Acknowledgement: This exercise is adapted from Stanford CS231n. # As usual, a bit of setup from future import print function import time import numpy as np import matplotlib.pyplot as plt from libs.classifiers.fc net import * from libs.data utils import get CIFAR10 data from libs.gradient check import eval numerical gradient, eval numerical gradient array from libs.solver import Solver %matplotlib inline plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots plt.rcParams['image.interpolation'] = 'nearest' plt.rcParams['image.cmap'] = 'gray' # for auto-reloading external modules # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython %load ext autoreload %autoreload 2 def rel error(x, y): """ returns relative error """ return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y)))) The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload In [16]: # Load the (preprocessed) CIFAR10 data. data = get_CIFAR10_data() for k, v in list(data.items()): print(('%s: ' % k, v.shape)) ('X train: ', (49000, 3, 32, 32)) ('y train: ', (49000,)) ('X_val: ', (1000, 3, 32, 32)) ('y_val: ', (1000,)) ('X_test: ', (1000, 3, 32, 32)) ('y test: ', (1000,)) Affine layer: foward Open the file libs/layers.py and implement the affine_forward function. Once you are done you can test your implementation by running the following: # Test the affine forward function In [17]: num inputs = 2 input shape = (4, 5, 6)output_dim = 3 input_size = num_inputs * np.prod(input_shape) weight_size = output_dim * np.prod(input_shape) x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape) $w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input shape), output dim)$ b = np.linspace(-0.3, 0.1, num=output dim)out, _ = affine_forward(x, w, b) correct_out = np.array([[1.49834967, 1.70660132, 1.91485297], [3.25553199, 3.5141327, 3.77273342]]) # Compare your output with ours. The error should be around e-9 or less. print('Testing affine_forward function:') print('difference: ', rel_error(out, correct_out)) Testing affine_forward function: difference: 9.769849468192957e-10 Affine layer: backward Now implement the affine_backward function and test your implementation using numeric gradient checking. In [18]: # Test the affine backward function np.random.seed(231) x = np.random.randn(10, 2, 3)w = np.random.randn(6, 5)b = np.random.randn(5) dout = np.random.randn(10, 5) dx num = eval numerical gradient_array(lambda x: affine_forward(x, w, b)[0], x, dout) dw num = eval numerical gradient_array(lambda w: affine_forward(x, w, b)[0], w, dout) db num = eval numerical gradient array(lambda b: affine forward(x, w, b)[0], b, dout) , cache = affine forward(x, w, b) dx, dw, db = affine backward(dout, cache)# The error should be around e-10 or less print('Testing affine_backward function:') print('dx error: ', rel_error(dx_num, dx)) print('dw error: ', rel_error(dw_num, dw)) print('db error: ', rel_error(db_num, db)) Testing affine_backward function: dx error: 5.399100368651805e-11 dw error: 9.904211865398145e-11 db error: 2.4122867568119087e-11 **ReLU** activation: forward Implement the forward pass for the ReLU activation function in the relu_forward function and test your implementation using the following: In [19]: # Test the relu_forward function x = np.linspace(-0.5, 0.5, num=12).reshape(3, 4)out, = relu forward(x) 0., 0., 0., 0., 0., 0., 0.13 correct out = np.array([[0., [0., 0.04545455, 0.13636364,], [0.22727273, 0.31818182, 0.40909091, 0.5, # Compare your output with ours. The error should be on the order of e-8 print('Testing relu forward function:') print('difference: ', rel error(out, correct out)) Testing relu forward function: difference: 4.999999798022158e-08 **ReLU** activation: backward Now implement the backward pass for the ReLU activation function in the relu_backward function and test your implementation using numeric gradient checking: In [20]: | np.random.seed(231) x = np.random.randn(10, 10)dout = np.random.randn(*x.shape) dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout) , cache = relu_forward(x) dx = relu backward(dout, cache) # The error should be on the order of e-12 print('Testing relu backward function:') print('dx error: ', rel_error(dx_num, dx)) Testing relu backward function: dx error: 3.2756349136310288e-12 "Sandwich" layers There are some common patterns of layers that are frequently used in neural nets. For example, affine layers are frequently followed by a ReLU nonlinearity. To make these common patterns easy, we define several convenience layers in the file libs/layer_utils.py . For now take a look at the affine_relu_forward and affine_relu_backward functions, and run the following to numerically gradient check the backward pass: In [21]: from libs.layer_utils import affine_relu_forward, affine relu backward np.random.seed(231) x = np.random.randn(2, 3, 4)w = np.random.randn(12, 10)b = np.random.randn(10) dout = np.random.randn(2, 10) out, cache = affine_relu_forward(x, w, b) dx, dw, db = affine_relu_backward(dout, cache) dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b)[0], x, dout) dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, b)[0], w, dout) db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, b)[0], b, dout) # Relative error should be around e-10 or less print('Testing affine relu forward and affine relu backward:') print('dx error: ', rel_error(dx_num, dx)) print('dw error: ', rel_error(dw_num, dw)) print('db error: ', rel_error(db_num, db)) Testing affine relu forward and affine relu backward: dx error: 2.299579177309368e-11 dw error: 8.162011105764925e-11 db error: 7.826724021458994e-12 **Loss layers: Softmax** You implemented these loss functions in the last assignment, so we'll give them to you for free here. You should still make sure you understand how they work by looking at the implementations in libs/layers.py. You can make sure that the implementations are correct by running the following: In [22]: | np.random.seed(231) num classes, num inputs = 10, 50 x = 0.001 * np.random.randn(num inputs, num classes)y = np.random.randint(num classes, size=num inputs) dx num = eval numerical gradient(lambda x: softmax loss(x, y)[0], x, verbose=False)loss, dx = softmax loss(x, y)# Test softmax loss function. Loss should be close to 2.3 and dx error should be around e-8 print('\nTesting softmax loss:') print('loss: ', loss) print('dx error: ', rel error(dx num, dx)) Testing softmax loss: loss: 2.302545844500738 dx error: 9.384673161989355e-09 Two-layer network In the previous assignment you implemented a two-layer neural network in a single monolithic class. Now that you have implemented modular versions of the necessary layers, you will reimplement the two layer network using these modular implementations. Open the file libs/classifiers/fc_net.py and complete the implementation of the TwoLayerNet class. This class will serve as a model for the other networks you will implement in this assignment, so read through it to make sure you understand the API. You can run the cell below to test your implementation. In [23]: | np.random.seed(231) N, D, H, C = 3, 5, 50, 7X = np.random.randn(N, D)y = np.random.randint(C, size=N) std = 1e-3model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std) print('Testing initialization ... ') W1 std = abs(model.params['W1'].std() - std) b1 = model.params['b1'] W2 std = abs(model.params['W2'].std() - std) b2 = model.params['b2'] assert W1 std < std / 10, 'First layer weights do not seem right'</pre> assert np.all(b1 == 0), 'First layer biases do not seem right' assert W2_std < std / 10, 'Second layer weights do not seem right'</pre> assert np.all(b2 == 0), 'Second layer biases do not seem right' print('Testing test-time forward pass ... ') model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)model.params['b1'] = np.linspace(-0.1, 0.9, num=H) model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C) model.params['b2'] = np.linspace(-0.9, 0.1, num=C) X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).Tscores = model.loss(X) correct scores = np.asarray([[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.33206765, 16.09215096], [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.49994135, 16.18839143], [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.66781506, 16.2846319]]) scores diff = np.abs(scores - correct_scores).sum() assert scores diff < 1e-6, 'Problem with test-time forward pass'</pre> print('Testing training loss (no regularization)') y = np.asarray([0, 5, 1])loss, grads = model.loss(X, y) correct loss = 3.4702243556assert abs(loss - correct loss) < 1e-10, 'Problem with training-time loss'</pre> model.reg = 1.0loss, grads = model.loss(X, y) correct loss = 26.5948426952assert abs(loss - correct loss) < 1e-10, 'Problem with regularization loss'</pre> # Errors should be around e-7 or less for reg in [0.0, 0.7]: print('Running numeric gradient check with reg = ', reg) model.reg = reg loss, grads = model.loss(X, y) for name in sorted(grads): f = lambda : model.loss(X, y)[0]grad_num = eval_numerical_gradient(f, model.params[name], verbose=False) print('%s relative error: %.2e' % (name, rel_error(grad num, grads[name]))) Testing initialization ... Testing test-time forward pass ... Testing training loss (no regularization) Running numeric gradient check with reg = 0.0W1 relative error: 1.83e-08 W2 relative error: 3.12e-10 b1 relative error: 9.83e-09 b2 relative error: 4.33e-10 Running numeric gradient check with reg = 0.7W1 relative error: 2.53e-07 W2 relative error: 2.85e-08 b1 relative error: 1.56e-08 b2 relative error: 7.76e-10 Solver In the previous assignment, the logic for training models was coupled to the models themselves. Following a more modular design, for this assignment we have split the logic for training models into a separate class. Open the file libs/solver.py and read through it to familiarize yourself with the API. After doing so, use a Solver instance to train a TwoLayerNet that achieves at least 50% accuracy on the validation set. In [24]: # X_val: (1000, 3, 32, 32) # X_train: (49000, 3, 32, 32) # X_test: (1000, 3, 32, 32) # y_val: (1000,) # y_train: (49000,) # y_test: (1000,) # model = TwoLayerNet() # solver = None # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least # 50% accuracy on the validation set. # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) **** model = TwoLayerNet() solver = Solver(model, data, num_epochs=10, batch_size=100, update_rule='sgd', optim config={'learning rate':1e-3}, # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) **** END OF YOUR CODE (Iteration 1 / 4900) loss: 2.305171 (Epoch 0 / 10) train acc: 0.103000; val acc: 0.085000 (Iteration 201 / 4900) loss: 1.932779 (Iteration 401 / 4900) loss: 1.538737 (Epoch 1 / 10) train acc: 0.388000; val acc: 0.378000 (Iteration 601 / 4900) loss: 1.701701 (Iteration 801 / 4900) loss: 1.699713 (Epoch 2 / 10) train acc: 0.497000; val acc: 0.474000 (Iteration 1001 / 4900) loss: 1.424826 (Iteration 1201 / 4900) loss: 1.666793 (Iteration 1401 / 4900) loss: 1.211955 (Epoch 3 / 10) train acc: 0.497000; val acc: 0.473000 (Iteration 1601 / 4900) loss: 1.281926 (Iteration 1801 / 4900) loss: 1.357318 (Epoch 4 / 10) train acc: 0.522000; val acc: 0.485000 (Iteration 2001 / 4900) loss: 1.311724 (Iteration 2201 / 4900) loss: 1.228021 (Iteration 2401 / 4900) loss: 1.336943 (Epoch 5 / 10) train acc: 0.525000; val acc: 0.483000 (Iteration 2601 / 4900) loss: 1.404788 (Iteration 2801 / 4900) loss: 1.238467 (Epoch 6 / 10) train acc: 0.519000; val acc: 0.509000 (Iteration 3001 / 4900) loss: 1.216040 (Iteration 3201 / 4900) loss: 1.293010 (Iteration 3401 / 4900) loss: 1.426607 (Epoch 7 / 10) train acc: 0.554000; val acc: 0.515000 (Iteration 3601 / 4900) loss: 1.121254 (Iteration 3801 / 4900) loss: 1.124680 (Epoch 8 / 10) train acc: 0.571000; val acc: 0.494000 (Iteration 4001 / 4900) loss: 1.221882 (Iteration 4201 / 4900) loss: 1.237958 (Iteration 4401 / 4900) loss: 1.325068 (Epoch 9 / 10) train acc: 0.564000; val acc: 0.505000 (Iteration 4601 / 4900) loss: 1.339394 (Iteration 4801 / 4900) loss: 1.071422 (Epoch 10 / 10) train acc: 0.590000; val acc: 0.499000 In [25]: # Run this cell to visualize training loss and train / val accuracy plt.subplot(2, 1, 1) plt.title('Training loss') plt.plot(solver.loss history, 'o') plt.xlabel('Iteration') plt.subplot(2, 1, 2) plt.title('Accuracy') plt.plot(solver.train_acc_history, '-o', label='train') plt.plot(solver.val acc history, '-o', label='val') plt.plot([0.5] * len(solver.val_acc_history), 'k--') plt.xlabel('Epoch') plt.legend(loc='lower right') plt.gcf().set_size_inches(15, 12) plt.show() Training loss

1.6

1.4

1.2

1.0

0.8

0.5

0.4

0.2

0.1

Multilayer network

batch/layer normalization; we will add those features soon.

For gradient checking, you should expect to see errors around 1e-7 or less.

model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,

Most of the errors should be on the order of e-7 or smaller.

TODO: Use a three-layer Net to overfit 50 training examples by # tweaking just the learning rate and initialization scale.

weight scale=weight scale, dtype=np.float64)

'learning rate': learning rate,

print every=10, num epochs=20, batch size=25,

'X_train': data['X_train'][:num_train],
'y_train': data['y_train'][:num_train],

weight_scale = 2e-2 # Experiment with this!
learning rate = 3e-3 # Experiment with this!

update_rule='sgd',
optim config={

(Epoch 0 / 20) train acc: 0.180000; val_acc: 0.109000 (Epoch 1 / 20) train acc: 0.360000; val_acc: 0.137000 (Epoch 2 / 20) train acc: 0.600000; val_acc: 0.155000 (Epoch 3 / 20) train acc: 0.720000; val_acc: 0.170000 (Epoch 4 / 20) train acc: 0.800000; val_acc: 0.171000 (Epoch 5 / 20) train acc: 0.880000; val_acc: 0.182000

(Epoch 6 / 20) train acc: 0.880000; val_acc: 0.194000 (Epoch 7 / 20) train acc: 0.9000000; val_acc: 0.183000 (Epoch 8 / 20) train acc: 0.940000; val_acc: 0.203000 (Epoch 9 / 20) train acc: 0.980000; val_acc: 0.195000 (Epoch 10 / 20) train acc: 0.980000; val acc: 0.185000

(Epoch 11 / 20) train acc: 1.000000; val_acc: 0.201000 (Epoch 12 / 20) train acc: 1.000000; val_acc: 0.180000 (Epoch 13 / 20) train acc: 1.000000; val_acc: 0.181000 (Epoch 14 / 20) train acc: 1.000000; val_acc: 0.189000 (Epoch 15 / 20) train acc: 1.000000; val_acc: 0.187000

(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.195000 (Epoch 17 / 20) train acc: 1.000000; val_acc: 0.196000 (Epoch 18 / 20) train acc: 1.000000; val_acc: 0.199000 (Epoch 19 / 20) train acc: 1.000000; val_acc: 0.191000 (Epoch 20 / 20) train acc: 1.000000; val_acc: 0.189000

10

15

20 Iteration 30

Training loss history

model = FullyConnectedNet([100, 100],

solver = Solver(model, small data,

plt.plot(solver.loss_history, 'o')
plt.title('Training loss history')

(Iteration 1 / 40) loss: 3.604568

(Iteration 11 / 40) loss: 0.402117

(Iteration 21 / 40) loss: 0.245577

(Iteration 31 / 40) loss: 0.107372

Initial loss and gradient check

the initial losses seem reasonable?

X = np.random.randn(N, D)

for reg in [0, 3.14]:

N, D, H1, H2, C = 2, 15, 20, 30, 10

= np.random.randint(C, size=(N,))

loss, grads = model.loss(X, y)
print('Initial loss: ', loss)

for the check when reg = 0.0
for name in sorted(grads):

Running check with reg = 0

W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
b1 relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
Running check with reg = 3.14
Initial loss: 7.052114776533016
W1 relative error: 3.90e-09
W2 relative error: 6.87e-08
W3 relative error: 2.13e-08
b1 relative error: 1.48e-08
b2 relative error: 1.72e-09
b3 relative error: 1.57e-10

accuracy within 20 epochs.

'X_val': data['X_val'],
'y_val': data['y_val'],

num_train = 50
small data = {

solver.train()

plt.show()

3.5

3.0

2.5

2.0

1.5

1.0

0.5

0.0

Training loss

plt.xlabel('Iteration')
plt.ylabel('Training loss')

Initial loss: 2.3004790897684924

f = lambda : model.loss(X, y)[0]

print('Running check with reg = ', reg)

np.random.seed(231)

1000

Next you will implement a fully-connected network with an arbitrary number of hidden layers.

Read through the FullyConnectedNet class in the file libs/classifiers/fc_net.py.

2000

Iteration Accuracy

Epoch

Implement the initialization, the forward pass, and the backward pass. For the moment don't worry about implementing dropout or

As a sanity check, run the following to check the initial loss and to gradient check the network both with and without regularization. Do

reg=reg, weight scale=5e-2, dtype=np.float64)

As another sanity check, make sure you can overfit a small dataset of 50 images. First we will try a three-layer network with 100 units in each hidden layer. In the following cell, tweak the **learning rate** and **weight initialization scale** to overfit and achieve 100% training

the however to see an error for W2 on the order of e-5 $^{\circ}$

grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))

3000

4000

5000

train

val

Fully-Connected Neural Nets

def layer_forward(x, w):

out = # the output

return out, cache

weights, like this:

Do some computations ...

def layer_backward(dout, cache):

Unpack cache values
x, w, z, out = cache

return dx, dw

and compute derivative with respect to inputs.

Use values in cache to compute derivatives
dx = # Derivative of loss with respect to x
dw = # Derivative of loss with respect to w

""" Receive inputs x and weights w """

z = # ... some intermediate value
Do some more computations ...

output and a cache object storing data needed for the backward pass, like this:

cache = (x, w, z, out) # Values we need to compute gradients

Receive dout (derivative of loss with respect to outputs) and cache,

In the previous homework you implemented a fully-connected two-layer neural network on CIFAR-10. The implementation was simple but not very modular since the loss and gradient were computed in a single monolithic function. This is manageable for a simple two-layer network, but would become impractical as we move to bigger models. Ideally we want to build networks using a more modular design so that we can implement different layer types in isolation and then snap them together into models with different architectures.

In this exercise we will implement fully-connected networks using a more modular approach. For each layer we will implement a

forward and a backward function. The forward function will receive inputs, weights, and other parameters and will return both an

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and

After implementing a bunch of layers this way, we will be able to easily combine them to build classifiers with different architectures.

introduce Dropout as a regularizer and Batch/Layer Normalization as a tool to more efficiently optimize deep networks.

In addition to implementing fully-connected networks of arbitrary depth, we will also explore different update rules for optimization, and