

2. Implementation - 1

```
def fibonacci_1(n):
```

```
    if n <= 0:
```

```
        print('Invalid input')
```

```
    elif n <= 2:
```

```
        return n-1
```

```
    else:
```

```
        return fibonacci_1(n-1) + fibonacci_1(n-2)
```

$$\begin{aligned} T(n) &= T(n-1) + T(n-2) + 1 \\ &= 2T(n-1) + 1 \quad [T(n-1) \approx T(n-2)] \\ &= 2 \{ 2T(n-2) + 1 \} + 1 \\ &= 2^2 T(n-2) + 2^1 + 2^0 \\ &= 2^2 \{ 2T(n-3) + 1 \} + 2^1 + 2^0 \\ &= 2^3 T(n-3) + 2^2 + 2^1 + 2^0 \end{aligned}$$

$$\begin{aligned} T(n+2) &= 2^{n+2} T(n-n+2) + 2^{n+1} + \dots + 2^0 \\ &= 2^{n+2} \cdot 1 + 2^{n+1} + \dots + 2^0 \\ &= 2^{n+2} - 1 \\ &= 2^n \cdot 2 - 1 \\ &= O(2^n) \end{aligned}$$

Implementation - 2

def fibonacci_2(n):

fibonacci_array = [0, 1] } $O(1)$

if $n < 0$:

print('Invalid input!') } $O(1)$

elif $n \leq 2$:

return fibonacci_array[n-1] } $O(1)$

else:

for i in range(2, n):

$O(1) \times n$ { fibonacci_array.append (fibonacci_array
[i-1] + fibonacci_array[i-2])
= $O(n)$ return fibonacci_array[-1]

Time complexity = $O(1) + O(n)$
= $O(n)$

4.
$$\left. \begin{array}{l} \text{for } i=0 \text{ to } n-1 \\ \quad \left\{ \begin{array}{l} \text{for } j=0 \text{ to } n-1 \\ \quad \text{for } k=0 \text{ to } n-1 \\ \quad \quad C[i,j] += A[i,k] * B[k,j] \end{array} \right\} O(n) \\ \quad \text{end for } \\ \text{end for } \\ \text{end for} \end{array} \right\} O(n)$$

Time complexity = $O(n(n(n)))$
 $= O(n^3)$