## Note

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$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}, \, \hat{\beta}_1 = \frac{Sxy}{Sxx}.$$

Residual Standard Error  $S = \sqrt{\frac{1}{n-2} \sum_{i=1}^{n} \hat{e_i}^2} = \sqrt{\frac{1}{n-2} \sum_{i=1}^{n} [y_i - \hat{y_i}]} = \sqrt{\frac{1}{n-2} \sum_{i=1}^{n} [y_i - (\hat{\beta_0} + \hat{\beta_1} * x_i)]}$ .

$$se(\hat{\beta}_1) = \frac{S}{\sqrt{Sxx}}, se(\hat{\beta}_0) = S\sqrt{(\frac{1}{n} + \frac{\bar{x}^2}{Sxx})}.$$

- 1. Confidence Interval for  $\beta_1$ :  $\hat{\beta_1} \pm t_{\alpha/2, n-2} * se(\hat{\beta_1})$ .
- 2. Confidence Interval for  $\beta_0$ :  $\hat{\beta_0} \pm t_{\alpha/2, n-2} * se(\hat{\beta_0})$ .
- 1. Confidence Interval for mean Y (regression line) at  $X = x^*$ :  $\hat{y}^* \pm t_{\alpha/2, n-2} * S\sqrt{(\frac{1}{n} + \frac{(x^* \bar{x})^2}{Sxx})}$
- 2. Prediction Interval for Single Y at  $X=x^*$ :  $\hat{y}^*\pm t_{\alpha/2,\ n-2}*S\sqrt{(1+\frac{1}{n}+\frac{(x^*-\bar{x})^2}{Sxx})}$

Note that One sample t-test for mean has statistic  $T = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ , where  $s = \sqrt{\frac{Sxx}{n-1}}$ , and the confidence interval is  $\bar{x} \pm t_{\alpha/2, n-1} * \frac{s}{\sqrt{n}}$ .