	Softmax exercise Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. In this exercise, you will: implement a fully-vectorized loss function for the Softmax classifier implement the fully-vectorized expression for its analytic gradient
In [26]:	 check your implementation with numerical gradient use a validation set to tune the learning rate and regularization strength optimize the loss function with SGD visualize the final learned weights Acknowledgement: This exercise is adapted from Stanford CS231n. import random import numpy as np from data_utils import load_CIFAR10 import matplotlib.pyplot as plt
In [27]:	
In [28]:	Load the CIFAR-10 dataset from disk and perform preprocessing to prepare it for the linear classifier. These are the same steps as we used for the Softmax, but condensed to a single function. """ # Load the raw CIFAR-10 data cifar10_dir = 'datasets/cifar-10-batches-py' X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir) # subsample the data mask = range(num_training, num_training + num_validation)
	<pre>X_val = X_train[mask] y_val = y_train[mask] mask = range(num_training) X_train = X_train[mask] y_train = y_train[mask] mask = range(num_test) X_test = X_test[mask] y_test = y_test[mask] # # We will also make a development set, which is a small subset of # the training set. mask = np.random.choice(num_training, num_dev, replace=False) X_dev = X_train[mask] y_dev = y_train[mask]</pre>
	<pre># Preprocessing: reshape the image data into rows X_train = np.reshape(X_train, (X_train.shape[0], -1)) X_val = np.reshape(X_val, (X_val.shape[0], -1)) X_test = np.reshape(X_test, (X_test.shape[0], -1)) X_dev = np.reshape(X_dev, (X_dev.shape[0], -1)) # Normalize the data: subtract the mean image mean_image = np.mean(X_train, axis = 0) X_train -= mean_image X_val -= mean_image X_test -= mean_image X_dev -= mean_image # add bias dimension and transform into columns</pre>
	<pre>X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))]) X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))]) X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))]) X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))]) return X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev # Invoke the above function to get our data. X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev = get_CIFAR10_data() print('Train data shape: ', X_train.shape) print('Train labels shape: ', y_train.shape) print('Validation data shape: ', X_val.shape) print('Validation labels shape: ', y_val.shape)</pre>
In [29]:	
	<pre>num_class = 10 y_train_oh = np.zeros((y_train.shape[0], 10)) y_train_oh[np.arange(y_train.shape[0]), y_train] = 1 y_val_oh = np.zeros((y_val.shape[0], 10)) y_val_oh[np.arange(y_val.shape[0]), y_val] = 1 y_test_oh = np.zeros((y_test.shape[0], 10)) y_test_oh[np.arange(y_test.shape[0]), y_test] = 1 y_dev_oh = np.zeros((y_dev.shape[0], 10)) y_dev_oh[np.arange(y_dev.shape[0]), y_dev] = 1</pre> Regression as classifier
	The most simple and straightforward approach to learn a classifier is to map the input data (raw image values) to class label (one-hot vector). The loss function is defined as following: $\mathcal{L} = \frac{1}{n} \ \mathbf{X}\mathbf{W} - \mathbf{y}\ _F^2 \qquad (1)$ Where: $ \mathbf{W} \in \mathbb{R}^{(d+1)\times C} \text{: Classifier weight} $ $ \mathbf{X} \in \mathbb{R}^{n\times (d+1)} \text{: Dataset} $ $ \mathbf{y} \in \mathbb{R}^{n\times C} \text{: Class label (one-hot vector)} $
	Optimization Given the loss function (1), the next problem is how to solve the weight W. We now discuss 2 approaches: Random search Closed-form solution Random search
In [30]:	<pre>for num in range(100): W = np.random.randn(3073, 10) * 0.0001 loss = np.linalg.norm(X_dev.dot(W) - y_dev_oh) if (loss < bestloss): bestloss = loss bestW = W print('in attempt %d the loss was %f, best %f' % (num, loss, bestloss)) in attempt 0 the loss was 36.637351, best 36.637351 in attempt 1 the loss was 32.924404, best 32.924404 in attempt 2 the loss was 33.806308, best 32.924404 in attempt 3 the loss was 32.562024, best 32.562024 in attempt 4 the loss was 34.541393, best 32.562024 in attempt 5 the loss was 38.085818, best 32.562024</pre>
	in attempt 6 the loss was 33.462505, best 32.562024 in attempt 7 the loss was 34.845458, best 32.562024 in attempt 8 the loss was 34.530255, best 32.562024 in attempt 9 the loss was 30.556467, best 30.556467 in attempt 10 the loss was 32.865647, best 30.556467 in attempt 11 the loss was 31.969817, best 30.556467 in attempt 12 the loss was 34.242383, best 30.556467 in attempt 13 the loss was 33.266100, best 30.556467 in attempt 14 the loss was 32.291301, best 30.556467 in attempt 15 the loss was 31.902112, best 30.556467 in attempt 16 the loss was 32.662677, best 30.556467 in attempt 17 the loss was 32.086070, best 30.556467 in attempt 18 the loss was 32.429612, best 30.556467 in attempt 19 the loss was 34.759837, best 30.556467 in attempt 19 the loss was 34.839806, best 30.556467
	in attempt 20 the loss was 34.839806, best 30.556467 in attempt 21 the loss was 33.814048, best 30.556467 in attempt 22 the loss was 31.959273, best 30.556467 in attempt 23 the loss was 34.050328, best 30.556467 in attempt 24 the loss was 33.007395, best 30.556467 in attempt 25 the loss was 31.268496, best 30.556467 in attempt 26 the loss was 32.748833, best 30.556467 in attempt 27 the loss was 33.876862, best 30.556467 in attempt 28 the loss was 33.987584, best 30.556467 in attempt 29 the loss was 34.709678, best 30.556467 in attempt 30 the loss was 34.033636, best 30.556467 in attempt 31 the loss was 32.155135, best 30.556467 in attempt 31 the loss was 32.289099, best 30.556467 in attempt 32 the loss was 33.856707, best 30.556467 in attempt 33 the loss was 33.856707, best 30.556467 in attempt 34 the loss was 34.027628, best 30.556467 in attempt 34 the loss was 34.027628, best 30.556467
	in attempt 35 the loss was 32.940843, best 30.556467 in attempt 36 the loss was 32.943750, best 30.556467 in attempt 37 the loss was 32.471462, best 30.556467 in attempt 38 the loss was 31.570291, best 30.556467 in attempt 39 the loss was 34.850495, best 30.556467 in attempt 40 the loss was 32.524384, best 30.556467 in attempt 41 the loss was 34.745756, best 30.556467 in attempt 42 the loss was 32.578902, best 30.556467 in attempt 43 the loss was 31.654832, best 30.556467 in attempt 44 the loss was 33.913211, best 30.556467 in attempt 45 the loss was 34.355702, best 30.556467 in attempt 46 the loss was 31.704243, best 30.556467 in attempt 47 the loss was 31.704243, best 30.556467 in attempt 47 the loss was 33.175149, best 30.556467 in attempt 48 the loss was 34.071437, best 30.556467 in attempt 48 the loss was 34.07
	in attempt 49 the loss was 34.997157, best 30.556467 in attempt 50 the loss was 35.274019, best 30.556467 in attempt 51 the loss was 33.183698, best 30.556467 in attempt 52 the loss was 33.342831, best 30.556467 in attempt 53 the loss was 33.385239, best 30.556467 in attempt 54 the loss was 34.570113, best 30.556467 in attempt 55 the loss was 33.290241, best 30.556467 in attempt 56 the loss was 35.698501, best 30.556467 in attempt 57 the loss was 32.386731, best 30.556467 in attempt 58 the loss was 32.386731, best 30.556467 in attempt 59 the loss was 33.883616, best 30.556467 in attempt 59 the loss was 34.300839, best 30.556467 in attempt 60 the loss was 33.362207, best 30.556467 in attempt 61 the loss was 31.564005, best 30.556467 in attempt 62 the loss was 31.564005, best 30.556467 in attempt 63 the loss was 31.564005, best 30.556467 in attempt 63 the loss was 33.877760, best 30.556467
	in attempt 64 the loss was 33.996048, best 30.556467 in attempt 65 the loss was 30.040423, best 30.040423 in attempt 66 the loss was 35.458894, best 30.040423 in attempt 67 the loss was 34.864141, best 30.040423 in attempt 68 the loss was 33.210894, best 30.040423 in attempt 69 the loss was 34.080812, best 30.040423 in attempt 70 the loss was 32.589782, best 30.040423 in attempt 71 the loss was 30.780545, best 30.040423 in attempt 72 the loss was 32.135493, best 30.040423 in attempt 73 the loss was 33.900922, best 30.040423 in attempt 74 the loss was 31.544491, best 30.040423 in attempt 75 the loss was 31.737214, best 30.040423 in attempt 76 the loss was 31.737214, best 30.040423 in attempt 77 the loss was 31.410754, best 30.040423 in attempt 77 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423 in attempt 78 the loss was 33.140367, best 30.040423
	in attempt 79 the loss was 31.773960, best 30.040423 in attempt 80 the loss was 35.066745, best 30.040423 in attempt 81 the loss was 33.984874, best 30.040423 in attempt 82 the loss was 32.162808, best 30.040423 in attempt 83 the loss was 31.921446, best 30.040423 in attempt 84 the loss was 35.018599, best 30.040423 in attempt 85 the loss was 36.462637, best 30.040423 in attempt 86 the loss was 32.381492, best 30.040423 in attempt 87 the loss was 33.151785, best 30.040423 in attempt 88 the loss was 34.853117, best 30.040423 in attempt 89 the loss was 33.642947, best 30.040423 in attempt 90 the loss was 33.865483, best 30.040423 in attempt 91 the loss was 31.825663, best 30.040423 in attempt 92 the loss was 34.795921, best 30.040423
In [31]:	in attempt 93 the loss was 33.789278, best 30.040423 in attempt 94 the loss was 31.951754, best 30.040423 in attempt 95 the loss was 32.916194, best 30.040423 in attempt 96 the loss was 33.177665, best 30.040423 in attempt 97 the loss was 33.900388, best 30.040423 in attempt 98 the loss was 33.620565, best 30.040423 in attempt 99 the loss was 34.202109, best 30.040423 in attempt 99 the loss was 34.202109, best 30.040423 # How bestW perform: print('Accuracy on train set: ', np.sum(np.argmin(np.abs(1 - X_dev.dot(W)), axis=1) == y_dev).astype(np.float32) print('Accuracy on test set: ', np.sum(np.argmin(np.abs(1 - X_test.dot(W)), axis=1) == y_test).astype(np.float32) Accuracy on train set: 10.0 Accuracy on test set: 9.5
	You can clearly see that the performance is very low, almost at the random level.
In [32]: In [33]:	######################################
	Train set accuracy: 51.163265306122454 Test set accuracy: $36.1999999999999999999999999999999999999$
In [34]:	<pre>lambdas = [0.01, 0.1, 1, 10, 100, 1000, 10000, 100000] train_acc = np.zeros((len(lambdas))) test_acc = np.zeros((len(lambdas))) for i in range(len(lambdas)):</pre>
In [35]:	<pre># Implement the closed-form solution of the weight W with regularization. # ###################################</pre>
	plt.grid(True) plt.show() Taining accuracy Testing accuracy
	42 40 38
	Question: Try to explain why the performances on the training and test set have such behaviors as we change the value of λ . Your answer: As λ increases, a simple model becomes more important than a model that fits the training set very well. Thus, at small values of λ , the training accuracy will be very high and the testing accuracy will be very low as the model will closely fit the training data but not the test data. As λ increases, training accuracy decreases as the model will not fit the training set as well before. Testing accuracy will increase as the model will be more general, but after a certain point, $\lambda = 1000$ in the above graph, testing accuracy drops as the model becomes too general.
	Softmax Classifier $P(y=j\mid x) = \frac{e^{-xw_j}}{\sum\limits_{c=1}^C e^{-xw_c}}$ Your code for this section will all be written inside classifiers/softmax.py.
In [36]:	# First implement the naive softmax loss function with nested loops. # Open the file classifiers/softmax.py and implement the # softmax_loss_naive function. from classifiers.softmax import softmax_loss_naive import time # Generate a random softmax weight matrix and use it to compute the loss. W = np.random.randn(3073, 10) * 0.0001 loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0) # As a rough sanity check, our loss should be something close to -log(0.1). print('loss: %f' % loss) print('sanity check: %f' % (-np.log(0.1)))
	loss: 2.380864 sanity check: 2.302585 Question: Why do we expect our loss to be close to -log(0.1)? Explain briefly.** Your answer: This is as this dataset only has 10 classes, thus the probability of getting the right label for each test example is 0.1. Hence, we expect the loss to be close to -log(0.1) Optimization
In [37]:	Random search bestloss = float('inf') for num in range(100): W = np.random.randn(3073, 10) * 0.0001 loss, _ = softmax_loss_naive(W, X_dev, y_dev, 0.0) if (loss < bestloss): bestloss = loss bestW = W print('in attempt %d the loss was %f, best %f' % (num, loss, bestloss)) in attempt 0 the loss was 2.346017, best 2.346017 in attempt 1 the loss was 2.323649, best 2.323649 in attempt 2 the loss was 2.346411, best 2.323649
	in attempt 3 the loss was 2.357735, best 2.323649 in attempt 4 the loss was 2.331117, best 2.323649 in attempt 5 the loss was 2.322321, best 2.322321 in attempt 6 the loss was 2.330263, best 2.322321 in attempt 7 the loss was 2.363373, best 2.322321 in attempt 8 the loss was 2.425869, best 2.322321 in attempt 9 the loss was 2.438606, best 2.322321 in attempt 10 the loss was 2.360946, best 2.322321 in attempt 11 the loss was 2.437143, best 2.322321 in attempt 12 the loss was 2.393287, best 2.322321 in attempt 13 the loss was 2.343271, best 2.322321 in attempt 14 the loss was 2.389024, best 2.322321 in attempt 15 the loss was 2.389024, best 2.322321 in attempt 16 the loss was 2.392865, best 2.322321 in attempt 16 the loss was 2.392865, best 2.322321
	in attempt 17 the loss was 2.357944, best 2.322321 in attempt 18 the loss was 2.379943, best 2.322321 in attempt 19 the loss was 2.357643, best 2.322321 in attempt 20 the loss was 2.316299, best 2.316299 in attempt 21 the loss was 2.334672, best 2.316299 in attempt 22 the loss was 2.404035, best 2.316299 in attempt 23 the loss was 2.304163, best 2.304163 in attempt 24 the loss was 2.386964, best 2.304163 in attempt 25 the loss was 2.339042, best 2.304163 in attempt 26 the loss was 2.415900, best 2.304163 in attempt 27 the loss was 2.427842, best 2.304163 in attempt 28 the loss was 2.375829, best 2.304163 in attempt 30 the loss was 2.375829, best 2.304163 in attempt 30 the loss was 2.346430, best 2.304163 in attempt 31 the loss was 2.321405, best 2.304163
	in attempt 32 the loss was 2.372458, best 2.304163 in attempt 33 the loss was 2.380628, best 2.304163 in attempt 34 the loss was 2.360905, best 2.304163 in attempt 35 the loss was 2.397161, best 2.304163 in attempt 36 the loss was 2.399699, best 2.304163 in attempt 37 the loss was 2.349561, best 2.304163 in attempt 38 the loss was 2.435108, best 2.304163 in attempt 39 the loss was 2.382840, best 2.304163 in attempt 40 the loss was 2.311527, best 2.304163 in attempt 41 the loss was 2.297903, best 2.297903 in attempt 42 the loss was 2.315568, best 2.297903 in attempt 43 the loss was 2.370139, best 2.297903 in attempt 44 the loss was 2.418890, best 2.297903 in attempt 45 the loss was 2.350125, best 2.297903
	in attempt 46 the loss was 2.314503, best 2.297903 in attempt 47 the loss was 2.388527, best 2.297903 in attempt 48 the loss was 2.323985, best 2.297903 in attempt 49 the loss was 2.348714, best 2.297903 in attempt 50 the loss was 2.352724, best 2.297903 in attempt 51 the loss was 2.353193, best 2.297903 in attempt 52 the loss was 2.3471915, best 2.297903 in attempt 53 the loss was 2.345294, best 2.297903 in attempt 54 the loss was 2.368835, best 2.297903 in attempt 55 the loss was 2.343611, best 2.297903 in attempt 56 the loss was 2.343611, best 2.297903 in attempt 57 the loss was 2.340418, best 2.297903 in attempt 58 the loss was 2.340418, best 2.297903 in attempt 59 the loss was 2.306470, best 2.297903 in attempt 59 the loss was 2.306470, best 2.297903 in attempt 50 the loss was 2.324161, best 2.297903 in attempt 60 the loss was 2.324161, best 2.297903
	in attempt 61 the loss was 2.278780, best 2.278780 in attempt 62 the loss was 2.439210, best 2.278780 in attempt 63 the loss was 2.361272, best 2.278780 in attempt 64 the loss was 2.383369, best 2.278780 in attempt 65 the loss was 2.269405, best 2.269405 in attempt 66 the loss was 2.411336, best 2.269405 in attempt 67 the loss was 2.396853, best 2.269405 in attempt 68 the loss was 2.380937, best 2.269405 in attempt 69 the loss was 2.380937, best 2.269405 in attempt 70 the loss was 2.349285, best 2.269405 in attempt 71 the loss was 2.302930, best 2.269405 in attempt 72 the loss was 2.356040, best 2.269405 in attempt 73 the loss was 2.373648, best 2.269405 in attempt 74 the loss was 2.379958, best 2.269405 in attempt 75 the loss was 2.307778, best 2.269405 in attempt 74 the loss was 2.307778, best 2.269405 in attempt 75 the loss was 2.341909, best 2.269405
	in attempt 76 the loss was 2.311944, best 2.269405 in attempt 77 the loss was 2.362005, best 2.269405 in attempt 78 the loss was 2.406865, best 2.269405 in attempt 79 the loss was 2.369891, best 2.269405 in attempt 80 the loss was 2.339579, best 2.269405 in attempt 81 the loss was 2.294596, best 2.269405 in attempt 82 the loss was 2.353653, best 2.269405 in attempt 83 the loss was 2.371741, best 2.269405 in attempt 84 the loss was 2.335790, best 2.269405 in attempt 85 the loss was 2.323281, best 2.269405 in attempt 86 the loss was 2.377277, best 2.269405 in attempt 87 the loss was 2.345165, best 2.269405 in attempt 88 the loss was 2.340496, best 2.269405 in attempt 88 the loss was 2.340496, best 2.269405 in attempt 89 the loss was 2.411736, best 2.269405
In [38]:	<pre>in attempt 90 the loss was 2.276195, best 2.269405 in attempt 91 the loss was 2.335273, best 2.269405 in attempt 92 the loss was 2.344019, best 2.269405 in attempt 93 the loss was 2.336443, best 2.269405 in attempt 94 the loss was 2.363609, best 2.269405 in attempt 95 the loss was 2.343149, best 2.269405 in attempt 96 the loss was 2.321319, best 2.269405 in attempt 97 the loss was 2.333862, best 2.269405 in attempt 98 the loss was 2.401409, best 2.269405 in attempt 99 the loss was 2.375979, best 2.269405 # How bestW perform on trainset scores = X_train.dot(bestW) y_pred = np.argmax(scores, axis=1) print('Accuracy on train set %f' % np.mean(y pred == y_train))</pre>
	# evaluate performance of test set scores = X_test.dot(bestW) y_pred = np.argmax(scores, axis=1) print('Accuracy on test set %f' % np.mean(y_pred == y_test)) Accuracy on train set 0.136449 Accuracy on test set 0.143000 Compare the performance when using random search with regression classifier and softmax classifier. You can see how much useful the softmax classifier is. Stochastic Gradient descent
In [39]:	Even though it is possible to achieve closed-form solution with softmax classifier, it would be more complicated. In fact, we could achieve very good results with gradient descent approach. Additionally, in case of very large dataset, it is impossible to load the whole dataset into the memory. Gradient descent can help to optimize the loss function in batch. $\mathbf{W}^{t+1} = \mathbf{W}^t - \alpha \frac{\partial \mathcal{L}(\mathbf{x}; \mathbf{W}^t)}{\partial \mathbf{W}^t}$ Where α is the learning rate, \mathcal{L} is a loss function, and \mathbf{x} is a batch of training dataset.
	loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0) # Use numeric gradient checking as a debugging tool. # The numeric gradient should be close to the analytic gradient. from gradient_check import grad_check_sparse f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 0.0)[0] grad_numerical = grad_check_sparse(f, W, grad, 10) # gradient check with regularization loss, grad = softmax_loss_naive(W, X_dev, y_dev, 1e2) f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 1e2)[0] grad_numerical = grad_check_sparse(f, W, grad, 10) numerical: 1.217947 analytic: 1.215857, relative error: 8.588240e-04 numerical: 0.132489 analytic: 0.152055, relative error: 6.876277e-02
	numerical: 0.795245 analytic: 0.759320, relative error: 2.310899e-02 numerical: 0.555071 analytic: 0.444335, relative error: 1.108019e-01 numerical: 0.141194 analytic: 0.133569, relative error: 2.775068e-02 numerical: -2.168304 analytic: -1.923995, relative error: 5.969954e-02 numerical: 1.650670 analytic: 1.277481, relative error: 1.274487e-01 numerical: 3.004256 analytic: 2.632132, relative error: 6.602164e-02 numerical: 4.017216 analytic: 3.289637, relative error: 9.957483e-02 numerical: -2.426998 analytic: -2.271771, relative error: 3.303559e-02 numerical: 0.621639 analytic: 0.640145, relative error: 1.466726e-02 numerical: 0.400419 analytic: 0.243615, relative error: 2.434716e-01 numerical: 2.203817 analytic: 1.785335, relative error: 1.049049e-01 numerical: 0.798253 analytic: 0.541017, relative error: 1.920719e-01 numerical: 2.089670 analytic: 1.897814, relative error: 4.811454e-02 numerical: 0.651894 analytic: 0.576449, relative error: 6.142058e-02
In [40]:	<pre># implement a vectorized version in softmax_loss_vectorized. # The two versions should compute the same results, but the vectorized version should be # much faster. tic = time.time() loss_naive, grad_naive = softmax_loss_naive(W, X_dev, y_dev, 0.00001) toc = time.time() print('naive loss: %e computed in %fs' % (loss_naive, toc - tic))</pre>
	<pre>from classifiers.softmax import softmax_loss_vectorized tic = time.time() loss_vectorized, grad_vectorized = softmax_loss_vectorized(W, X_dev, y_dev, 0.00001) toc = time.time() print('vectorized loss: %e computed in %fs' % (loss_vectorized, toc - tic)) # We use the Frobenius norm to compare the two versions # of the gradient. grad_difference = np.linalg.norm(grad_naive - grad_vectorized, ord='fro') print('Loss difference: %f' % np.abs(loss_naive - loss_vectorized)) print('Gradient difference: %f' % grad_difference) naive loss: 2.375979e+00 computed in 0.262602s vectorized loss: 2.375979e+00 computed in 0.017003s Loss difference: 0.000000 Gradient difference: 39.164211</pre>
In [41]:	<pre>from classifiers.linear_classifier import * classifier = Softmax() tic = time.time() loss_hist = classifier.train(X_train, y_train, learning_rate=1e-7, reg=5e4,</pre>
In [42]:	<pre>iteration 400 / 1500: loss 15.845203 iteration 500 / 1500: loss 7.149301 iteration 600 / 1500: loss 3.958358 iteration 700 / 1500: loss 2.725728 iteration 800 / 1500: loss 2.342481 iteration 900 / 1500: loss 2.118801 iteration 1000 / 1500: loss 2.136342 iteration 1100 / 1500: loss 2.122971 iteration 1200 / 1500: loss 2.111508 iteration 1300 / 1500: loss 2.085928 iteration 1400 / 1500: loss 2.098787 That took 18.467031s</pre>
In [43]:	<pre># training and validation set y_train_pred = classifier.predict(X_train) print('training accuracy: %f' % (np.mean(y_train == y_train_pred),)) y_val_pred = classifier.predict(X_val) print('validation accuracy: %f' % (np.mean(y_val == y_val_pred),)) training accuracy: 0.327184 validation accuracy: 0.342000</pre>
	800 - 700 - 600 - 500 -
	300 - 200 - 100 - 100 - 1200 1400 1
In [44]:	