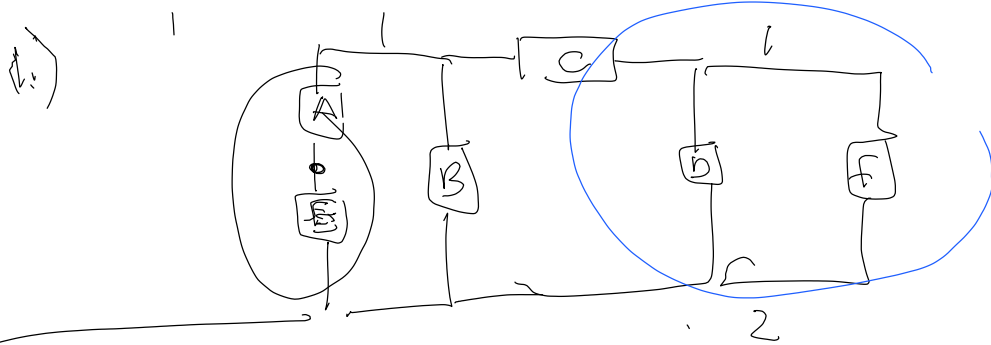
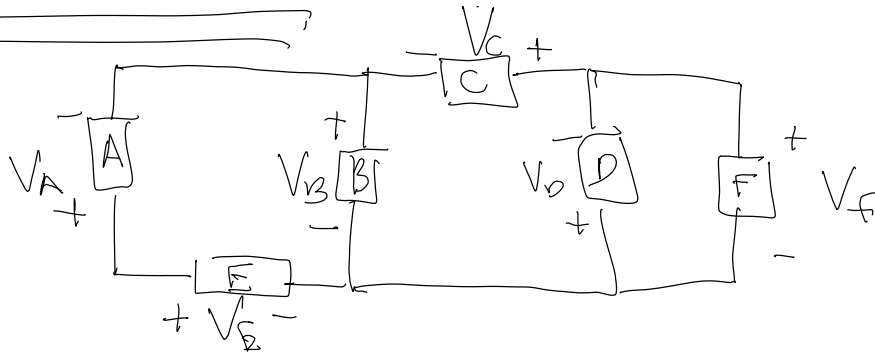


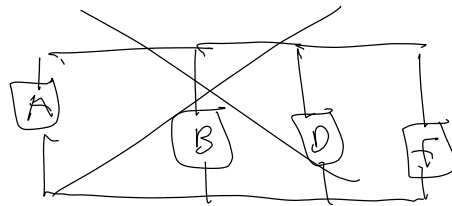
Discussion 1B (Week 1)

Thursday, April 1, 2021 8:52 AM

Review Quiz #2:



D & F
are in
parallel

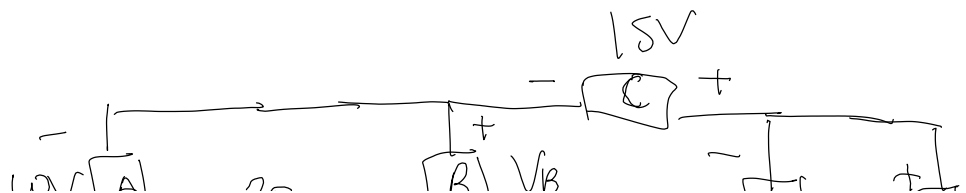


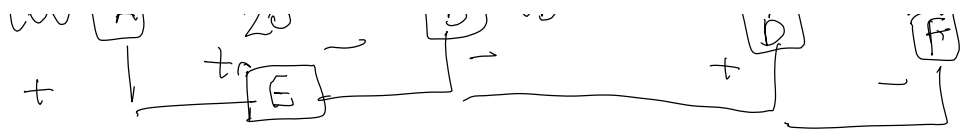
2) A & E are in series

3) Relationship between D & F

$$V_D = -V_F$$

4) $V_A = 10V$, $V_C = 15V$, $V_E = 20V$





$$\textcircled{1} \quad V_A + V_B - V_E = 0$$

$$V_B = V_E - V_A = 20 - 10 = \boxed{10V}$$

$$V_E = -V_D$$

$$\textcircled{2} \quad V_B + V_C + V_D = 0$$

$$10V + 15V + V_D = 0 \rightarrow V_D = -25V$$

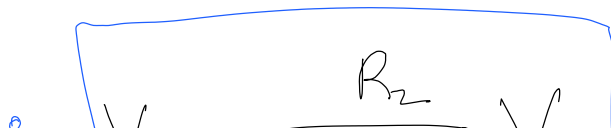
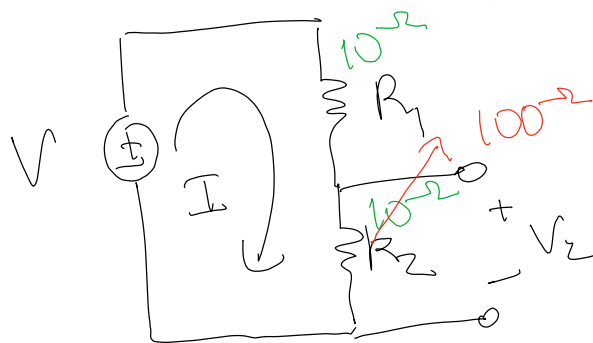
$$\boxed{V_E = 25V}$$

Theory

① Voltage Divider

$$\textcircled{1} \quad V = IR_1 + IR_2$$

$$V_2 = IR_2$$



$$V_2 = \frac{R_2}{R_1 + R_2} V$$

$$V = I(R_1 + R_2) \quad V_2 = IR_2$$

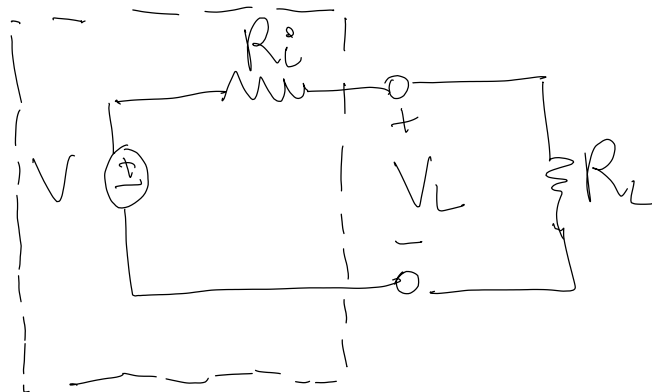
$$I = \frac{V}{R_1 + R_2} \quad I = \frac{V_2}{R_2}$$

$$\frac{V}{R_1 + R_2} = \frac{V_2}{R_2}$$

$$V_2 = \frac{10}{10+10} V = \frac{1}{2} V$$

$$V_2 = \frac{100}{10+100} V = \frac{10}{11} V$$

→ non-ideal battery

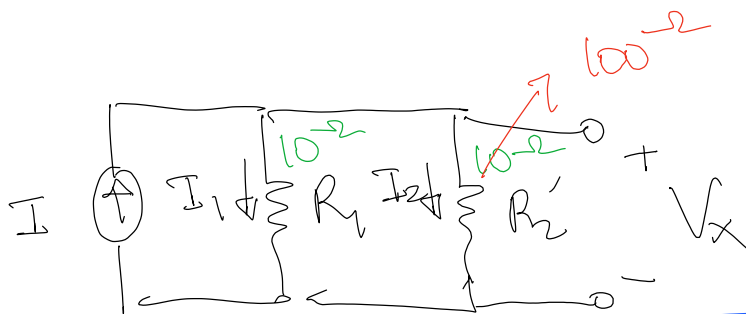


$$V_L = \frac{R_L}{R_L + R_i} V$$

$$\text{If } R_i \rightarrow \infty$$

$$V_L \rightarrow 0$$

② Current Divider



$$I_1 = \frac{R_2}{R_1 + R_2} I \quad I_2 = \frac{R_1}{R_1 + R_2} I$$

$$I = I_1 + I_2$$

$$V_x = I_1 R_1 = I_2 R_2$$

$$I_1 : \textcircled{1} I_1 = I - I_2 \quad \textcircled{2} I_2 = I_1 \frac{R_1}{R_2}$$

$$I_1 = I - \left(I_1 \frac{R_1}{R_2} \right)$$

$$I_1 \left(1 + \frac{R_1}{R_2} \right) = I$$

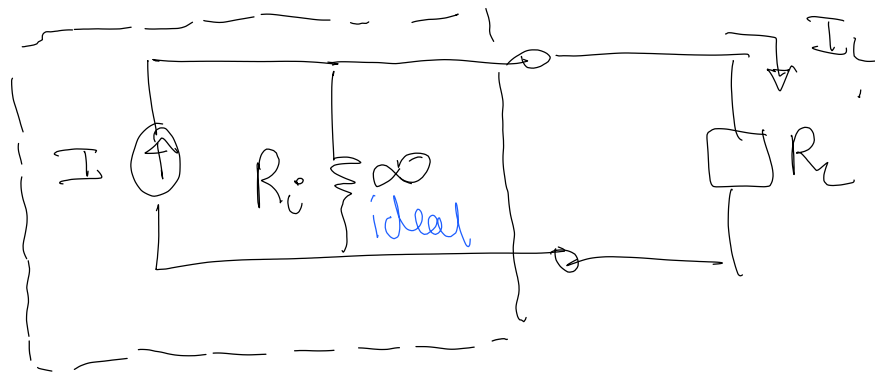
$$I_1 = \left(\frac{R_2}{R_1 + R_2} \right) I$$

$$I_1 = \frac{10}{10 + 10} I = \frac{1}{2} I$$

$$I_1 = \frac{100}{10+100} I = \frac{10}{11} I$$

Why? sometimes its easier to solve for a current in terms of another current (solve for I_1 in terms of

\Rightarrow current source



$$I_L = \frac{R_i}{R_i + R_L} I \rightarrow I_L \approx I$$

(Note: In the original image, R_i and $R_i + R_L$ are both crossed out with blue arrows pointing to ∞ .)

Problem 1

$$I_A = i_1 - i_3$$

KVL expressions

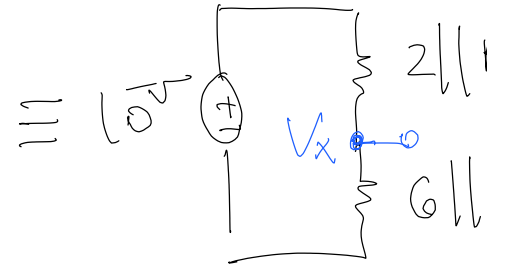
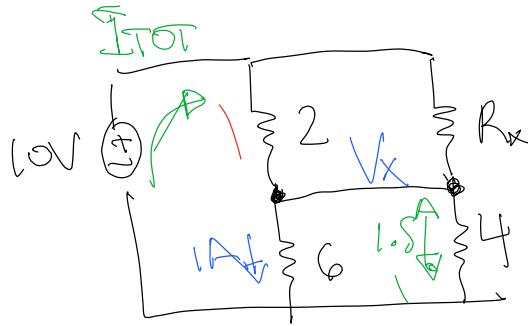


$$\begin{aligned} \textcircled{1} & 10V - i_1(2\Omega) - (\\ \textcircled{2} & -10V - (i_2 - i_3)4\Omega - \\ \textcircled{3} & (i_3 - i_2)4\Omega - i_3 \end{aligned}$$

(Note: The original image has some additional markings and a small diagram below the equations.)



$$R_1 \parallel R_2 \equiv R_K =$$

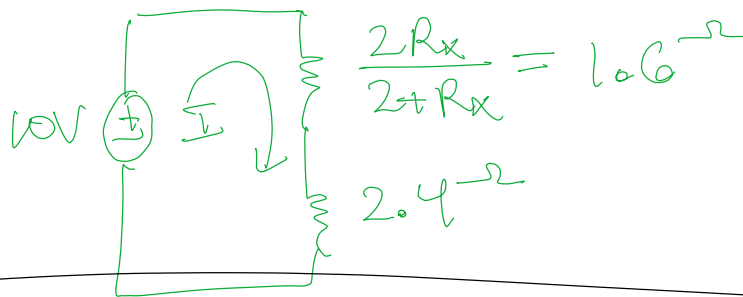


$$\frac{V_x}{4\Omega} = 1.5A \quad V_x = 1A \times 6\Omega = 6V$$

$$V_x = 6V = \frac{R_2}{R_1 + R_2} 10V$$

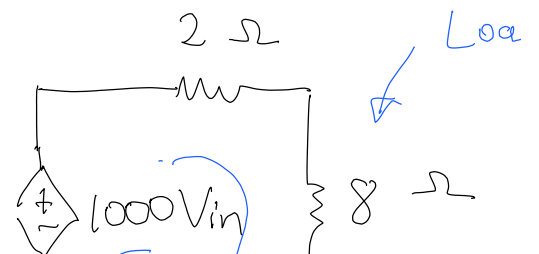
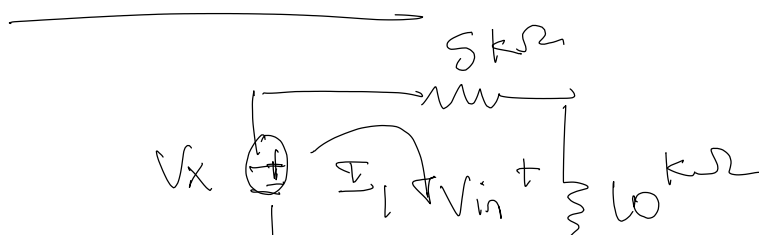
$$\frac{6V}{10V} = \frac{2.4\Omega}{2.4\Omega + \frac{2R_x}{2+R_x}} \rightarrow R_x$$

$$I_{TOT} = 1A + 1.5A = 2.5A$$



$$I = \frac{10V}{(1.6\Omega + 2.4\Omega)}$$

Problem 2





* 8W are delivered to the load (8Ω res)

$$P = I^2 R$$

$$\hookrightarrow I_2^2 = \frac{8W}{8\Omega} \rightarrow \boxed{I_2 = 1A}$$

$$\textcircled{2} \quad 1000V_{in} - I_2(2\Omega) - I_2(8\Omega) = 0$$

$$1000V_{in} = 10V$$

$$\rightarrow V_{in} = \frac{10V}{1000} = 10mV$$

* What must V_x (source) = ?

$$V = IR$$

$$I = \frac{V}{R}$$

$$V_{IN} = I_1(10k\Omega) = 10mV$$

$$I_1 = \frac{10mV}{10k\Omega} = 1\mu A$$

$$\textcircled{1} \quad V_x - I_1(5k\Omega) - I_1(10k\Omega) = 0$$

$$V_x = I_1(15k\Omega) = \boxed{15mV}$$