

Introduction

Finding the size of a vector, its angle, and projection

Changing the reference frame

✓ **Video:** Changing basis  
11 min

📋 **Practice Quiz:** Changing basis  
5 questions

▶ **Video:** Basis, vector space, and linear independence  
4 min

▶ **Video:** Applications of changing basis  
3 min

📋 **Practice Quiz:** Linear dependency of a set of vectors  
6 questions

Doing some real-world vectors examples



**Congratulations! You passed!**

TO PASS 80% or higher PRACTICE QUIZ • 15 MIN

Keep Learning

GRADE  
100%

## Changing basis

### Changing basis

TOTAL POINTS 5

1. In this quiz, you will practice changing from the standard basis to a basis consisting of orthogonal vectors.

1 / 1 point

Try again

Given vectors  $\mathbf{v} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$ ,  $\mathbf{b}_1 = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$  and  $\mathbf{b}_2 = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$  all written in the standard basis, what is  $\mathbf{v}$  in the basis defined by  $\mathbf{b}_1$  and  $\mathbf{b}_2$ ? You are given that  $\mathbf{b}_1$  and  $\mathbf{b}_2$  are orthogonal to each other.

Grade  
100%

View Feedback

We keep your highest score

☒  $\mathbf{v}_b = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} -3 \\ 2 \end{bmatrix}$

✓ **Correct**

The vector  $\mathbf{v}$  is projected onto the two vectors  $\mathbf{b}_1$  and  $\mathbf{b}_2$ .

2. Given vectors  $\mathbf{v} = \begin{bmatrix} 10 \\ -5 \end{bmatrix}$ ,  $\mathbf{b}_1 = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$  and  $\mathbf{b}_2 = \begin{bmatrix} 4 \\ -3 \end{bmatrix}$  all written in the standard basis, what is  $\mathbf{v}$  in the basis defined by  $\mathbf{b}_1$  and  $\mathbf{b}_2$ ? You are given that  $\mathbf{b}_1$  and  $\mathbf{b}_2$  are orthogonal to each other.

1 / 1 point

☐  $\mathbf{v}_b = \begin{bmatrix} 11/5 \\ 2/5 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} -2/5 \\ 11/5 \end{bmatrix}$

☒  $\mathbf{v}_b = \begin{bmatrix} 2/5 \\ 11/5 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} 2 \\ 11 \end{bmatrix}$

✓ **Correct**

The vector  $\mathbf{v}$  is projected onto the two vectors  $\mathbf{b}_1$  and  $\mathbf{b}_2$ .

3. Given vectors  $\mathbf{v} = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ ,  $\mathbf{b}_1 = \begin{bmatrix} -3 \\ 1 \end{bmatrix}$  and  $\mathbf{b}_2 = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$  all written in the standard basis, what is  $\mathbf{v}$  in the basis defined by  $\mathbf{b}_1$  and  $\mathbf{b}_2$ ? You are given that  $\mathbf{b}_1$  and  $\mathbf{b}_2$  are orthogonal to each other.

1 / 1 point

☐  $\mathbf{v}_b = \begin{bmatrix} 2/5 \\ -4/5 \end{bmatrix}$

☒  $\mathbf{v}_b = \begin{bmatrix} -2/5 \\ 4/5 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} 5/4 \\ -5/2 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} -2/5 \\ 5/4 \end{bmatrix}$

✓ **Correct**

The vector  $\mathbf{v}$  is projected onto the two vectors  $\mathbf{b}_1$  and  $\mathbf{b}_2$ .

4. Given vectors  $\mathbf{v} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ ,  $\mathbf{b}_1 = \begin{bmatrix} 2 \\ 1 \\ 0 \end{bmatrix}$ ,  $\mathbf{b}_2 = \begin{bmatrix} 1 \\ -2 \\ -1 \end{bmatrix}$  and  $\mathbf{b}_3 = \begin{bmatrix} -1 \\ 2 \\ -5 \end{bmatrix}$  all written in the standard basis, what is  $\mathbf{v}$  in the basis defined by  $\mathbf{b}_1$ ,  $\mathbf{b}_2$  and  $\mathbf{b}_3$ ? You are given that  $\mathbf{b}_1$ ,  $\mathbf{b}_2$  and  $\mathbf{b}_3$  are all pairwise orthogonal to each other.

1 / 1 point

☐  $\mathbf{v}_b = \begin{bmatrix} -3/5 \\ -1/3 \\ 2/15 \end{bmatrix}$

☐  $\mathbf{v}_b = \begin{bmatrix} -3/5 \\ -1/3 \\ -2/15 \end{bmatrix}$

☒  $\mathbf{v}_b = \begin{bmatrix} 3/5 \\ -1/3 \\ -2/15 \end{bmatrix}$