

Introduction

Finding the size of a vector, its angle, and projection

- ✓ **Video:** Modulus & inner product 10 min
- ✓ **Video:** Cosine & dot product 5 min
- ✓ **Video:** Projection 6 min
- ✓ **Practice Quiz:** Dot product of vectors 6 questions

Changing the reference frame

- ✓ **Video:** Changing basis 11 min
- ✓ **Practice Quiz:** Changing basis 5 questions
- ✓ **Video:** Basis, vector space, and linear independence 4 min
- ▶ **Video:** Applications of changing basis 3 min

- ✓ **Practice Quiz:** Linear dependency of a set of vectors 6 questions

Doing some real-world vectors examples



Congratulations! You passed!

TO PASS 80% or higher PRACTICE QUIZ • 15 MIN

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GRADE
100%

Linear dependency of a set of vectors

Linear dependency of a set of vectors

TOTAL POINTS 6

1. In the lecture video, you saw that two vectors are linearly dependent if it is possible to write one vector as a linear combination of the others. For example, the vectors **a**, **b** and **c** are linearly dependent if $\mathbf{a} = q_1 \mathbf{b} + q_2 \mathbf{c}$ where q_1 and q_2 are scalars.

1 / 1 point

Try again

Are the following vectors linearly dependent?

Receive grade

$$\mathbf{a} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \text{ and } \mathbf{b} = \begin{bmatrix} 2 \\ 2 \end{bmatrix}.$$

☒ Yes

☐ No

Grade
100%

View Feedback

We keep your highest score



✓ **Correct**

When there are two vectors we only need to check if one can be written as a scalar multiple of the other. We can see that the vectors are linearly dependent because $\mathbf{a} = \frac{1}{2} \mathbf{b}$.

2. We say that two vectors are linearly independent if they are *not* linearly dependent, that is, we cannot write one of the vectors as a linear combination of the others. Be careful not to mix the two definitions up!

1 / 1 point

Are the following vectors linearly independent?

$$\mathbf{a} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \text{ and } \mathbf{b} = \begin{bmatrix} 2 \\ 1 \end{bmatrix}.$$

☒ Yes

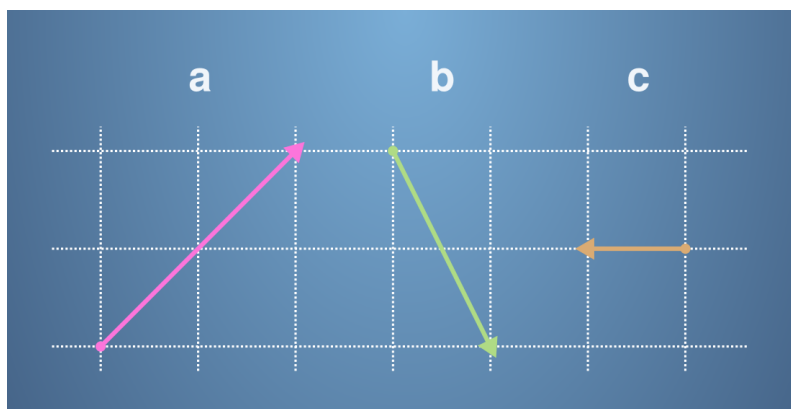
☐ No

✓ **Correct**

These vectors are linearly independent as one is not a scalar multiple of the other.

3. We also saw in the lectures that three vectors that lie in the same two dimensional plane must be linearly dependent. This tells us that **a**, **b** and **c** are linearly dependent in the following diagram:

1 / 1 point



What are the values of q_1 and q_2 that allow us to write $\mathbf{a} = q_1 \mathbf{b} + q_2 \mathbf{c}$? Put your answer in the following codeblock:

```
1 # Assign the correct values for q1 and q2 to write a as a linear combination of b and c
2 q1 = -1
3 q2 = -3
```

Run

Reset

✓ **Correct**

Good job!

4. In fact, an n -dimensional space can have as many as n linearly independent vectors. The following three vectors are three dimensional, which means that we must check if they are linearly dependent or independent.

1 / 1 point

Are the following vectors linearly independent?

$$\mathbf{a} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} \text{ and } \mathbf{c} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$$

☒ Yes