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# This script plots the frequency response of a low-pass filter and transformed versions
import numpy as np
import matplotlib.pyplot as plt
# frequency array
w_array = np.arange(-np.pi, np.pi + 1, 0.01)
# low-pass filter
H1p = []
for w in w_array:
  if np.abs(w) < 0.2 * np.pi:
     H1p.append(1)
  else:
     H1p.append(0)
# plot low-pass filter
plt.plot(w_array, H1p)
plt.xlim(-np.pi, np.pi)
plt.ylim(0, 1.5)
plt.xlabel('$\omega$')
plt.ylabel('$H(e^{j\omega})$')
plt.show()
# part (a)
H1 = []
for w in w_array:
  if (np.abs(w) < 1.2 * np.pi) and (np.abs(w) > 0.8 * np.pi):
     H1.append(1)
  else:
     H1.append(0)
# plot H1
plt.plot(w_array, H1)
plt.xlim(-np.pi, np.pi)
plt.ylim(0, 1.5)
plt.xlabel('$\omega$')
plt.ylabel('$H(e^{j\omega})$')
plt.show()
# part (b)
H2 = []
for w in w_array:
  if (np.abs(w) < 0.7 * np.pi) and (np.abs(w) > 0.3 * np.pi):
     H2.append(1)
  else:
     H2.append(0)
# plot H2
plt.plot(w_array, H2)
plt.xlim(-np.pi, np.pi)
plt.ylim(0, 1.5)
plt.xlabel('$\omega$')
plt.ylabel('$H(e^{j\omega})$')
plt.show()
# part (c)
H3 = []
for w in w_array:
  if (np.abs(w) < 0.1 * np.pi):
     H3.append(0.1)
  elif (w >= -0.3 * \text{ np.pi}) and (w <= -0.1 * \text{ np.pi}):
     H3.append(w / (2 * np.pi) + 0.15)
  elif (w >= 0.1 * np.pi) and (w <= 0.3 * np.pi):
     H3.append(-w / (2 * np.pi) + 0.15)
  else:
     H3.append(0)
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plot H3 plt.plot(w_array, H3) plt.xlim(-np.pi, np.pi) plt.ylim(0, 0.15) plt.xlabel('\$\omega\$') plt.ylabel('\$H(e^{j\omega})\$') plt.show()