

Functional Programming

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- 1 **FP Introduction**
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Function are values, i.e., a function can be

	Value	Function
• Anonymous	3	$x \Rightarrow x + 1$
• Assigned to a variable	$x = 3$	$f = x \Rightarrow x + 1$
• Passed as input/output parameter	$f(3)$	$f(x \Rightarrow x + 1)$
• Created dynamically	$3 + 4$	$f \circ g$

- Imperative languages \Rightarrow Von Neumann Architecture
 - Efficiency
- Functional languages \Rightarrow Lambda Calculus
 - A solid theoretical basis that is also closer to the user, but
 - relatively unconcerned with the architecture of the machines on which programs will run

- A mathematical function is
 - a mapping of members of one set, called the domain set, to another set, called the range set
- A **lambda expression** specifies the **parameter(s)** and **an expression** in the following form **to express an anonymous function**

$\lambda(x) x * x * x$

like the function cube $\text{cube}(x) = x * x * x$

- Lambda expressions are **applied to parameter(s)** by **placing the parameter(s) after the expression**

$(\lambda(x) x * x * x)(2)$ which evaluates to 8

- A higher-order function is one that either takes functions as parameters or yields a function as its result, or both
- For example,
 - Function composition
 - Apply-to-all
 - Forall/Exists
 - Insert-left/Insert-right
 - Functions as parameters
 - Closures

A function that

- takes two functions as parameters and
- yields a function whose value is the first actual parameter function applied to the application of the second

$$f \circ g = f : (g : x)$$

$$\text{For } f(x) = x + 2; g(x) = x * x; f \circ g (x) = x * x + 2$$

Example in Scala,

```
val f = (x:Double) => x + 2
```

```
val g = (x:Double) => x * x
```

```
val h = f compose g
```

```
h(3)
```

```
val k = f andThen g
```

```
k(3)
```

A functional form that

- takes a single function as a parameter and
- yields a list of values obtained by applying the given function to each element of a list of parameters

$$\alpha f : \langle x_1, x_2, \dots, x_n \rangle = \langle f : x_1, f : x_2, \dots, f : x_n \rangle$$

For $h(x)=x*x \Rightarrow \alpha h:(1,2,3)$ yields $(1,4,9)$

Example in Scala,

```
List(2,3,4).map((x:Int) => x * x)
def inc (x:Int) = x + 1
List(4,5,6).map(inc)
```


A functional form that

- takes a single **predicate function** as a parameter and
- yields a value obtained by applying the given function to each element of a list of parameters and take the **and/or** of the results

$$\forall f : \langle x_1, x_2, \dots, x_n \rangle = \bigcap f : x_i$$
$$\exists f : \langle x_1, x_2, \dots, x_n \rangle = \bigcup f : x_i$$

Example in Scala,

```
def isEqualToThree(x:Int) = x == 3
List(2,3,4).forall(isEqualToThree)
// yield false
List(2,3,4).exists(isEqualToThree)
// yield true
```

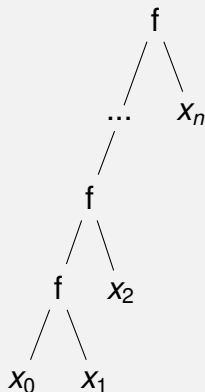
A functional form that

- takes a single **predicate function** as a parameter and
- yields a value that includes elements from the list parameter on which the given function returns true

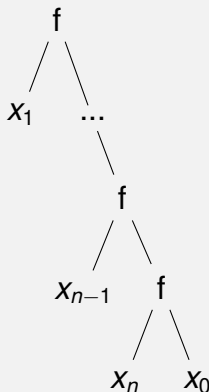
$$\beta f : \langle x_1, x_2, \dots, x_n \rangle = \langle x_i \mid f : x_i = T \rangle$$

Insert Left / Insert Right

$/f : \langle x_0 \rangle, \langle x_1, x_2, \dots, x_n \rangle$



$\backslash f : \langle x_0 \rangle, \langle x_1, x_2, \dots, x_n \rangle$



Example in Scala

```
List(2,3,4).foldLeft(0)((a,b) => a+b) // yield 9
List(2,3,4).foldLeft(1)((a,b) => a*b) // yield 24
List(2,3,4).foldLeft("A")((a,b) => a + b)
// yield "A234"
List(2,3,4).foldRight("A")((a,b) => a + b)
// yield "234A"
```

In user-defined functions, functions can be passed as parameters.

```
def apply(x:Int) (f:Int=>Int) = f(x)
val incl = (x:Int) => x + 1
val sq = (x:Int) => x * x
val fl = List(incl,sq)
fl.map(apply(3)) //yield List(4,9)
```

"An object is data with functions. A closure is a function with data." - John D. Cook

```
def power(exp:Double) =  
    (x:Double) => math.pow(x,exp)  
val square = power(2)  
square(4) //yield 16.0  
val cube = power(3)  
cube(3) //yield 27.0
```

Closure = function + binding of its free variables

$f : X_1 \times X_2 \times \dots \times X_n \rightarrow Y$

curry: $f : X_1 \rightarrow X_2 \rightarrow \dots \rightarrow X_n \rightarrow Y$

Example in Scala

```
def add(x:Int, y:Int) = x + y
```

```
add(1,3)
```

```
add(1) add(1) (3)
```

```
def plus(x:Int)(y:Int) = x + y
```

```
plus(1)(3)
```

```
val incl = plus(1) _
```

```
incl(3)
```

```
val addCurried = (add _).curried
```

```
val plusUncurried = Function.uncurried(plus _)
```

Read more on Partially Applied Functions [2]

- **Immutable: Cannot change**
- In Java, strings are immutable
"Hello".toUpperCase() doesn't change "Hello" but returns a new string "HELLO"
- In Scala, **val** is immutable
val num = 12
num = 10 // wrong
- **Pure functional programming: No mutations**
- Don't mutate—always return the result as a new value
- Functions that don't mutate state are inherently parallelizable

Example on Immutability

```
abstract class IntStack
  def push(x: Int): IntStack =
    new IntNonEmptyStack(x, this)
  def isEmpty: Boolean
  def top: Int
  def pop: IntStack
class StackEmpty extends IntStack
  def isEmpty = true
  def top = error("EmptyStack.top")
  def pop = error("EmptyStack.pop")
class IntNonEmptyStack(elem: Int, rest: IntStack)
  extends IntStack
  def isEmpty = false
  def top = elem
  def pop = rest
```

- Immutable Data Structures
- lambda function
- First-class functions
- High-order functions: map, filter, reduce
- Closure
- Decorator

This is a style of programming that avoids side effects by performing computation

- through the evaluation of pure functions
- relying heavily on immutable data structures

Benefits of functional programming:

- Pure functions are easier to reason about
- Testing is easier
- Debugging is easier
- Programs are more bulletproof
- Parallel/Concurrent programming is easier

- Apply immutable data types in Python
 - Number (int,float,complex)
 - Boolean (bool)
 - String (str)
 - Sequence (tuple, range)
(1,'a',True)
 - Set (frozenset)
x = frozenset({1,'a',True})
 - Mapping (collections.namedtuple)
Student = collections.namedtuple('Student',['name','age'])
x = Student('Vinh',14)
x.name
- Apply immutable operations on mutable data types
 - + instead of **extend()**
[1,2,3] + [4,5]

- Syntax:

lambda (<param> (, <param> *)?): <exp>

- For example,

lambda a,b: a + b

(**lambda** a,b: a + b) (3,4) => 7

x = **lambda** a,b: a + b

x(3,4) => 7

- Anonymous function
- Any number of parameters
- Body is just one expression
- Used in high-order functions

- A function is treated as any other value, i.e. it is

- assigned to a variable

```
def foo(a,b): pass
x = foo
x(3,4)
```

- passed into another function as a parameter

```
def foo(f,x):
    return f(x)
foo(lambda a: a ** 2, 4) => 16
```

- returned as a value

```
def f(x):
    def g(y):
        return x * y
    return g
m = f(3)
m(4) => 12
```

High-order functions: map, filter, reduce

- **map(<function>,<sequence>)**: apply <function> to each element of <sequence> and return an iterator

```
cels = [36.5, 37, 37.5, 38, 39]
```

```
fahr = list(map(lambda c: (float(9) / 5) * c  
+ 32, cels))
```

```
=> [97.7, 98.6, 99.5, 100.4, 102.2] list(map(lambda  
x,y: x + y, [1,2,3], [4,5,6,7])) => [5,7,9]
```

- **filter(<function>,<sequence>)** return an iterator that contains elements in <sequence> for which <function> returns True

```
list(filter(lambda c: c % 2 == 1, [0,1,2,3,4,5]  
[1,3,5])
```

- **reduce(<function>,<sequence>(<initial>))**: if <sequence> is $[s_1, s_2, s_3]$, **reduce** return $\text{function}(\text{function}(s_1, s_2), s_3)$ or $\text{function}(\text{function}(\text{function}(\text{<initial>}, s_1), s_2), s_3)$

```
from functools import reduce
```

- **Closure** is a **function object** together with an environment (binding of its **free data**).

```
def power(y):  
    def inner(x):  
        return x ** y  
    return inner  
square = power(2)  
square(5) => 25
```


- **Decorator** allows to **modify the behavior of function or class without permanently modifying it.**

```
@log_decorator
```

```
def foo(x,y):
```

```
    return x*y
```

```
print(foo(3,4)) => 12
```

- **How?**

```
=> 12
```

```
def log_decorator(func):
```

```
    def inner(*arg):
```

```
        print(func.__name__+" is running")
```

```
        return func(*arg)
```

```
    return inner
```

```
def foo(x,y):
```

```
    return x*y
```

```
foo = log_decorator(foo)
```

```
print(foo(3,4))
```

- Functional programming languages use **function application**, **conditional expressions**, **recursion**, and **functional forms** to control program execution instead of imperative features such as variables and assignments
- Purely functional languages have **advantages over imperative** alternatives, but their **lower efficiency on existing machine architectures** has prevented them from enjoying widespread use

- [1] **Methods and Closures**, <http://www.artima.com/pinsltd/functions-and-closures.html>, 19 06 2014.
- [2] **Function Currying in Scala**, <http://www.codecommit.com/blog/scala/function-currying-in-scala>, 19 06 2014.
- [3] **Case classes and pattern matching**,
<http://www.artima.com/pinsltd/case-classes-and-pattern-matching.html>, 19 06 2014.
- [4] **Control Abstraction**, <http://www.artima.com/pinsltd/control-abstraction.html>, 19 06 2014.