



## Introduction

✓ **Video:** Introduction to module 2 - Vectors  
49 sec

## Finding the size of a vector, its angle, and projection

✓ **Video:** Modulus & inner product  
10 min

✓ **Video:** Cosine & dot product  
5 min

✓ **Video:** Projection  
6 min

✓ **Practice Quiz:** Dot product of vectors  
6 questions

## Changing the reference frame

▶ **Video:** Changing basis  
11 min

📖 **Practice Quiz:** Changing basis  
5 questions

▶ **Video:** Basis, vector space, and linear independence  
4 min

▶ **Video:** Applications of changing basis  
3 min

📖 **Practice Quiz:** Linear dependency of a set of vectors  
6 questions

## Doing some real-world vectors examples

📖 **Quiz:** Vector operations assessment  
5 questions

▶ **Video:** Summary  
1 min



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## Dot product of vectors

## Dot product of vectors

TOTAL POINTS 6

1. As we have seen in the **Submit your assignment** video, the dot product of vectors has a lot of applications. Here, you will complete some exercises involving the dot product.

1 / 1 point

Try again

We have seen that the size of a vector with two components is calculated using Pythagoras' theorem, for example the

following diagram shows how we calculate the size of the orange vector  $\mathbf{r} = \begin{bmatrix} r_1 \\ r_2 \end{bmatrix}$ :

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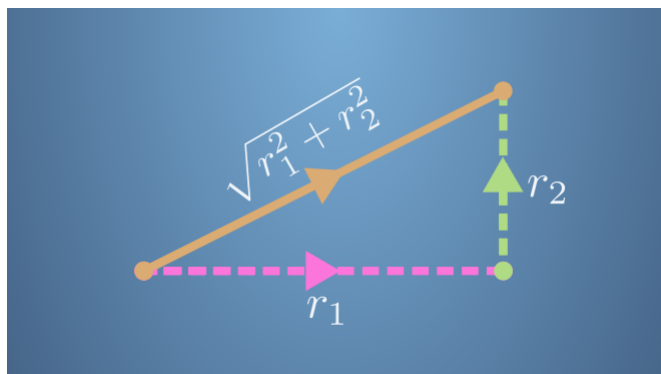
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In fact, this definition can be extended to any number of dimensions; the size of a vector is the square root of the sum of

the squares of its components. Using this information, what is the size of the vector  $\mathbf{s} = \begin{bmatrix} 1 \\ 3 \\ 4 \\ 2 \end{bmatrix}$ ?

☐  $|\mathbf{s}| = 10$ ☒  $|\mathbf{s}| = \sqrt{30}$ ☐  $|\mathbf{s}| = \sqrt{10}$ ☐  $|\mathbf{s}| = 30$ ✓ **Correct**

The size of the vector is the square root of the sum of the squares of the components.

2. Remember the definition of the dot product from the videos. For two  $n$  component vectors,  $\mathbf{a} \cdot \mathbf{b} = a_1b_1 + a_2b_2 + \dots + a_nb_n$ .

1 / 1 point

What is the dot product of the vectors  $\mathbf{r} = \begin{bmatrix} -5 \\ 3 \\ 2 \\ 8 \end{bmatrix}$  and  $\mathbf{s} = \begin{bmatrix} 1 \\ 2 \\ -1 \\ 0 \end{bmatrix}$ ?

☐  $\mathbf{r} \cdot \mathbf{s} = \begin{bmatrix} -5 \\ 6 \\ -2 \\ 0 \end{bmatrix}$ ☐  $\mathbf{r} \cdot \mathbf{s} = \begin{bmatrix} -4 \\ 5 \\ 1 \\ 9 \end{bmatrix}$ ☒  $\mathbf{r} \cdot \mathbf{s} = -1$ ☐  $\mathbf{r} \cdot \mathbf{s} = 1$ ✓ **Correct**

The dot product of two vectors is the total of the component-wise products.

3. The lectures introduced the idea of projecting one vector onto another. The following diagram shows the projection of  $\mathbf{s}$  onto  $\mathbf{r}$  when the vectors are in two dimensions:

1 / 1 point

