoch 4, iteration 400, loss = 1.0666
Validation:
     Got 481 / 1000 correct (48.10%)
Epoch 4, iteration 500, loss = 1.3250
Validation:
     Got 498 / 1000 correct (49.80%)
Epoch 4, iteration 600, loss = 1.2657
Validation:
     Got 491 / 1000 correct (49.10%)
Epoch 4, iteration 700, loss = 1.3783
Validation:
     Got 515 / 1000 correct (51.50%)
Done!
```

Test Set - DO THIS ONLY ONCE

Now that we've gotten a result that we're happy with, we test our final model on the test set. This would be the score we would achieve on a competition. Think about how this compares to your validation set accuracy.

In [17]:
```python
print('Test')
check_accuracy(test_dset, two_layer_fc, trained_params)
```

```
Test
     Got 5010 / 10000 correct (50.10%)
```

Barebones TensorFlow: Train a three-layer ConvNet

We will now use TensorFlow to train a three-layer ConvNet on CIFAR-10.

You need to implement the `three_layer_convnet_init` function. Recall that the architecture of the network is:

1. Convolutional layer (with bias) with 32 5x5 filters, with zero-padding 2
2. ReLU
3. Convolutional layer (with bias) with 16 3x3 filters, with zero-padding 1
4. ReLU
5. Fully-connected layer (with bias) to compute scores for 10 classes

You don't need to do any hyperparameter tuning, but you should see validation accuracies above 43% after one epoch of training.

In [18]:
```python
def three_layer_convnet_init():
    """
    Initialize the weights of a Three-Layer ConvNet, for use with the
    three_layer_convnet function defined above.
    You can use the `create_matrix_with_kaiming_normal` helper!

    Inputs: None

    Returns a list containing:
    - conv_w1: TensorFlow tf.Variable giving weights for the first conv layer
    - conv_b1: TensorFlow tf.Variable giving biases for the first conv layer
    - conv_w2: TensorFlow tf.Variable giving weights for the second conv layer
    - conv_b2: TensorFlow tf.Variable giving biases for the second conv layer
    - fc_w: TensorFlow tf.Variable giving weights for the fully-connected layer
    - fc_b: TensorFlow tf.Variable giving biases for the fully-connected layer
    """
    params = None
    ############################################################################
    # TODO: Initialize the parameters of the three-layer network.              #
    ############################################################################
    # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****

    params = []
    conv_w1 = tf.Variable(create_matrix_with_kaiming_normal((5,5,3,6)))
    conv_b1 = tf.Variable(tf.keras.backend.random_normal((6,)))
    conv_w2 = tf.Variable(create_matrix_with_kaiming_normal((3, 3, 6, 9)))
    conv_b2 = tf.Variable(tf.keras.backend.random_normal((9,)))
    fc_w = tf.Variable(create_matrix_with_kaiming_normal((32 * 32 * 9, 10)))
    fc_b = tf.Variable(tf.keras.backend.random_normal((10,)))
    params = [conv_w1, conv_b1, conv_w2, conv_b2, fc_w, fc_b]

    # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****
    ############################################################################
    #                             END OF YOUR CODE                             #
    ############################################################################
    return params

learning_rate = 3e-3
train_part2(three_layer_convnet, three_layer_convnet_init, learning_rate,5)
```

```
Epoch 0, iteration 0, loss = 3.4912
Validation:
     Got 96 / 1000 correct (9.60%)
Epoch 0, iteration 100, loss = 2.0192
Validation:
     Got 309 / 1000 correct (30.90%)
Epoch 0, iteration 200, loss = 1.6970
Validation:
     Got 314 / 1000 correct (31.40%)
Epoch 0, iteration 300, loss = 1.9069
Validation:
     Got 278 / 1000 correct (27.80%)
Epoch 0, iteration 400, loss = 1.9812
Validation:
     Got 378 / 1000 correct (37.80%)
Epoch 0, iteration 500, loss = 1.8868
Validation:
     Got 380 / 1000 correct (38.00%)
Epoch 0, iteration 600, loss = 1.8454
Validation:
     Got 407 / 1000 correct (40.70%)
Epoch 0, iteration 700, loss = 1.7536
Validation:
     Got 395 / 1000 correct (39.50%)
Epoch 1, iteration 0, loss = 1.7158
Validation:
     Got 420 / 1000 correct (42.00%)
Epoch 1, iteration 100, loss = 1.5391
Validation:
     Got 438 / 1000 correct (43.80%)
Epoch 1, iteration 200, loss = 1.3815
Validation:
     Got 432 / 1000 correct (43.20%)
Epoch 1, iteration 300, loss = 1.6087
Validation:
     Got 411 / 1000 correct (41.10%)
Epoch 1, iteration 400, loss = 1.7290
Validation:
     Got 455 / 1000 correct (45.50%)
Epoch 1, iteration 500, loss = 1.7438
Validation:
     Got 455 / 1000 correct (45.50%)
Epoch 1, iteration 600, loss = 1.6969
Validation:
     Got 464 / 1000 correct (46.40%)
Epoch 1, iteration 700, loss = 1.6120
Validation:
     Got 444 / 1000 correct (44.40%)
Epoch 2, iteration 0, loss = 1.5220
Validation:
     Got 468 / 1000 correct (46.80%)
Epoch 2, iteration 100, loss = 1.3861
Validation:
     Got 480 / 1000 correct (48.00%)
Epoch 2, iteration 200, loss = 1.2272
Validation:
     Got 455 / 1000 correct (45.50%)
Epoch 2, iteration 300, loss = 1.5306
Validation:
     Got 454 / 1000 correct (45.40%)
Epoch 2, iteration 400, loss = 1.5997
Validation:
     Got 478 / 1000 correct (47.80%)
Epoch 2, iteration 500, loss = 1.6634
Validation:
     Got 466 / 1000 correct (46.60%)
Epoch 2, iteration 600, loss = 1.6340
Validation:
     Got 482 / 1000 correct (48.20%)
Epoch 2, iteration 700, loss = 1.5313
Validation:
     Got 460 / 1000 correct (46.00%)
Epoch 3, iteration 0, loss = 1.4125
Validation:
     Got 487 / 1000 correct (48.70%)
Epoch 3, iteration 100, loss = 1.3280
Validation:
     Got 488 / 1000 correct (48.80%)
Epoch 3, iteration 200, loss = 1.1351
Validation:
     Got 480 / 1000 correct (48.00%)
Epoch 3, iteration 300, loss = 1.4892
Validation:
     Got 469 / 1000 correct (46.90%)
Epoch 3, iteration 400, loss = 1.4847
Validation:
     Got 492 / 1000 correct (49.20%)
Epoch 3, iteration 500, loss = 1.6001
Validation:
     Got 480 / 1000 correct (48.00%)
Epoch 3, iteration 600, loss = 1.5752
Validation:
     Got 490 / 1000 correct (49.00%)
Epoch 3, iteration 700, loss = 1.4686
Validation:
     Got 470 / 1000 correct (47.00%)
Epoch 4, iteration 0, loss = 1.3534
Validation:
     Got 501 / 1000 correct (50.10%)
Epoch 4, iteration 100, loss = 1.2806
Validation:
     Got 504 / 1000 correct (50.40%)
Epoch 4, iteration 200, loss = 1.0873
Validation:
     Got 495 / 1000 correct (49.50%)
Epoch 4, iteration 300, loss = 1.4536
Validation:
     Got 480 / 1000 correct (48.00%)
Epoch 4, iteration 400, loss = 1.3897
Validation:
     Got 499 / 1000 correct (49.90%)
Epoch 4, iteration 500, loss = 1.5538
Validation:
     Got 494 / 1000 correct (49.40%)
Epoch 4, iteration 600, loss = 1.5211
Validation:
     Got 511 / 1000 correct (51.10%)
Epoch 4, iteration 700, loss = 1.4154
Validation:
     Got 496 / 1000 correct (49.60%)
```

Out[18]:

```
[<tf.Variable 'Variable:0' shape=(5, 5, 3, 6) dtype=float32, numpy=
 array([[[[-1.61023080e-01, -3.57654124e-01, -5.57530113e-02,
            1.08809434e-01,  6.69642091e-02, -2.09259894e-02],
          [-1.76452994e-01,  1.78291574e-01, -1.91033855e-01,
           -1.28879309e-01,  1.63099810e-01,  1.96192876e-01],
          [-2.51754194e-01,  1.24469576e-02, -1.14151292e-01,
           -1.71669394e-01,  1.76264435e-01, -1.27576426e-01]],

         [[-2.63451815e-01, -2.82874908e-02,  3.18080068e-01,
            5.89057393e-02,  2.69026458e-01,  8.54602829e-02],
          [ 1.12584002e-01, -2.92198081e-02, -7.99711496e-02,
            1.18740834e-01,  3.32016081e-01, -1.06072687e-01],
          [ 4.59256262e-01, -2.69302279e-01, -1.08170494e-01,
            2.99252689e-01, -1.40057772e-01,  3.64535786e-02]],

         [[-4.17102873e-03,  1.92432920e-03,  3.51799667e-01,
           -4.44434956e-02, -1.49059489e-01, -1.18448369e-01],
          [-6.14424087e-02, -1.47815809e-01, -2.68678784e-01,
            1.67379193e-02,  1.31854743e-01,  1.88780159e-01],
          [ 1.27318025e-01, -1.67568833e-01,  1.48361757e-01,
            4.19210225e-01,  3.83997947e-01,  3.22185606e-01]],

         [[-6.12008162e-02,  2.96073891e-02,  4.05141972e-02,
           -2.31950760e-01,  5.95969670e-02,  1.70635313e-01],
          [ 1.25713110e-01,  2.92245205e-02,  1.35159967e-02,
            3.65649283e-01, -2.91873336e-01,  1.16394892e-01],
          [ 6.65615126e-02,  3.02799642e-01,  1.90781474e-01,
            9.97016430e-02, -4.16725799e-02, -1.06976582e-02]],

         [[-6.81720078e-02, -3.84814143e-02,  1.49973348e-01,
           -4.11530882e-02, -1.50413096e-01, -1.63804308e-01],
          [-6.40001073e-02,  2.71310449e-01, -2.10033208e-01,
           -1.35941505e-01,  6.66388869e-02,  1.17558539e-01],
          [-9.06707626e-03,  1.22606978e-01,  4.33413796e-02,
            7.73371384e-02, -1.08259305e-01, -1.82767719e-01]]],


        [[[ 8.20036680e-02,  3.88933450e-01, -9.08889323e-02,
           -2.37561613e-01, -1.64695352e-01,  6.63509518e-02],
          [ 7.26601034e-02, -5.42058572e-02, -2.59345174e-01,
           -4.48032558e-01,  1.97651181e-02, -1.25800148e-01],
          [ 2.64301211e-01, -4.70886044e-02, -1.71780884e-01,
            1.54368550e-01, -1.11420639e-01, -1.95297286e-01]],

         [[-5.90994470e-02, -1.18476257e-01,  3.93894017e-01,
           -2.80745298e-01, -3.12330723e-02,  7.48639777e-02],
          [ 1.11728400e-01, -9.67562646e-02, -9.88375768e-02,
           -9.93190240e-03,  1.37872353e-01,  1.09919002e-02],
          [-1.50638506e-01, -1.35570243e-01,  6.99630976e-02,
           -3.77782404e-01,  3.14936042e-02,  1.25454262e-01]],

         [[-1.26522509e-02, -5.51094413e-02,  1.66640893e-01,
           -5.41249057e-03,  2.04144195e-01, -3.21926296e-01],
          [-9.02229548e-03,  2.20002890e-01,  2.44143605e-01,
            2.51814663e-01, -1.03261270e-01, -2.02067405e-01],
          [ 2.18486518e-01,  2.94500589e-01, -2.04122793e-02,
            9.64790955e-02,  2.24568039e-01, -6.72873110e-02]],

         [[-1.18441507e-01,  1.13491334e-01, -1.47159681e-01,
            9.05961823e-03, -1.91679612e-01,  1.48271382e-01],
          [-1.23273812e-01,  1.47988096e-01, -8.07834491e-02,
           -2.57321775e-01,  4.06926394e-01, -9.65830982e-02],
          [ 1.16713159e-01, -5.26903272e-02, -7.13911578e-02,
            1.85620666e-01, -1.80933878e-01, -9.98366177e-02]],

         [[ 6.44773170e-02,  6.72514969e-03,  1.04621246e-01,
           -1.50316030e-01,  8.18532147e-03, -1.15929782e-01],
          [-3.04808587e-01,  5.43309450e-02, -3.28920037e-02,
            1.58403233e-01, -4.11343157e-01,  1.32309556e-01],
          [ 2.91832894e-01, -7.57390112e-02,  3.63887958e-02,
            8.41281861e-02, -6.63854033e-02, -1.58029214e-01]]],


        [[[ 1.72687992e-01,  6.04600972e-03,  4.50536888e-03,
           -1.97907850e-01, -1.91568136e-01,  3.36992592e-02],
          [ 2.47801110e-01, -5.12441635e-01, -1.95457146e-01,
            5.28516136e-02,  1.54274851e-01, -2.56007373e-01],
          [ 1.51660517e-01,  1.14080429e-01, -2.41359890e-01,
           -3.68347436e-01, -1.56985328e-01,  1.76137924e-01]],

         [[-3.15878242e-01,  4.35388228e-03,  8.09998140e-02,
           -3.52561697e-02, -2.71875143e-01,  1.17808133e-01],
          [ 2.21005559e-01,  1.50973678e-01,  2.84645762e-02,
           -1.01251014e-01,  2.59770583e-02,  2.04798207e-02],
          [-1.32070526e-01,  1.56649128e-01,  5.08544594e-02,
           -3.52941044e-02, -5.03243618e-02,  5.39527461e-02]],

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          [ 1.37512341e-01, -1.70524850e-01, -3.92835354e-03,
           -1.26837835e-01, -2.48225749e-01, -2.52311140e-01,
            1.93193018e-01,  3.92947458e-02, -1.85098946e-01]]]],
       dtype=float32)>,
 <tf.Variable 'Variable:0' shape=(9,) dtype=float32, numpy=
 array([ 0.20835146,  1.776194  , -0.9318092 ,  0.7346297 ,  0.11271965,
        -1.7630045 ,  1.1199703 , -0.6265498 ,  0.5340252 ], dtype=float32)>,
 <tf.Variable 'Variable:0' shape=(9216, 10) dtype=float32, numpy=
 array([[-0.02678335,  0.0027101 , -0.00452382, ..., -0.00343052,
         -0.00512886, -0.01311511],
        [-0.00632157, -0.01650657, -0.00103352, ..., -0.00153817,
         -0.01987005,  0.00564548],
        [ 0.02122953, -0.00029352, -0.02545957, ...,  0.02639172,
          0.00221391, -0.00986239],
        ...,
        [-0.01464436, -0.02326785,  0.01029822, ..., -0.02495557,
         -0.00308805, -0.00309393],
        [-0.00019059, -0.02311676,  0.0104869 , ..., -0.01642016,
          0.01026233,  0.00478034],
        [-0.01648459,  0.01684218,  0.00822433, ..., -0.01297023,
         -0.0005013 ,  0.0079396 ]], dtype=float32)>,
 <tf.Variable 'Variable:0' shape=(10,) dtype=float32, numpy=
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        -0.1812138 , -1.1118903 , -0.45288122, -2.5208182 , -0.310304  ],
       dtype=float32)>]
```

Part V: Train a *GREAT* model on CIFAR-10!

In this section you can experiment with whatever ConvNet architecture you'd like on CIFAR-10.

You should experiment with architectures, hyperparameters, loss functions, regularization, or anything else you can think of to train a model that achieves **at least 70%** accuracy on the **validation** set within 10 epochs. You can use the built-in train function, the `train_part34` function from above, or implement your own training loop.

Describe what you did at the end of the notebook.

Some things you can try:

- **Filter size**: Above we used 5x5 and 3x3; is this optimal?
- **Number of filters**: Above we used 16 and 32 filters. Would more or fewer do better?
- **Pooling**: We didn't use any pooling above. Would this improve the model?
- **Normalization**: Would your model be improved with batch normalization, layer normalization, group normalization, or some other normalization strategy?
- **Network architecture**: The ConvNet above has only three layers of trainable parameters. Would a deeper model do better? Good architectures to try include:
  - [conv-relu-pool]xN -> [affine]xM -> [softmax or SVM]
  - [conv-relu-conv-relu-pool]xN -> [affine]xM -> [softmax or SVM]
  - [batchnorm-relu-conv]xN -> [affine]xM -> [softmax or SVM]
- **Global average pooling**: Instead of flattening after the final convolutional layer, would global average pooling do better? This strategy is used for example in Google's Inception network and in Residual Networks.
- **Regularization**: Would some kind of regularization improve performance? Maybe weight decay or dropout?

NOTE: Batch Normalization / Dropout

If you are using Batch Normalization and Dropout, remember to pass `is_training=True` if you use the `train_part34()` function. BatchNorm and Dropout layers have different behaviors at training and inference time. `training` is a specific keyword argument reserved for this purpose in any `tf.keras.Model`'s `call()` function. Read more about this here :
https://www.tensorflow.org/versions/r2.0/api_docs/python/tf/keras/layers/BatchNormalization#methods
https://www.tensorflow.org/versions/r2.0/api_docs/python/tf/keras/layers/Dropout#methods

Tips for training

For each network architecture that you try, you should tune the learning rate and other hyperparameters. When doing this there are a couple important things to keep in mind:

- If the parameters are working well, you should see improvement within a few hundred iterations
- Remember the coarse-to-fine approach for hyperparameter tuning: start by testing a large range of hyperparameters for just a few training iterations to find the combinations of parameters that are working at all.
- Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs.
- You should use the validation set for hyperparameter search, and save your test set for evaluating your architecture on the best parameters as selected by the validation set.

Going above and beyond

If you are feeling adventurous there are many other features you can implement to try and improve your performance. You are **not required** to implement any of these, but don't miss the fun if you have time!

- Alternative optimizers: you can try Adam, Adagrad, RMSprop, etc.
- Alternative activation functions such as leaky ReLU, parametric ReLU, ELU, or MaxOut.
- Model ensembles
- Data augmentation
- New Architectures
  - ResNets where the input from the previous layer is added to the output.
  - DenseNets where inputs into previous layers are concatenated together.
  - This blog has an in-depth overview

Have fun and happy training!

In [21]:

```python
def train_part34(model_init_fn, optimizer_init_fn, num_epochs=1, is_training=False):
    ############################################################################
    # TODO: Train a model on CIFAR-10.                                        #
    ############################################################################
    # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****

    loss_fn = tf.keras.losses.SparseCategoricalCrossentropy()

    model = model_init_fn()
    optimizer = optimizer_init_fn()

    train_loss = tf.keras.metrics.Mean(name='train_loss')
    train_accuracy = tf.keras.metrics.SparseCategoricalAccuracy(name='train_accuracy')

    val_loss = tf.keras.metrics.Mean(name='val_loss')
    val_accuracy = tf.keras.metrics.SparseCategoricalAccuracy(name='val_accuracy')

    t = 0
    for e in range(num_epochs):

        train_loss.reset_states()
        train_accuracy.reset_states()

        for x_np, y_np in train_dset:
            with tf.GradientTape() as tape:

                # Use the model function to build the forward pass.
                scores = model(x_np, training=is_training)
                loss = loss_fn(y_np, scores)

            gradients = tape.gradient(loss, model.trainable_variables)
```