

4.40 a. $P(K) = .7$

b. $P(R|K) = 1$

c. $P(K|R) = \frac{P(R|K)P(K)}{P(R)} = \frac{.7 \cdot 1}{P(R)}$

$$\begin{aligned} P(R) &= P(R \cap K) + P(R \cap K^c) \\ &= .7 + P(R|K^c)P(K^c) \\ &= .7 + \frac{1}{n} \cdot .3 \end{aligned}$$

$$P(K|R) = \frac{.7}{.7 + \frac{1}{n} \cdot .3}$$

d. $P(K|R) = \frac{.7}{.7 + \frac{1}{n} \cdot .3} \geq .99$

$$\begin{aligned} .7 &\geq .643 + .297 \frac{1}{n} \\ \frac{1}{n} &\leq .0236 \\ n &\geq 42.4 \end{aligned}$$

$$n_{\min} = 43 \text{ options}$$

4.41 r_3 isn't random. By the definition of r_3 , revealing a goat in door 2 guarantees a car behind door one. Thus, ~~$P(C_1|G_2, r_3)$~~ $P(C_1|G_2, r_3) = \boxed{1 \text{ or } 100\%}$

4.42 $P(C_1|G_2, r_4) = \frac{P(C_1 \cap G_2)}{P(G_2 \cap C_1) + P(G_2 \cap C_2) + P(G_2 \cap C_3)}$

$$\begin{aligned} &= \frac{P(G_2|C_1) \cdot P(C_1)}{P(G_2|C_1)P(C_1) + 0 + P(G_2|C_3)P(C_3)} \\ &= \frac{\frac{1}{6}}{\frac{1}{6} + \frac{1}{6}} = \boxed{\frac{1}{2}} \end{aligned}$$