

Lab4

Lâm Nhật Tân - 2010597

Question 1: Given the main memory that has an address space of 32 bit, a cache with the size of 1 MB, 1 block is 256B, the accessing unit of the system is 1 byte. Determine the bit-width of tag, index, byte-offset with below configurations:

a. Directed map.

Block: $256\text{B} = 2^8 \text{ B}$

=> byte-offset: 8 bits

Cache: 1MB => Cache/Block: 2^{12} B

=> index: 12 bits

Tag: $32 - 8 - 12 = 12 \text{ bits}$

b. 4-way set associative.

Byte-offset (4-way) = byte-offset (directed map): 8 bits

Index (4-way) = index (directed map) / 4: 10 bits

Tag: $32 - 8 - 10 = 14 \text{ bits}$

c. Full associative.

Byte-offset (full associative) = byte-offset (directed map): 8 bits

Index (full associative) = 0 bits

Tag: $32 - 8 - 0 = 24 \text{ bits}$

Question 2: Given the main memory that has the capacity of 256MB, a cache with the size of 256KB, 1 block is 64 words, the accessing unit of the system is 2 bytes. Determine the bit-width of tag, index, byte-offset with below configurations:

- The capacity of $256\text{MB} = 2^{28} \text{ B}$ => an address space of 28 bits

a. Directed map.

“the accessing unit of the system is 2 bytes”

Block: 64 words = 2^8 B => byte-offset: 7 bits

Cache: 256KB => Cache/Block: 2^{10} B => index: 10 bits

Tag: $28 - 7 - 10 = 11 \text{ bits}$

b. 4-way set associative.

Byte-offset (4-way) = byte-offset (directed map) : 7 bits

Index (4-way) = index(directed map) / 4 : 8 bits

Tag: $28 - 7 - 8 = 13$ bits

c. Full associative

Byte-offset (full associative) = byte-offset (directed map) : 7 bits

Index (full associative) = 0 bits

Tag: $28 - 7 - 0 = 21$ bits

Question 3: A program accesses data in main memory with the sequence below (word address): 0, 4, 1, 5, 65, 46, 1, 70, 2, 0. Know that the system is 256B cache, 4-word block, 1-byte accessing unit. Hit time = 6 cycles, RAM (main memory) access time = 10ns, the system works with the frequency of 2GHz. Determine the number of HIT/MISS when executing the program, then calculate the AMAT (Average memory access time) with the below configurations:

- Hit time = $6 / 2 \times 10^9 = 3\text{ns}$

a. Directed map.

4-word block $\sim 2^4 \text{ B} \Rightarrow$ offset: 4 bits

256 B cache \Rightarrow cache/block = $2^4 \text{ B} \Rightarrow$ index: 4 bits

	TAG	INDEX	OFFSET	
0	0	0	0	M
4	0	1	0	M
1	0	0	4	H
5	0	1	4	H
65	1	0	4	M
46	0	11	8	M
1	0	0	4	M
70	1	1	8	M
2	0	0	8	H
0	0	0	0	H

Hit ratio = 4/10; Miss ratio = 6/10

AMAT = Hit time + Miss rate x Miss penalty = $3 + 6 / 10 \times 10 = 9\text{ns}$

b. 2-way set associative.

4-word block $\sim 2^4$ B \Rightarrow offset: 4 bits

256 B cache \Rightarrow cache/block = 2^4 B \Rightarrow index: 3 bits

	TAG	INDEX	OFFSET	
0	0	0	0	M
4	0	1	0	M
1	0	0	4	H
5	0	1	4	H
65	2	0	4	M
46	1	3	8	M
1	0	0	4	H
70	2	1	8	M
2	0	0	8	H
0	0	0	0	H

Hit ratio = 5/10; Miss ratio = 5/10

AMAT = Hit time + Miss rate x Miss penalty = $3 + 5 / 10 \times 10 = 8\text{ns}$

c. Full associative.

4-word block $\sim 2^4$ B \Rightarrow offset: 4 bits

index: 0 bits

	TAG	INDEX	OFFSET	
0	0	0	0	M
4	1	0	0	M
1	0	0	4	H
5	1	0	4	H
65	16	0	4	M
46	11	0	8	M
1	0	0	4	H
70	17	0	8	M
2	0	0	8	H
0	0	0	0	H

Hit ratio = 5/10; Miss ratio = 5/10

Hit time = $6 / 2 \times 10^9 = 3\text{ns}$

AMAT = Hit time + Miss rate x Miss penalty = $3 + 5 / 10 \times 10 = 8\text{ns}$

Question 4: Given L1 cache hit time is 10 cycles, L2 cache hit time is 15 cycles, time to access RAM (main memory) is 100 cycles. L1 miss rate is 25%, L2 miss rate is 5%. Determine AMAT of the system.

$$\begin{aligned}\text{AMAT} &= \text{Hit } t.1 + \text{Miss } r.1 \times (\text{Hit } t.2 + \text{Miss } r.2 \times \text{Miss penalty}) \\ &= 10 + 0.25 \times (15 + 0.05 \times 100) = 15\end{aligned}$$

Question 5: Determine average CPI of a pipeline system that its Instruction memory miss rate is 5% and its Data memory miss rate is 10%. Know that the program has 1000 instructions included 100 load/store instructions and miss penalty is 100 cycles.

$$\begin{aligned}\text{CPI} &= \text{CPI base} + \text{I-cache} + \text{D-cache} = 1004/1000 + 0.05 \times 100 + 0.1 \times 0.1 \times 100 \\ &= 7.004\end{aligned}$$