k-Nearest Neighbor (kNN) exercise Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. The kNN classifier consists of two stages: During training, the classifier takes the training data and simply remembers it During testing, kNN classifies every test image by comparing to all training images and transfering the labels of the k most similar training examples The value of k is cross-validated In this exercise you will implement these steps and understand the basic Image Classification pipeline, cross-validation, and gain proficiency in writing efficient, vectorized code. Acknowledgement: This exercise is adapted from Stanford CS231n. # Run some setup code for this notebook. In [52]: from __future__ import print function import random import numpy as np from data utils import load CIFAR10 import matplotlib.pyplot as plt # rather than in a new window. %matplotlib inline plt.rcParams['image.interpolation'] = 'nearest' plt.rcParams['image.cmap'] = 'gray' %load_ext autoreload %autoreload 2 The autoreload extension is already loaded. To reload it, use: %reload ext autoreload In [53]: def rel_error(out, correct out): cifar10 dir = 'datasets/cifar-10-batches-py' X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir) print('Training data shape: ', X train.shape) print('Training labels shape: ', y train.shape) print('Test data shape: ', X test.shape) print('Test labels shape: ', y_test.shape) Training data shape: (50000, 32, 32, 3) Training labels shape: (50000,) Test data shape: (10000, 32, 32, 3)

for i, idx in enumerate(idxs):

plt.title(cls)

bird

plt.axis('off') **if** i == 0:

plt.show()

num training = 5000

num test = 500

th train example.

In [59]:

In [61]:

mask = range(num training)

X_train = X_train[mask] y_train = y_train[mask]

mask = range(num test) X_test = X_test[mask] y_test = y_test[mask]

In [57]: # Reshape the image data into rows

(5000, 3072) (500, 3072)

print(X train.shape, X test.shape)

In [58]: **from** classifiers **import** KNearestNeighbor

classifier = KNearestNeighbor() classifier.train(X train, y train)

compute distances two loops.

its distances to training examples plt.imshow(dists, interpolation='none')

1000

Test your implementation:

print(dists.shape)

(500, 5000)

plt.show()

Create a kNN classifier instance.

plane

plt_idx = i * num_classes + y + 1

plt.imshow(X train[idx].astype('uint8'))

plt.subplot(samples per class, num classes, plt idx)

deer

In [56]: # Subsample the data for more efficient code execution in this exercise

X train = np.reshape(X train, (X train.shape[0], -1)) X test = np.reshape(X test, (X test.shape[0], -1))

Remember that training a kNN classifier is a noop:

Open classifiers/k nearest neighbor.py and implement

dists = classifier.compute distances two loops(X test)

In [60]: # We can visualize the distance matrix: each row is a single test example and

2000

Now implement the function predict labels and run the code below:

Compute and print the fraction of correctly predicted examples

with the default color scheme black indicates low distances while white indicates high distances.)

bright column represents a training example which has a large distance compared to all the test examples.

print('Got %d / %d correct => accuracy: %f' % (num correct, num test, accuracy))

You should expect to see approximately 27% accuracy. Now lets try out a larger k, say k = 5:

print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))

the Classifier simply remembers the data and does no further processing

1. First we must compute the distances between all test examples and all train examples.

We would now like to classify the test data with the kNN classifier. Recall that we can break down this process into two steps:

Lets begin with computing the distance matrix between all training and test examples. For example, if there are Ntr training examples and **Nte** test examples, this stage should result in a **Nte x Ntr** matrix where each element (i,j) is the distance between the i-th test and j-

First, open classifiers/k_nearest_neighbor.py and implement the function compute_distances_two_loops that uses a (very

2. Given these distances, for each test example we find the k nearest examples and have them vote for the label

inefficient) double loop over all pairs of (test, train) examples and computes the distance matrix one element at a time.

3000

Inline Question #1: Notice the structured patterns in the distance matrix, where some rows or columns are visible brighter. (Note that

Your Answer: Test images which have a large distance between themselves and most training images cause distinctly bright rows. Each

To ensure that our vectorized implementation is correct, we make sure that it agrees with the naive implementation. There are many ways

 $\|A\|_F = \sqrt{\sum_{i=1}^m \sum_{j=1}^n A_{ij}^2}$

• Frobenius norm of $m \times n$ matrix A is defined as the square root of the sum of the absolute squares of its elements,:

Hint: It is fine to use 2-nested for-loop. However, you can implement this

NOTE: numpy provides built-in function for Frobenius Norm, in this exercise,

END OF YOUR CODE

4000

dog

frog

horse

ship

truck

This is a bit of magic to make matplotlib figures appear inline in the notebook plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots # Some more magic so that the notebook will reload external python modules; # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython return np.sum(abs(out - correct out) / (abs(out) + abs(correct out))) # As a sanity check, we print out the size of the training and test data.

Test labels shape: (10000,)

In [54]: # Load the raw CIFAR-10 data. In [55]: # Visualize some examples from the dataset. # We show a few examples of training images from each class.

classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck'] num classes = len(classes)

samples per class = 7for y, cls in enumerate(classes): idxs = np.flatnonzero(y train == y) idxs = np.random.choice(idxs, samples per class, replace=False)

What in the data is the cause behind the distinctly bright rows? What causes the columns?

We use k = 1 (which is Nearest Neighbor).

num_correct = np.sum(y_test_pred == y_test) accuracy = float(num_correct) / num_test

Got 137 / 500 correct => accuracy: 0.274000

In [62]: y_test_pred = classifier.predict_labels(dists, k=5) num_correct = np.sum(y_test_pred == y_test) accuracy = float(num_correct) / num_test

Got 139 / 500 correct => accuracy: 0.278000

Frobenius Norm

In [63]: def Frobenius norm(A):

TODO:

Fnorm = None

return Fnorm

A = np.random.rand(3,2)

The difference: 0.0

if difference < 0.001:</pre>

Difference was: 0.000000

print('dists two: ', dists two)

4203.28086142 4354.20256764]

4694.09767687 7768.33347636]

4464.99921613 6353.57190878]

4537.30613911 5920.94156364]

3182.3673578 4448.65305458]

4128.24744898 8041.05223214]]

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4537.30613911 5920.94156364]

3182.3673578 4448.65305458]

4128.24744898 8041.05223214]]

Good! The distance matrices are the same

In [67]: # Let's compare how fast the implementations are

Two loop version took 57.822969 seconds One loop version took 85.534709 seconds No loop version took 0.576198 seconds

Difference was: 0.000000

import time

f(*args)

tic = time.time()

toc = time.time() return toc - tic

def time function(f, *args):

and run the code

print('dists: ', dists)

if difference < 0.001:</pre>

code below:

else:

else:

You should expect to see a slightly better performance than with k = 1.

to decide whether two matrices are similar; one of the simplest is **the Frobenius norm**.

Implement a function to calculate Frobenius Norm of matrix A.

print('The difference: ', rel error(Frobenius norm(A), np.linalg.norm(A)))

with one loop. Implement the function compute distances one loop and run the

In [65]: # Now lets speed up distance matrix computation by using partial vectorization

In [66]: # Now implement the fully vectorized version inside compute distances no loops

check that the distance matrix agrees with the one we computed before:

dists two: [[3803.92350081 4210.59603857 5504.0544147 ... 4007.64756434

dists one = classifier.compute distances one loop(X test)

difference = np.linalg.norm(dists - dists one, ord='fro')

print('Good! The distance matrices are the same')

print('Uh-oh! The distance matrices are different')

dists two = classifier.compute distances no loops(X test)

difference = np.linalg.norm(dists - dists two, ord='fro')

print('Good! The distance matrices are the same')

print('Uh-oh! The distance matrices are different')

[6336.83367306 5270.28006846 4040.63608854 ... 4829.15334194

[5224.83913628 4250.64289255 3773.94581307 ... 3766.81549853

[5366.93534524 5062.8772452 6361.85774755 ... 5126.56824786

[3671.92919322 3858.60765044 4846.88157479 ... 3521.04515734

[6960.92443573 6083.71366848 6338.13442584 ... 6083.55504619

[6336.83367306 5270.28006846 4040.63608854 ... 4829.15334194

[5224.83913628 4250.64289255 3773.94581307 ... 3766.81549853

[5366.93534524 5062.8772452 6361.85774755 ... 5126.56824786

[3671.92919322 3858.60765044 4846.88157479 ... 3521.04515734

[6960.92443573 6083.71366848 6338.13442584 ... 6083.55504619

print('Two loop version took %f seconds' % two loop time)

print('One loop version took %f seconds' % one loop time)

print('No loop version took %f seconds' % no loop time)

Call a function f with args and return the time (in seconds) that it took to execute.

you should see significantly faster performance with the fully vectorized implementation

two loop time = time function(classifier.compute distances two loops, X test)

one loop time = time function(classifier.compute distances one loop, X test)

no loop time = time function(classifier.compute distances no loops, X test)

dists: [[3803.92350081 4210.59603857 5504.0544147 ... 4007.64756434

print('Difference was: %f' % (difference,))

Good! The distance matrices are the same

print('Difference was: %f' % (difference,))

function with matrix calculation, which is much faster.

you are required to implement this function.

Fnorm = np.sqrt(np.sum(np.square(A)))

In [64]: # Check the accuracy of your implementation

y test pred = classifier.predict labels(dists, k=1)